

# Nonrelativistic QCD and X(3872)

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**Zhejiang University, Hangzhou, Nov.8-11**

## 1. NRQCD and Heavy Quarkonium

Nonrelativistic hadron system

Separate scales  $m$ ,  $mv$ ,  $mv^2$ ,  $\Lambda_{\text{QCD}}$  with  $v^2 \ll 1$   $\square$   $\square 1$

Effective theory, Factorization of short- distance and long- distance parts

Experimental challenges from LHC data

How to understand production and decay

Important test ground for QCD and hadron physics

## 2. New hadron states—XYZ

$X(3872)$ ,  $Y(4260)$ ,  $Z(4430)$ , ...  $Z(3900)$ ,  $Z(4020)$ , ...

What is the nature of XYZ: Hadronic molecules, 4-quark states, Hybrids, threshold effects?

What is the relation of XYZ to conventional quarkonia?

# Interpretations of $X(3872)$ and Its Production at Hadron Colliders

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**In Collaboration with C. Meng & H. Han**

# Outline

- Mini review of  $X(3872)$
- $X$  production at hadron colliders
- $X$  decays to  $J/\psi\gamma$  and  $\psi(2S)\gamma$
- $X$  production in B meson decays
- Summary

# Experimental information

- 1<sup>st</sup> observed by Belle Collaboration in

$$B \rightarrow J/\psi \pi^+ \pi^- K$$

Belle'03

- Mass, width and quantum numbers:

- $m_X = 3871.68 \pm 0.17 \text{ MeV}$

PDG'12

- $m_X - m_{D^0 D^{*0}} = -0.142 \pm 0.220 \text{ MeV}$   
*al.'12*

Tomaradze *et al.*'12

- $\Gamma < 1.2 \text{ MeV}$     CL = 90%

PDG'12

- $J^{PC} = 1^{++}$  or  $2^{-+}$

- ✓  $J^{PC} = 2^{-+}$  is favored by the  $\omega \rightarrow \pi^+ \pi^- \pi^0$  mass spectrum in

$B \rightarrow X(3872)K \rightarrow J/\psi \omega (\pi^+ \pi^- \pi^0) K$  [BaBar'10], but **is**

**excluded** by the recent analysis on the angular correlations in

$B \rightarrow X(3872)K \rightarrow J/\psi \rho (\pi^+ \pi^-) K$  by LHCb [arXiv:1302.6269]

# Experimental information

➤ Decay pattern:

- Well-established decay modes:

$$J/\psi\rho(\pi^+\pi^-), J/\psi\omega(\pi^+\pi^-\pi^0), D^0\bar{D}^{*0}/\bar{D}^0D^{*0}/D\bar{D}\pi, J/\psi\gamma$$

Relative ratios of these 4 modes: **1:1:10:0.3** PDG'12

✓ Large isospin violations

$$R_{\rho/\omega} = \text{Br}(X \rightarrow J/\psi\rho)/\text{Br}(X \rightarrow J/\psi\omega) \approx 1$$

✓  $\text{Br}(X \rightarrow J/\psi\rho) = \text{Br}(X \rightarrow J/\psi\pi^+\pi^-) \equiv \text{Br}_0 < 9\%$

➤ B-production:

$$1 \times 10^{-4} < \text{Br}(B \rightarrow X(3872)K) < 3.2 \times 10^{-4} \quad \text{BaBar'05}$$

$$\text{Br}(B \rightarrow X(3872)K)\text{Br}_0 = (8.6 \pm 0.8) \times 10^{-6} \quad \text{PDG'12}$$

$$2.6\% < \text{Br}_0 < 9\%$$

# Experimental information

## ➤ Hadro-production

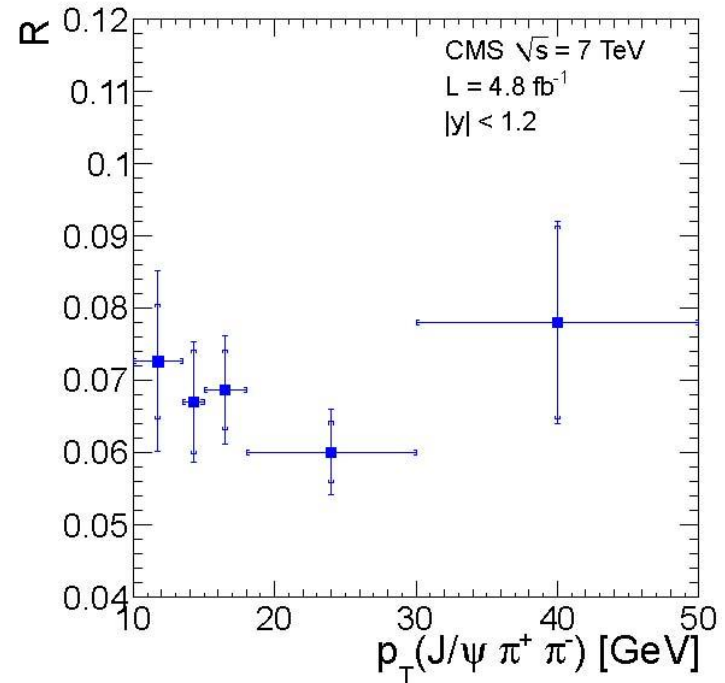
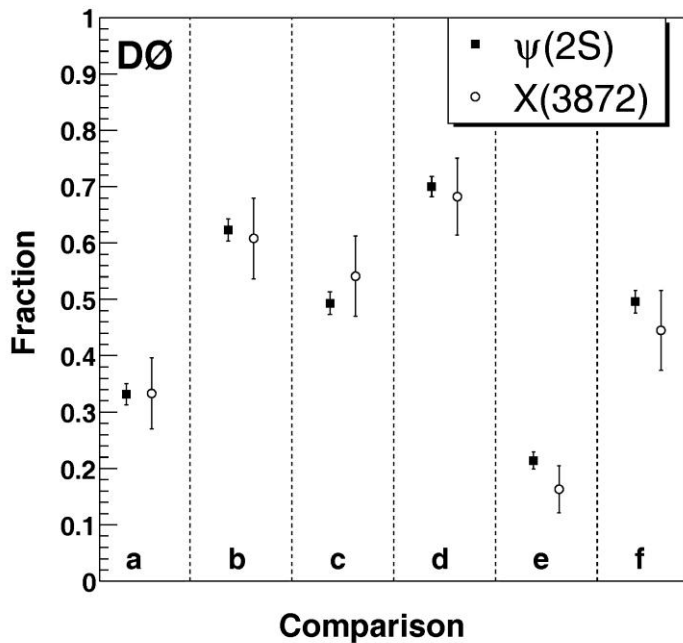
- Large production rate:  $\frac{\sigma(p\bar{p}\rightarrow X)Br_0}{\sigma(p\bar{p}\rightarrow\psi')} \frac{\epsilon_{\psi'}}{\epsilon_X} = (4.8 \pm 0.8)\%$  CDF'04
- Similar behaviors to  $\psi'$  production in  $p_T$  distribution and ...

D0 PRL'04

CMS arXiv:1302.3968

a.  $p_T > 15$  GeV b. ...

Ratio to  $\psi'$  is not depend on  $p_T$



# $D^0 \bar{D}^{*0}$ molecule models

[Tornqvist'04, Voloshin'04, Swanson'04, Braaten'04, ...]

- $X(3872)$  is a loosely bound state of  $D^0 \bar{D}^{*0} / \bar{D}^0 D^{*0}$ 
  - The mass, quantum numbers and the large isospin violation can be understood naturally.
  - The large production rate seems to be questionable
- ✓ Naively,  $\sigma(X) \sim k_0^3$ , where the relative momentum of  $D^0 \bar{D}^{*0}$  in the bound state  $k_0 = \sqrt{2\mu_{D\bar{D}^*} |E_b|} < 40$  MeV
- ✓ Explicit calculations [Bignamini *et al*, PRL'09]:  
 $\sigma_{\text{CDF}}^{\text{th}}(X) < 0.085$  nb *v.s.*  $\sigma_{\text{CDF}}^{\text{ex}}(X)_{\text{Br}_0} = 3.1 \pm 0.7$  nb
- ✓ Artoisenet and Braaten [PRD'10] proposed that rescattering effects of  $D^0 \bar{D}^{*0}$  may enhance the rate to values consistent with the CDF data if the upper bound of the relative momentum of  $D^0 \bar{D}^{*0}$  in rescattering is as large as  $3m_\pi \approx 400$  MeV



# $\chi'_{c1} - D^0 \bar{D}^{*0}$ mixing model

Meng, Gao and Chao, hep-ph/0506222, PRD87(2013)074035

- $X(3872)$  is a mixed state of  $\chi'_{c1}$  and  $D^0 \bar{D}^{*0} / \bar{D}^0 D^{*0}$  continuum
- Both the two components are substantial, and they may play different roles in the dynamics of  $X(3872)$ .
  1. The short distance (the  $b$ - and  $hadro$ -) production and the quark annihilation decays of  $X(3872)$  proceed dominantly through the  $\chi'_{c1}$  component.
  2. The  $D^0 \bar{D}^{*0}$  component is mainly in charge of the hadronic decays of  $X(3872)$  into  $DD\pi/DD\gamma$  as well as  $J/\psi\rho$  and  $J/\psi\omega$ .
  3. The long distance coupled-channel effects between the two components could renormalize the short distance dynamics by a product factor  $Z_{c\bar{c}}$ , the equivalent probability of  $\chi'_{c1}$  in  $X(3872)$ .

# $\chi'_{c1} - D^0 \bar{D}^{*0}$ mixing model

- $B$  production rate: Meng, Gao and Chao'05

$$\frac{\text{Br}(B \rightarrow \chi'_{c1} K)}{\text{Br}(B \rightarrow \chi_{c1} K)} = 0.75 - 1$$

$$\text{Br}(B \rightarrow \chi'_{c1} K) = (2-4) \times 10^{-4}$$

- Rescattering of the  $D^0 \bar{D}^{*0}$  and  $D^+ \bar{D}^{*-}$  (*virtual*) components:  
Meng and Chao, PRD'07

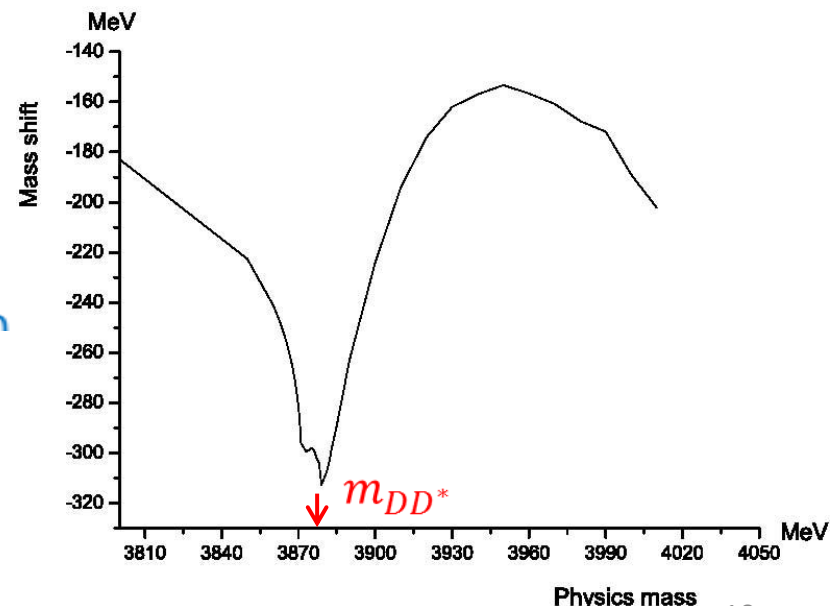
$$\frac{\text{Br}(X \rightarrow J/\psi \rho)}{\text{Br}(X \rightarrow J/\psi \omega)} = 0.9 - 1.2$$

- Mass problem:

Coupled-channel models

Li & Meng & Chao'09; Danilkin & Simenov'10

The sharp mass shift curve induced by the S-wave coupling lower the "bare" mass of  $\chi'_{c1}$  towards the  $D^0 \bar{D}^{*0}$  threshold.



# X production at hadron colliders

# NRQCD factorization formula

- $\chi'_{c1}$  production mechanism in the mixing model:

[Meng & Han & Chao, arXiv:1304.6710]

[Similar work was done by Butenschoen & He & Kniehl, arXiv: 1303.3524]

- Energy scales:  $m_c \gg m_c v, m_c v^2, \Lambda_{QCD} \gg E_b$
- Assume  $X$  is produced at short-distance via the  $\chi'_{c1}$  component  
 $\sigma(pp \rightarrow X(J/\psi\pi^+\pi^-)) = \sigma(pp \rightarrow \chi'_{c1}) \cdot k, \quad k = Z_{c\bar{c}} Br_0$
- Factorization in NRQCD Bodwin & Braaten & Lepage'95

$$d\sigma(pp \rightarrow \chi'_{c1}) = \sum_n d\hat{\sigma}((c\bar{c})_n) \frac{\langle O_n^{\chi'_{c1}} \rangle}{m_c^{2L_n}}$$

$$= \sum_{i,j,n} \int dx_1 dx_2 G_{i/p} G_{j/p} d\hat{\sigma}(ij \rightarrow (c\bar{c})_n) \langle O_n^{\chi'_{c1}} \rangle$$

$n = {}^3P_1^{[1]} \& {}^3S_1^{[8]}$  at leading order in  $v$  for  $\chi'_{c1}$  production

# NRQCD factorization formula

- **Molecule production mechanism** in the molecule model:

Artoisenet & Braaten, PRD'09

$$d\sigma(pp \rightarrow X_{D^0\bar{D}^{*0}}) = d\hat{\sigma}\left({}^3S_1^{[1]}\right) \left\langle O_{3S_1^{[1]}}^{D^0\bar{D}^{*0}} \right\rangle + d\hat{\sigma}\left({}^3S_1^{[8]}\right) \left\langle O_{3S_1^{[8]}}^{D^0\bar{D}^{*0}} \right\rangle$$

At NLO in  $\alpha_s$ :  $d\hat{\sigma}\left({}^3S_1^{[1]}\right) / d\hat{\sigma}\left({}^3S_1^{[8]}\right) \approx 5.3 \times 10^{-4}$  for CDF widow, thus [Meng & Han & Chao, arXiv:1304.6710]

$$d\sigma(pp \rightarrow X_{D^0\bar{D}^{*0}}) = d\hat{\sigma}\left({}^3S_1^{[8]}\right) \left\langle O_{3S_1^{[8]}}^{D^0\bar{D}^{*0}} \right\rangle$$

- ✓ The two models are different in combinations of the  $c\bar{c}$  channels in the factorization formula, leading to different CMS pT distributions.
- ✓ The  $\chi'_{c1}$  production is similar to  $\chi_{c1}$ , and therefore large production rate is expected (like  $\psi(2S)$  and  $J/\psi$ ).

# NRQCD factorization formula

## ➤ NLO calculations:

- We choose  $\mu_r = \mu_f = m_T = \sqrt{p_T^2 + 4m_c^2}$ ,  $\mu_{NR} = m_c = 1.5 \pm 0.1$  GeV, and vary  $\mu_{r,f}$  from  $m_T/2$  to  $m_T$  to estimate the errors.
- The other details can be found in [Ma & Wang & Chao'11 \(MWC'11\)](#)

## ➤ To compare our following results with the available ones for $\chi_{c1}$ production [[MWC'11](#)], we parameterize the matrix elements as

- $\left\langle O_{3P_1^{[1]}}^{\chi'_{c1}} \right\rangle = \left\langle O_{3P_1^{[1]}}^{\chi_{c1}} \right\rangle = \frac{9}{4\pi} |R'_{1P}(0)|^2, |R'_{1P}(0)|^2 = 0.075 \text{ GeV}^5$

- $r = m_c^2 \left\langle O_{3S_1^{[8]}}^{\chi'_{c1}} \right\rangle / \left\langle O_{3P_1^{[1]}}^{\chi'_{c1}} \right\rangle \quad (r_{1P} = 0.27 \pm 0.06, \text{MWC'11})$

- The cross section in the  $\chi'_{c1}$  production mechanism is a simple function of  $r$ ,  $k$  and  $p_T$

# Fit to the CMS $p_T$ distribution

$$\sqrt{s} = 7 \text{ TeV}, \quad |y| > 1.2, \quad 10 \text{ GeV} < p_T < 30 \text{ GeV}$$

➤  $\chi'_{c1}$  production mechanism:

$$r = 0.26 \pm 0.07, \quad k = 0.014 \pm 0.006$$

$$\sigma_{\text{CMS}}^{\text{fit}}(pp\bar{p} \rightarrow X(J/\psi\pi^+\pi^-)) = 1.09^{+0.08}_{-0.12} \text{ nb} \quad ((1.06 \pm 0.19 \text{ nb})_{\text{ex}})$$

- The central values correspond  $\chi^2/2 = 0.26$
- The value of  $r_{2P}$  for  $\chi'_{c1}$  is almost the same as that for  $\chi_{c1}(1P)$ :

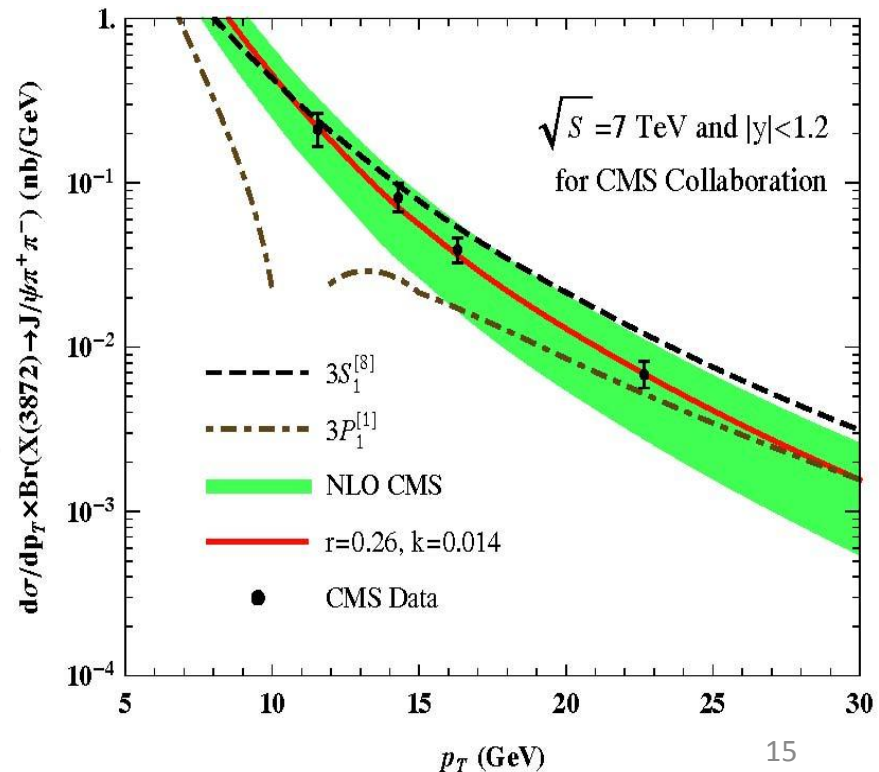
$$r_{1P} = 0.27 \pm 0.06 \text{ [MWC'11]}$$

which suggests that X(3872) be produced through its  $\chi'_{c1}$  component at short distance

➤ Molecule production mechanism:

$$\left\langle O_{3S_1^{[8]}}^{D^0\bar{D}^{*0}} \right\rangle \text{Br}_0 = (6.0 \pm 0.6) 10^{-5} \text{ GeV}^3$$

$$\chi^2/3 = 1.03$$



# Predictions v.s. CDF data

$$\sqrt{S} = 1.96 \text{ TeV}, \quad |y| > 0.6, \quad p_T > 5 \text{ GeV}$$

- $\chi'_{c1}$  production mechanism:

Inputs:  $r = 0.26, k = 0.014$

$$\sigma_{\text{CDF}}^{\text{th}}(p\bar{p} \rightarrow X(J/\psi\pi^+\pi^-)) = 2.5 \pm 0.7 \text{ nb} \quad (\text{v. s. } (3.1 \pm 0.7 \text{ nb})_{\text{ex}})$$

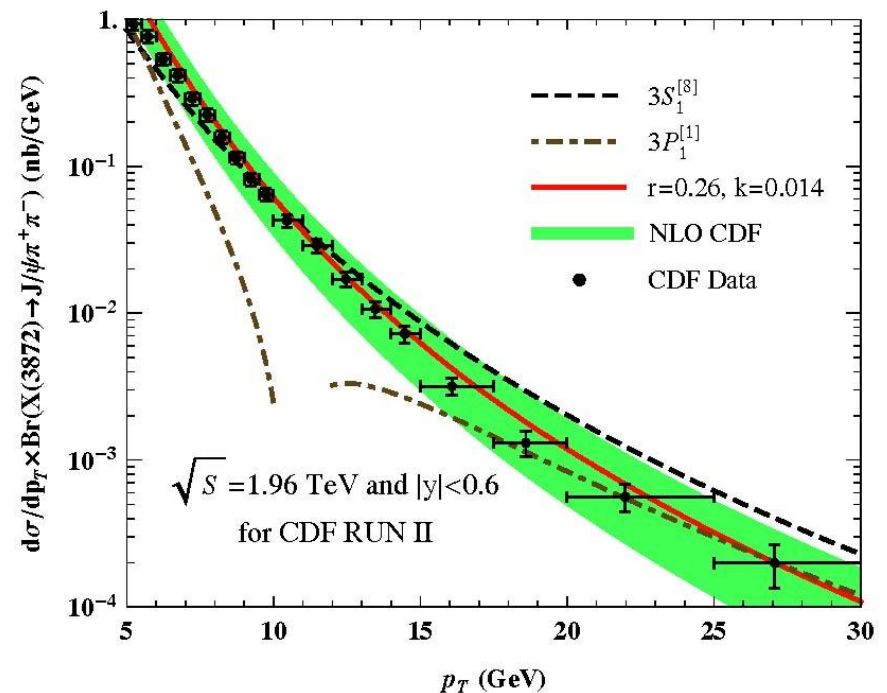
The predicted  $p_T$  distribution of  $X(3872)$  is compared with that of  $\psi'$  [CDF, PRD'09] (see the diagram)

- Molecule production mechanism:

$$\sigma_{\text{CDF}}^{\text{molecule}} = 1.1 \pm 0.4 \text{ nb}$$

2.6  $\sigma$  deviation from data

- Both the CMS and the CDF data favor the  $\chi'_{c1}$  production mechanism, rather than the molecule production mechanism.





# Predictions v.s LHCb data

$$\sqrt{s} = 7 \text{ TeV}, \quad 2.5 < y < 4.5, \quad 5 \text{ GeV} < p_T < 20 \text{ GeV}$$

➤  $\chi'_{c1}$  production mechanism:

Inputs:  $r = 0.26, k = 0.014;$

$$\sigma_{\text{LHCb}}^{\text{th-prompt}}(p\bar{p} \rightarrow X(J/\psi\pi^+\pi^-)) = 9.4 \pm 2.2 \text{ nb}$$

$$v.s. \sigma_{\text{LHCb}}^{\text{inclusive}} = 5.4 \pm 1.4 \text{ nb} \quad \text{LHCb, PRL'11}$$

- About 20% of data come from non-prompt contributions, thus our prediction is about 2 times larger than the data.
- Both the theoretical and the experimental uncertainties are large.
- More available data are expected to be analyzed.

➤ Molecule production mechanism:

$$\sigma_{\text{LHCb}}^{\text{molecule}} = 4.0 \pm 1.3 \text{ nb}$$

Better than ours, but the predicted  $p_T$  distribution at CMS is less consistent with data.

# Single parameter fit

- Fitting  $k$  to the CMS data with fixed  $r$

$$(3.1 \pm 0.7 \text{ nb})_{\text{CDF}}^{\text{ex}}$$

$$(5.4 \pm 1.4 \text{ nb})_{\text{LHCb}}^{\text{ex}} \cdot 80\%$$

- Fitting  $k$  to  $B$  decay data

$r$	$k$	$\chi^2/3$	$\sigma_{\text{CDF}}^{\text{th}}(\text{nb})$	$\sigma_{\text{LHCb}}^{\text{th}}(\text{nb})$
0.20	0.021	0.39	3.26	12.2
0.25	0.015	0.17	2.63	9.87
0.30	0.012	0.20	2.28	8.58
0.35	0.010	0.27	2.06	7.72
0.40	0.008	0.34	1.90	7.14

$$\begin{aligned} \text{Br}(B \rightarrow X(J/\psi\pi^+\pi^-)K) &= \text{Br}(B \rightarrow \chi'_{c1}K) \cdot k \\ &= (8.6 \pm 0.8) \times 10^{-6} \quad \text{PDG'12} \end{aligned}$$

$$\text{Br}^{\text{fit}}(B \rightarrow \chi'_{c1}K) = (3.7-5.7) \times 10^{-4} \quad \text{Kalashnikova \& Nefediev PRD'09}$$

$$\therefore k = Z_{c\bar{c}} \text{Br}_0 = 0.018 \pm 0.004$$

✓ Window in the table:  $r = 0.20-0.26$

✓ With a modest value  $\text{Br}_0 = 5\% \in (2.6\%-9\%)$

$$Z_{c\bar{c}} = 28\%-44\%$$

# X(3872) decays to $\psi(2s)\gamma$ and $J/\psi\gamma$

$$R_{\psi\gamma} \equiv \frac{B(X(3872) \rightarrow \psi(2S)\gamma)}{B(X(3872) \rightarrow J/\psi\gamma)} = 3.4 \pm 1.4,$$

BaBar arxiv:0809.0042

Belle arxiv:1105.0177

$$R < 2.1 \text{ (at 90\% C.L.)}$$

LHCb arxiv:1404.0275 (NEW)

$$\frac{B(X(3872) \rightarrow \psi(2S)\gamma)}{B(X(3872) \rightarrow J/\psi\gamma)} = 2.46 \pm 0.64 \pm 0.29,$$

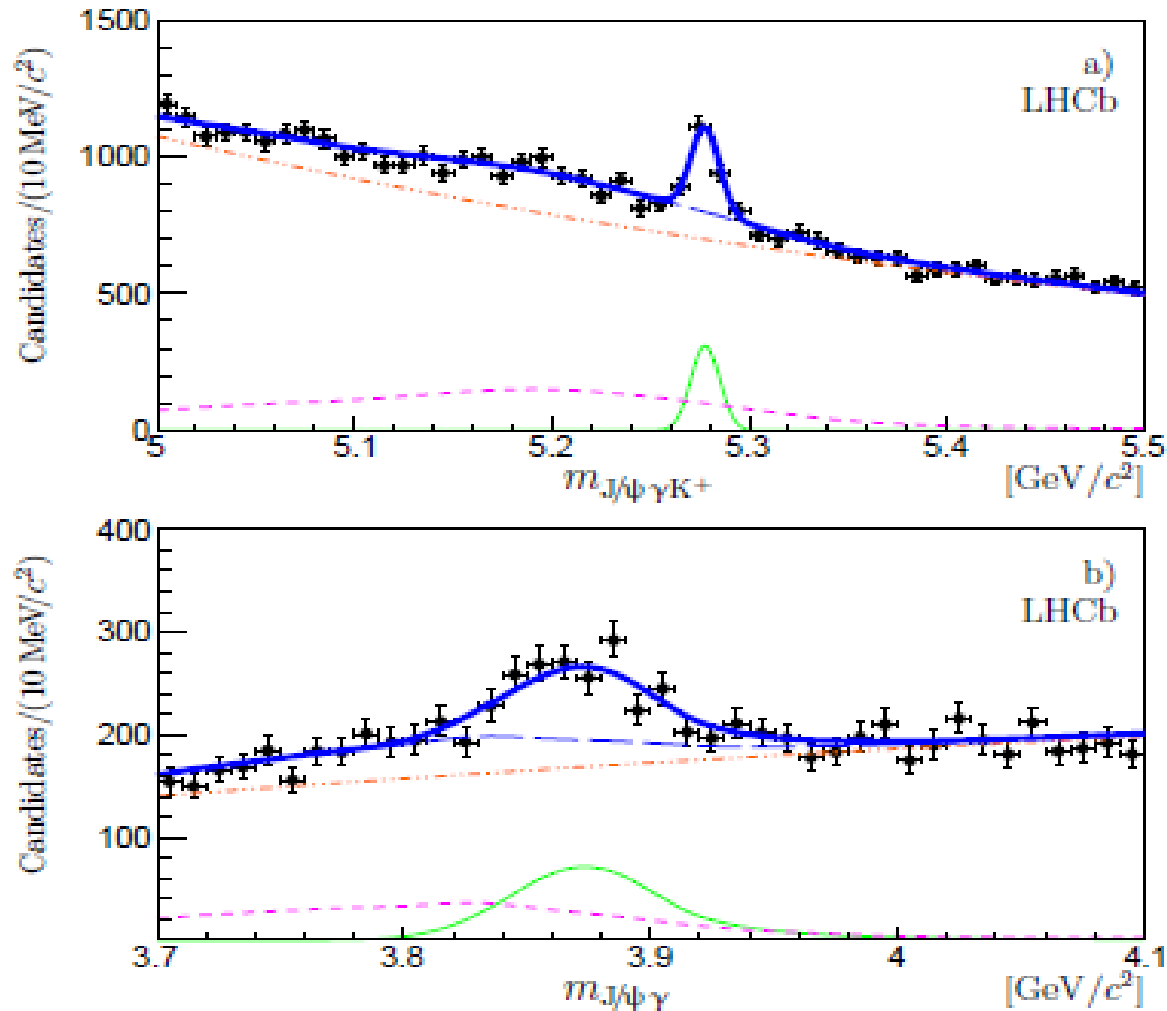


Figure 1: a) Distribution of the  $J/\psi\gamma K^+$  invariant mass with fit projection overlaid, restricted to those candidates with  $J/\psi\gamma$  invariant mass within  $\pm 3\sigma$  from the  $X(3872)$  peak position. b) Distribution of the  $J/\psi\gamma$  invariant mass with fit projection overlaid, restricted to those candidates with  $J/\psi\gamma K^+$  invariant mass within  $\pm 3\sigma$  from the  $B^+$  peak position. The total fit (thick solid blue) together with the signal (thin solid green) and background components (dash-dotted orange for the combinatorial, dashed magenta for the peaking component and long dashed blue for their sum) are shown.

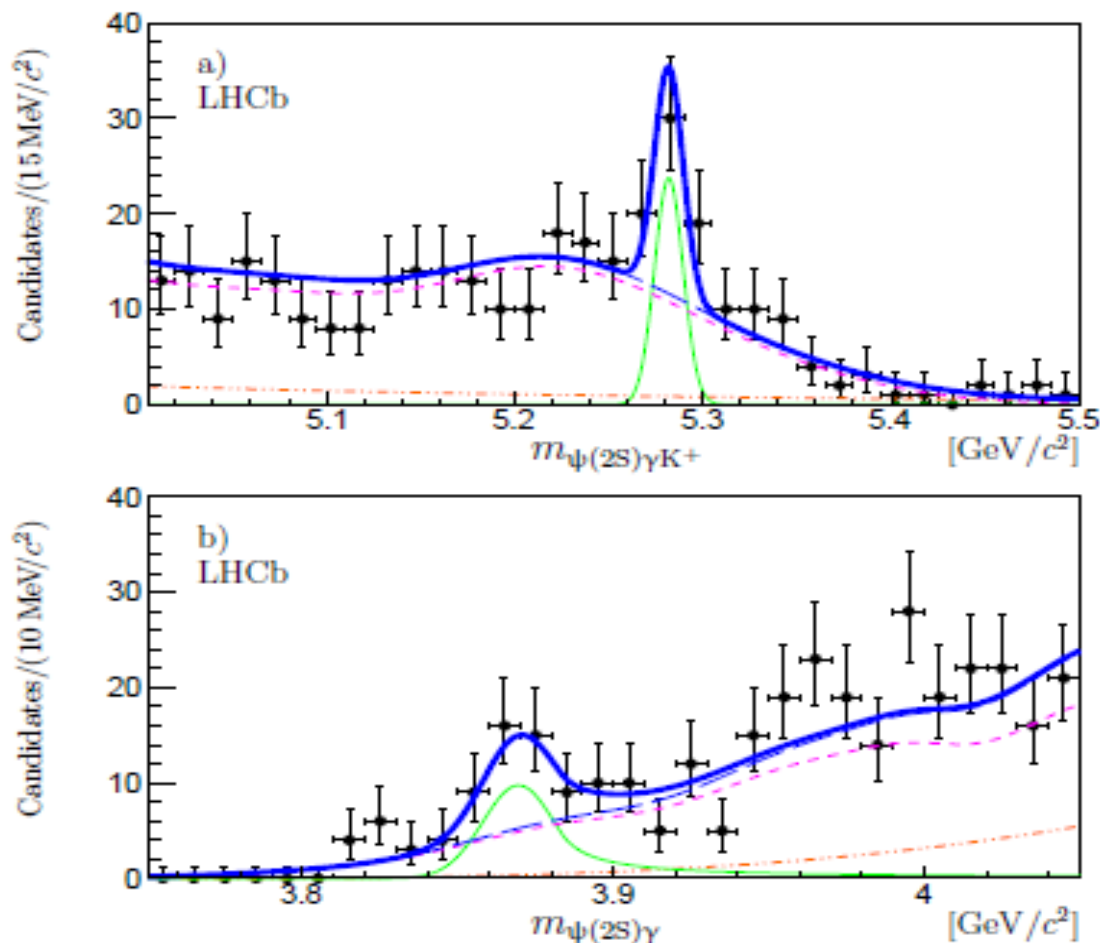


Figure 2: a) Distribution of the  $\psi(2S)\gamma K^+$  invariant mass with fit projection overlaid, restricted to those candidates with  $\psi(2S)\gamma$  invariant mass within  $\pm 3\sigma$  from the X(3872) peak position. b) Distribution of the  $\psi(2S)\gamma$  invariant mass with fit projection overlaid, restricted to those candidates with  $\psi(2S)\gamma K^+$  invariant mass within  $\pm 3\sigma$  from the  $B^+$  peak position. The total fit (thick solid blue) together with the signal (thin solid green) and background components (dash-dotted orange for the combinatorial, dashed magenta for the peaking component and long dashed blue for their sum) are shown.

# Theoretical results for the ratio R

- Earlier molecule model:  $R=(3-4)\times 10^{-3}$  Swanson PLB'04
- Recent molecule: systematical study for long-distance and short-distance contributions in XEFT: Mehen & Springer PRD'11
- $\chi'_{c1}$  model: E1 transition rates  
 $\Gamma(\chi_{c1}(2p)\rightarrow\psi(2s)\gamma)=(40-60) \text{ KeV} >$   
 $\Gamma(\chi_{c1}(2p)\rightarrow\psi(1s)\gamma)$   
due to node structure in wave functions.  
Measured ratio R may be naturally understood.
- Li & Chao, PRD'09, Badalin et al., PRD'12, and many earlier potential model calculations for E1 transitions

# Summary

- With NRQCD factorization, the hadronic production cross section of  $X(3872)$  is evaluated up to NLO in  $\alpha_s$  in the mixing model:
  - The CMS  $p_T$  distribution can be fitted very well with  $\chi^2/2 = 0.26$ .
  - The obtained  $r_{2P}$  for  $\chi'_{c1}$  is almost the same as  $r_{1P}$  for  $\chi_{c1}$  [MWC'11], which suggests that the  $X(3872)$  be produced through its  $\chi'_{c1}$  component at short distances.
  - The outcomes of the fit explain the CDF total cross section very well, however, the predicted cross section for the LHCb widow is larger than the data by a factor of 2, which might due to the large uncertainties.
- By harmonizing the fit results with those in B decays, we get
$$k = Z_{c\bar{c}}\text{Br}(X \rightarrow J/\psi\pi^+\pi^-) = 0.018 \pm 0.004, \quad r = 0.20-0.26,$$
which could be important to understand the nature of  $X(3872)$ .
- The cross section in the molecule model is also evaluated at NLO in  $\alpha_s$ , which is disfavored by both the CMS and the CDF data.

# Summary

- The large ratio of  $X(3872)$  decays to  $\psi(2S)\gamma$  to that of  $J/\psi\gamma$  may be understood in the mixing model via  $\chi'_{c1}$  decay .
- The **large** and nearly **equal** production rates in both charged and neutral B meson decays may be understood by  $\chi'_{c1}$  production at short-distances.
- Further studies are needed in both the molecule model and mixing model to understand various puzzles about the nature of  $X(3872)$ .



Thanks!

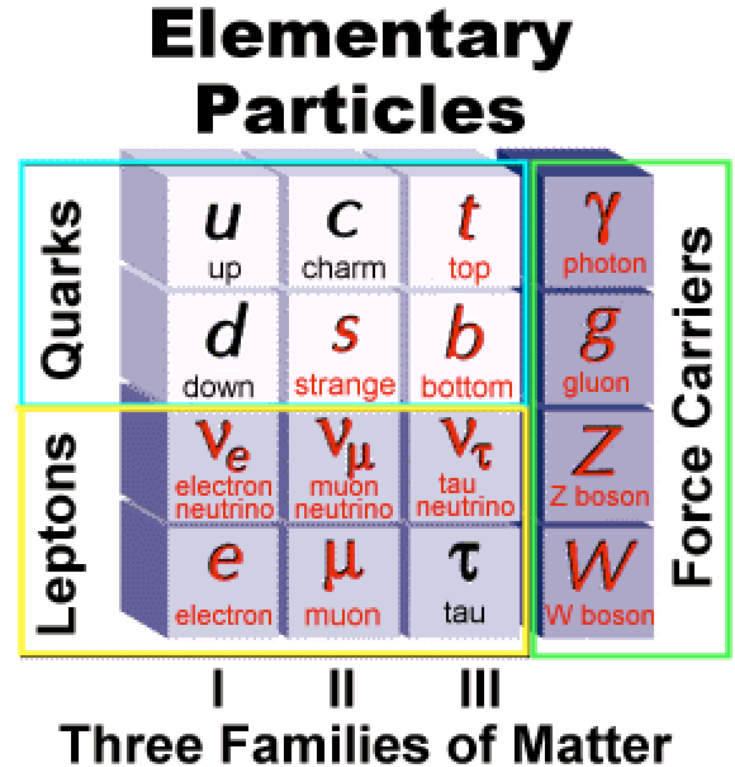
# Heavy quarkonium: charmonium and bottomonium

Flavor	Mass
$u$	1.5 – 4.5 MeV
$d$	5.0 – 8.5 MeV
$s$	80 – 155 MeV
$c$	1.0 – 1.4 GeV
$b$	4.0 – 4.5 GeV
$t$	$174.3 \pm 5.1$ GeV

Light quarks (u, d, s)

Heavy quarks (c, b, t)

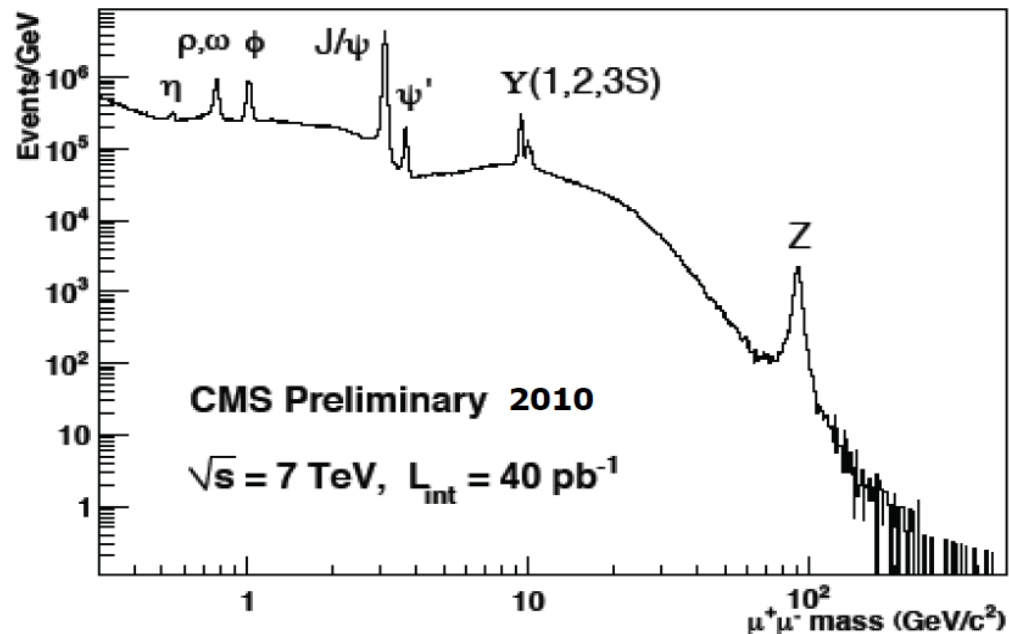
$\Lambda_{\text{QCD}}$



- Heavy quarkonium: composed of heavy quark and antiquark pair ( $J/\psi$ ,  $\psi'$ ,  $\chi_{cJ}$ ,  $\Upsilon(nS)$ ,  $\chi_{bJ}$  ... ); nonrelativistic system:  $v^2 \ll 1$ , effective theories with different scales:  $m$ ,  $mv$ ,  $mv^2$
- Heavy quark  $m_Q \gg \Lambda_{\text{QCD}}$ , produced at short distances, pQCD applicable.

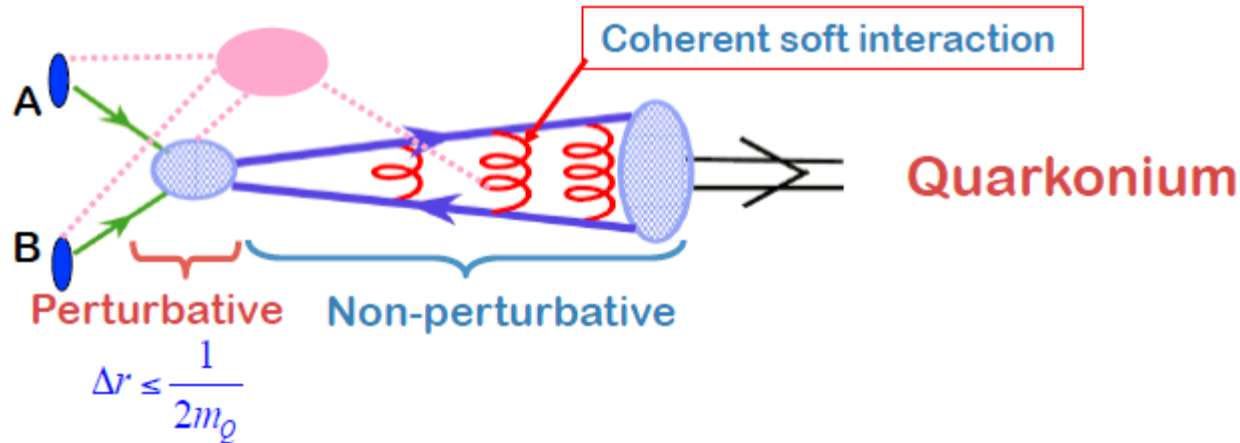
# Study of heavy quarkonium production

- Heavy quarkonia production: Provide an ideal laboratory to study pQCD and hadronization.
- Lots of heavy quarkonia ( $J/\psi$ ,  $\Psi'$ ,  $\chi_{cJ}$ ,  $\Upsilon(nS)$ ), and even charmonium-like states  $X(3872)$  observed at LHC.



# Factorization and hadronization

- Short distance and long distance parts. Hadronization followed by production of an **off-shell** heavy quark pair.



- Approximation: **on-shell** pair + hadronization.
  - ◆ Different assumptions/treatments on how the heavy quark pair becomes a heavy quarkonium: different factorization models.

$$\sigma_{AB \rightarrow H+X} = \sum_n \int_n d\Gamma_{(Q\bar{Q})_n} \left[ \frac{d\hat{\sigma}(Q^2)}{d\Gamma_{(Q\bar{Q})_n}} \right] F_{(Q\bar{Q})_n \rightarrow H}(p_Q, p_{\bar{Q}}, P_H)$$

# NRQCD – factorization

$$d\sigma_\psi = \sum_{i,j,n} \int dx_1 dx_2 \underbrace{G_{i/A} G_{j/B}}_{\Lambda_{QCD}} \times \underbrace{\hat{\sigma}[ij \rightarrow c\bar{c}[n] + X]}_{m_c} \times \underbrace{\langle O_n^\psi \rangle}_{m_c v}$$

Parton distribution function

Long distance ( $\sim 1/\Lambda_{QCD}$ )

CTEQ6L1, CTEQ6M

Hadronization (LDMEs)

Long distance ( $\sim 1/(m_c v)$ )

input from experiments needed.

Production of heavy quark pair

Short distance ( $\sim 1/m_c$ )  
perturbative calculable.

# Widely used factorization methods

Since November revolution: Discovery of  $J/\psi$  in 1974

- Color-singlet model (CSM): 1975 –
  - The pair has the same quantum numbers as the quarkonium
  - Effectively **no free parameter**.
- Color evaporation model (CEM): 1977 –
  - All pairs with mass less than open flavor heavy meson threshold;
  - **One parameter** per quarkonium state.
- NRQCD approach: 1986 –
  - Pairs can be produced in both color-singlet and color-octet states with various probabilities
  - **Infinite parameters** – organized in power of  $v$ .

Einhorn, Ellis, PRL 1975  
Chang, NPB 1980  
Berger, Jones, PRD 1981 .....

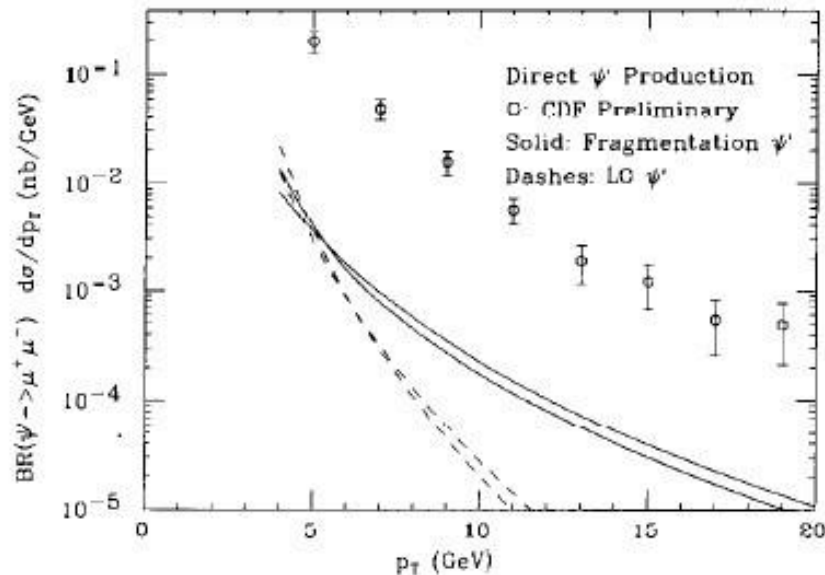
Fritsch, PLB 1977  
Halzen, PLB 1977 .....

Caswell, Lepage, PRD 1986  
Bodwin, Braaten, Lepage, PRD 1992

# Heavy quarkonium production at hadron colliders

# CSM – $\Psi'$ puzzle

- Twenty year ago, CDF collaboration found a surprisingly large production rate of  $\Psi'$  at high  $p_T$ .
- The yield is larger than the theoretic prediction by **a factor of 30**, even though the fragmentation contribution is included.



Braaten, Doncheski, Fleming,  
Mangano, PLB 1994

Fig. 4. Preliminary CDF data for prompt  $\psi'$  production (O) compared with theoretic predictions of the total fragmentation contribution (solid curves) and the total leading-order contribution (dashed curves).



# CSM – NLO Calculation

- Differential cross section is enhanced by **2 orders** relative to **LO** CS result at high  $p_T$ . Still much smaller than data.
- Polarization is changed from being **transversely polarized** to

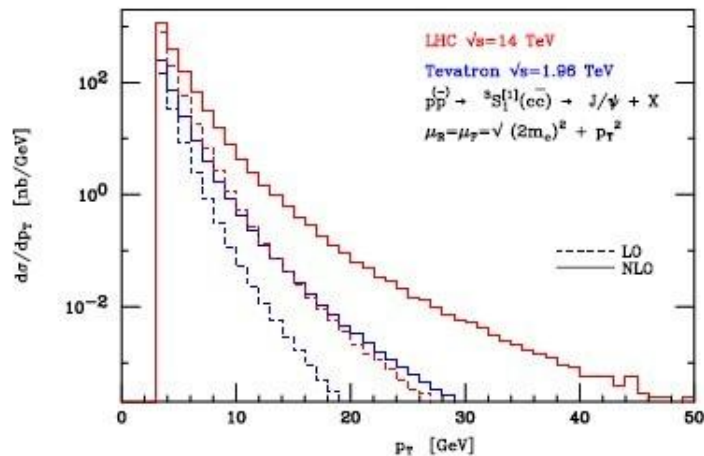
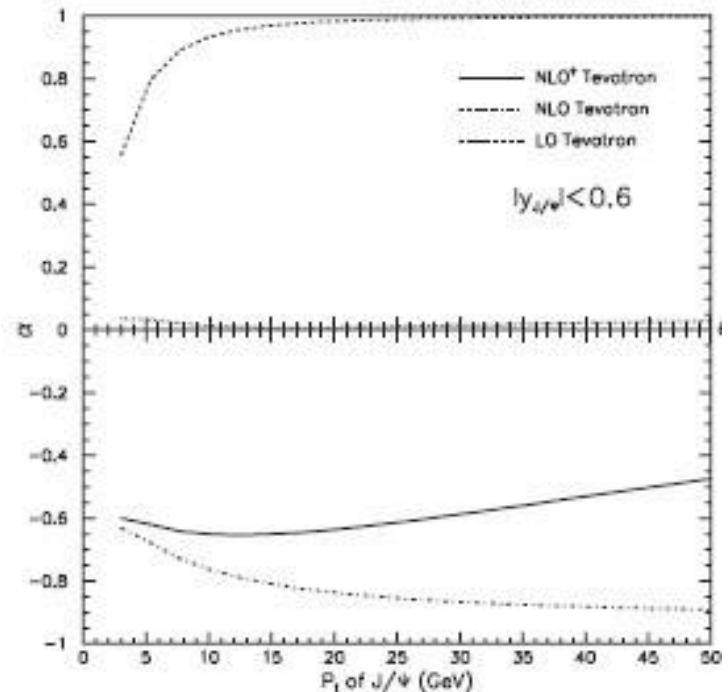


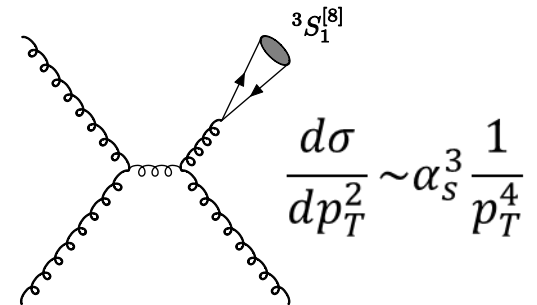
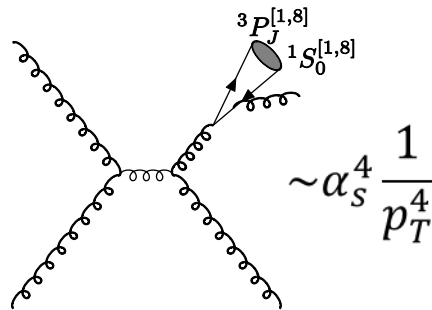
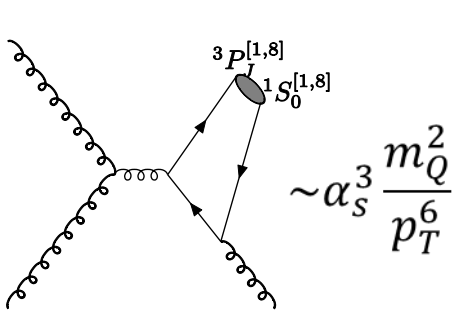
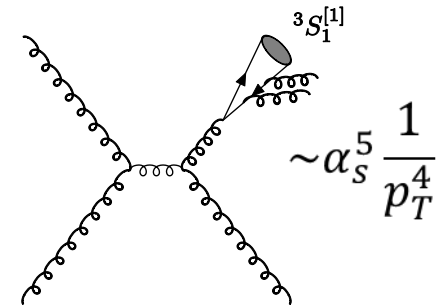
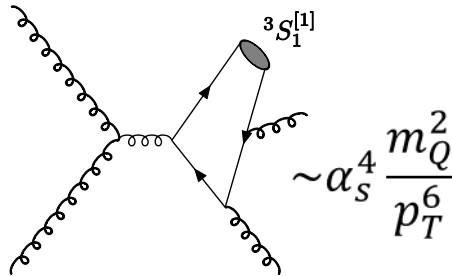
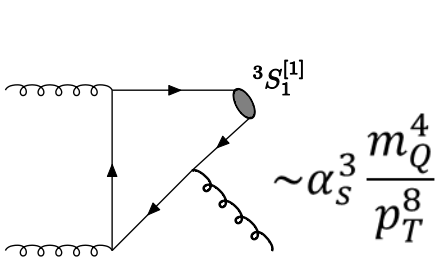
FIG. 5 (color online). Differential cross sections for direct  $J/\psi$  production via a  $^3S_1^{[1]}$  intermediate state, at the Tevatron (lower histograms) and LHC (upper histograms), at LO (dashed line) and NLO (solid line).  $p_T^{J/\psi} > 3$  GeV and  $|y^{J/\psi}| < 3$ . Details on the input parameters are given in the text.



Campbell, Maltoni, Tramontano, PRL 2007

Gong, Wang, PRL 2008

- At large  $p_T$ ,  $p_T$  enhancement is more important than  $\alpha_s$  suppression;



# Importance of complete NLO calculation

- One can conclude nothing definitely until the  $p_T^{-4}$  behavior of all channels are opened.
- NNLO contributions for  $^3S_1^{[1]}$  may be safely ignored. (Ma, Wang, Chao, PRD 2011)

*A complete NLO calculation to heavy quarkonia production is essential to understand the production mechanism.*

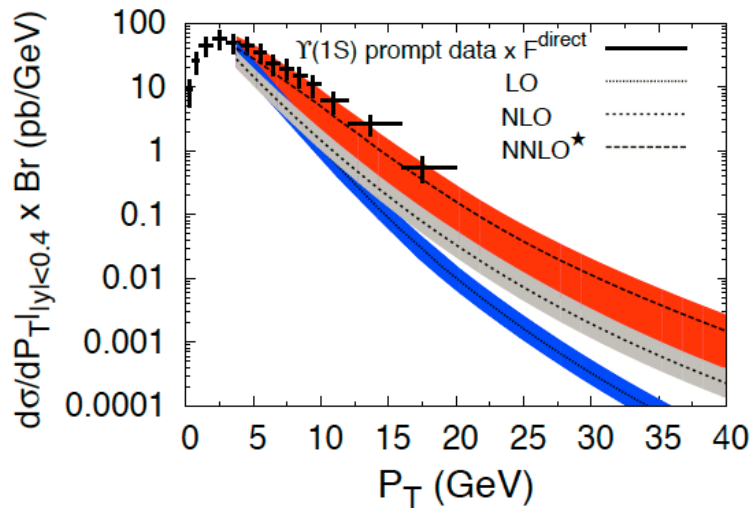
❑ **NLO correction for P-wave channel is needed!**

States	Order where $p_T^{-4}$ present
$^3S_1^{[1]}$	NNLO
$^3S_1^{[8]}$	LO
$^1S_0^{[1,8]}$	NLO
$^3P_J^{[1,8]}$	NLO

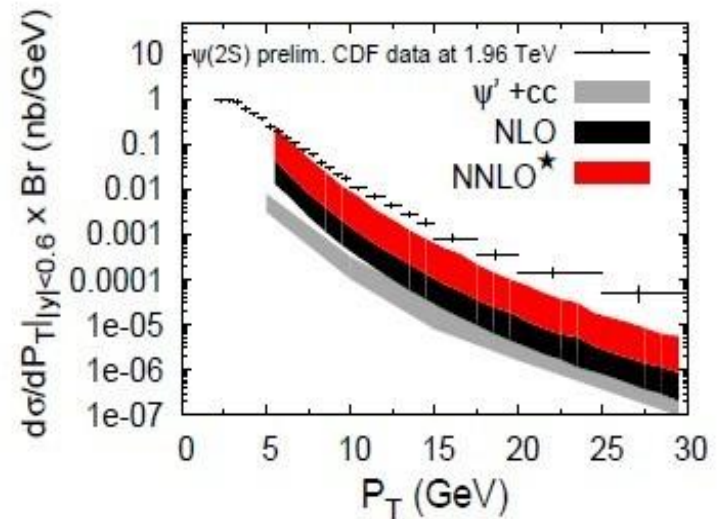
- Typical NLO calculation: a small correction, improve the precision of theoretic prediction and reduce uncertainties induced by renormalization scale and factorization scale.
- NLO calculation here: **NOT A CORRECTION!** But provide the main contribution for some channels which are suppressed by kinematics at LO.

# CSM – NNLO\* calculation

- NNLO correction to CS channel is estimated by calculating only tree level diagrams (NNLO\*). An **infrared cutoff**  $s_{ij}^{\min}$  is imposed to control soft and collinear divergences.



Artoisenet, Campbell, Lansberg, Maltoni,  
Tramontano, PRL 2008

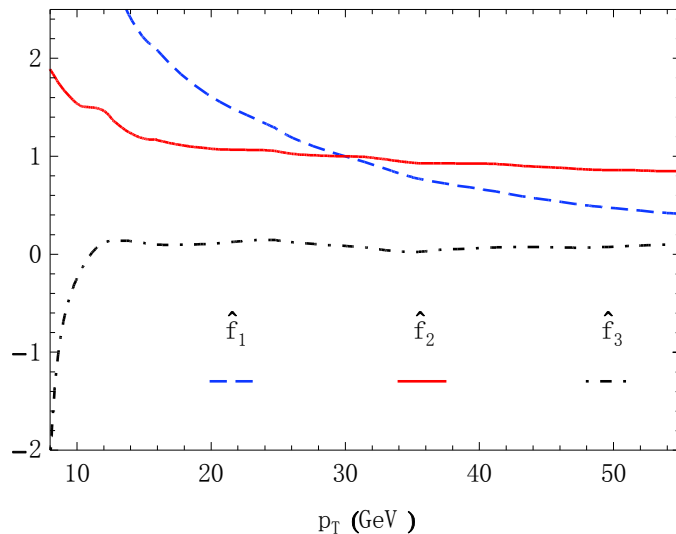


Lansberg, EPJC 2009

- Large corrections. Almost reach the data.

# ➤ Theoretically: **CSM – Problem**

- ◆ IR divergence in NLO correction for P-wave.
- Phenomenology: CSM cannot explain experiment data even including NNLO contribution (Ma, Wang, Chao, PRD 2011)
  - ◆ The only new behavior is the gluon fragmentation, which scaling as  $p_T^{-4}$ . Other contributions at this order is suppressed by  $\alpha_s$  relative to NLO.
  - ◆ The fragmentation contribution has been calculated by E. Braaten et al. , and they are as small as 1/30 of the experiment data.
  - ◆ NNLO\* is dominated by double logarithm, which will be canceled by loop corrections. Thus NNLO\* method may overestimate the CSM contribution.



$$R^* = d\sigma_{NNLO^*}/d\sigma_{NLO}$$

$$\hat{f}_1 = \frac{R^*}{p_T^2} \Big|_{s_{ij}^{min}=0.5m_b^2}$$

$$\hat{f}_2 = \frac{R^*}{\log^2(p_T^2/s_{ij}^{min})} \Big|_{s_{ij}^{min}=0.5m_b^2}$$

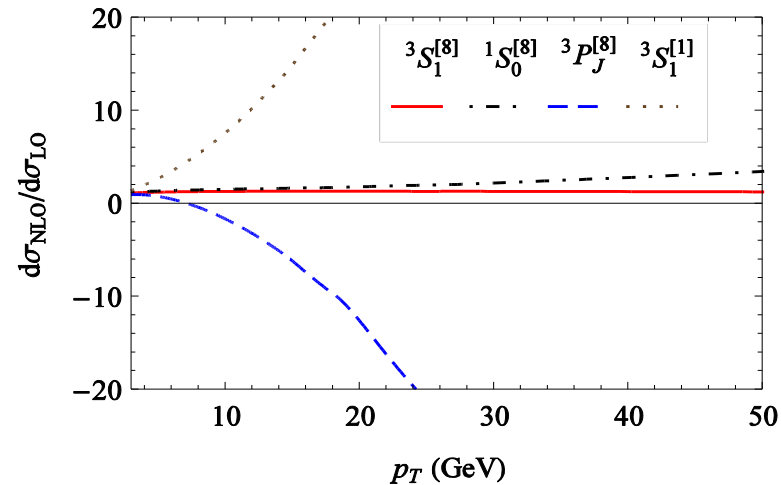
$$\hat{f}_3 = 1 - \frac{R^*/\log^2(p_T^2/s_{ij}^{min}) \Big|_{s_{ij}^{min}=2m_b^2}}{R^*/\log^2(p_T^2/s_{ij}^{min}) \Big|_{s_{ij}^{min}=0.5m_b^2}}$$

# CSM – Convergence of $v^2$ expansion

- To further confirm that the CSM is not enough to explain data, it is needed to study the convergence of  $v^2$  expansion.
- Up to relative-order- $v^4$  correction for gluon fragmentation into  $J/\psi$  in the CS channel has been done by [Bodwin, Kim, Lee, 1208.5301](#). The finite term of order- $v^4$  contribution was found to be not important numerically. That is,  $p_T^{-4}$  contribution of CSM is not important.
- $v^2$  correction for  $p_T^{-6}$  contribution of CSM is studied by [Chao, Li, Ma \(In progress\)](#). The convergence of  $v^2$  expansion is found to be very good.  $p_T^{-6}$  contribution of CSM is less than one-tenth of experiment data when  $p_T > 10$  GeV.
- Considering also that other higher power contributions are not important at large  $p_T$ , CS channel contributions are neglectable when  $p_T > 10$  GeV.

# Complete NLO correction for $\Psi$ – yield

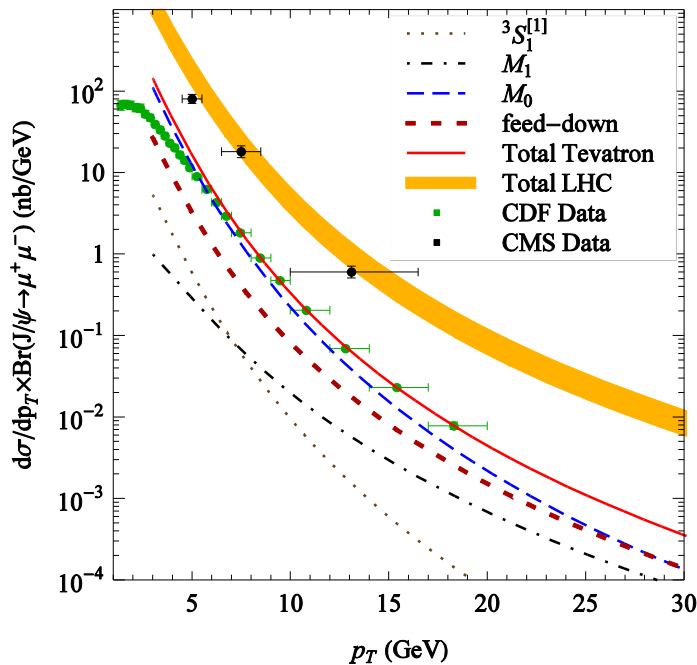
- Two groups calculated it independently: Ma, Wang, Chao (MWC) and Butensckön, Kniehl (BK).
- The results of the two groups for the short-distance coefficients agree.



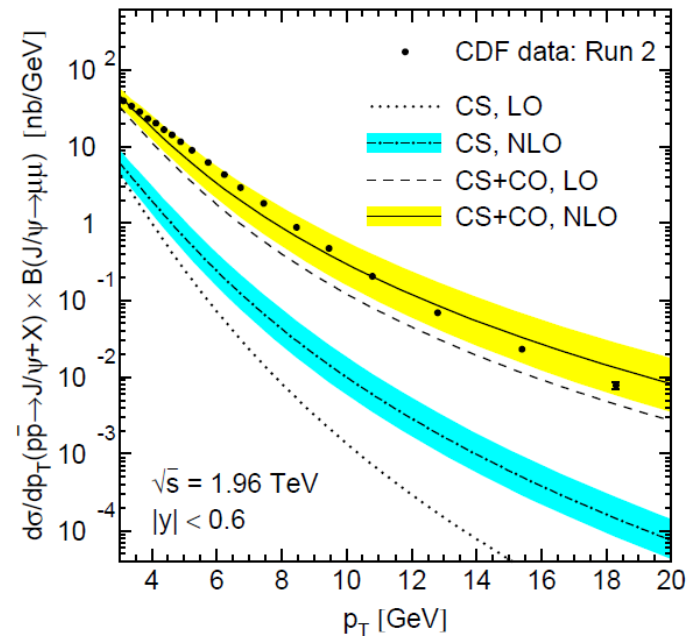
- Methods of fit NRQCD LDMEs are different:
  - ◆ MWC: **select only data that can be safely described by perturbation theory to fit LDMEs**, although only some linear combinations of LDMEs can be determined.
  - ◆ BK: **fit as many as possible data to determine all three CO LDMEs**.

# Complete NLO correction for $\Psi$ – yield

- MWC: agree with data only for  $p_T > 7\text{GeV}$ , but the agreement is very good;
- BK: all data for  $p_T > 3\text{GeV}$  can be described within large errors.



MWC, PRL 2011

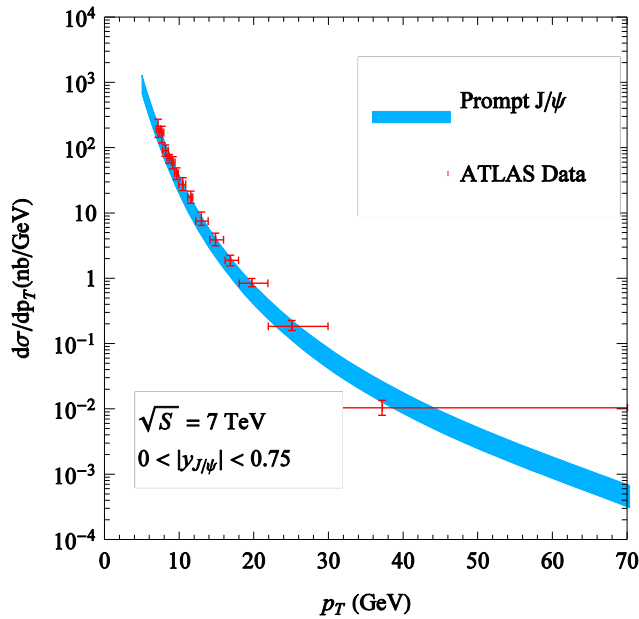


BK, PRL 2011

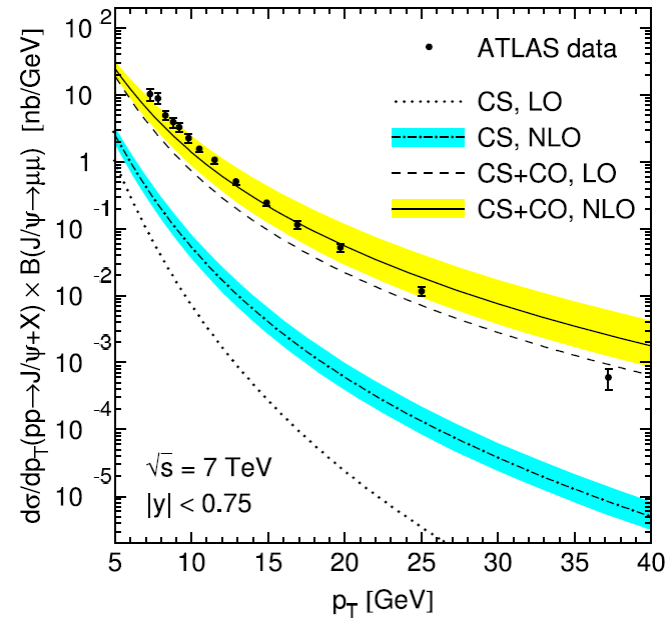


- MWC: agree with data only for  $p_T > 7\text{GeV}$ , but the agreement is very good (up to 40-70 GeV);
- BK: data for  $p_T > 3\text{GeV}$  can be described within large errors.

### Confront with Large $p_T$ data



MWC

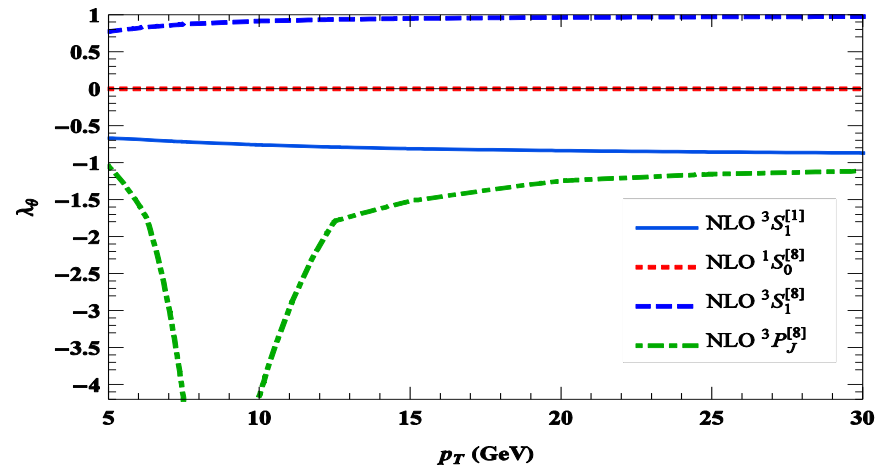
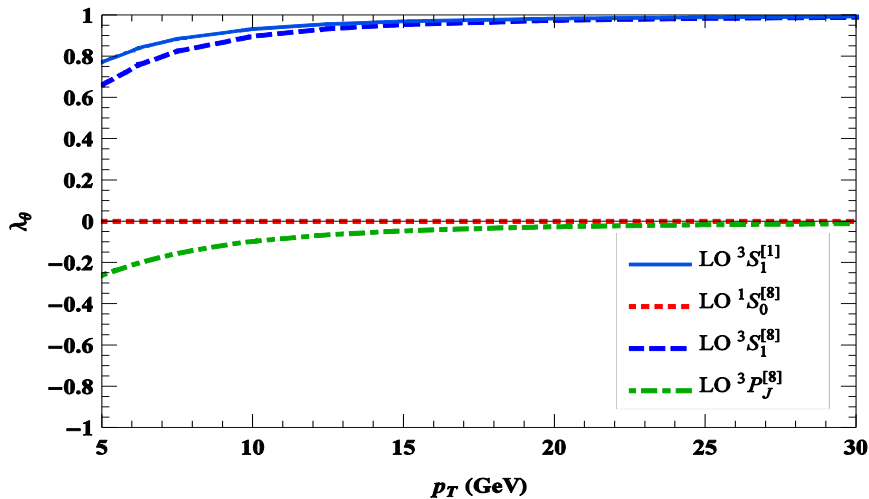


BK

# Complete NLO correction for $\Psi$ – polarization

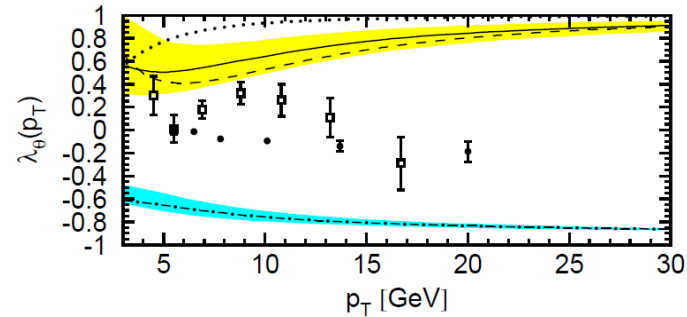
- For P-wave channel  $\lambda_\theta < 1$ , which results from short distance coefficient behavior:  $d\hat{\sigma}_T < 0$  and  $d\hat{\sigma}_L > 0$ ;
- **Negative transverse component of  $^3P_J^{[8]}$  channel** may cancel the transverse component of  $^3S_1^{[8]}$  channel, leading to mainly unpolarized  $J/\Psi$ .

$$\lambda_\theta = \frac{d\hat{\sigma}_T - 2d\hat{\sigma}_L}{d\hat{\sigma}_T + 2d\hat{\sigma}_L}$$

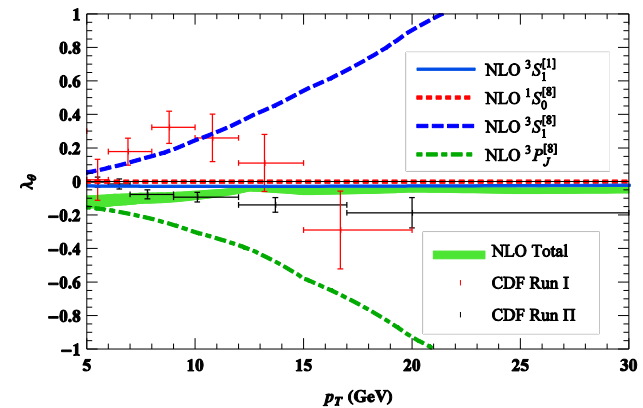


# Polarization predicted by three groups

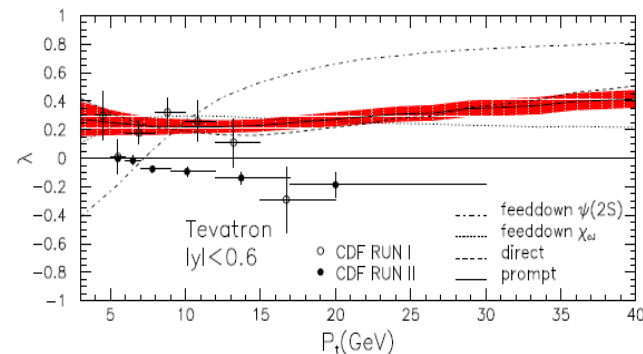
1. Butensckön and Kniehl: **direct**; LDMEs: global fit of pp, ep,  $\gamma\gamma$  and  $e^+e^-$  data; **conflict with CDF data**.
  2. Chao, Ma, Shao, Wang and Zhang: **direct**; LDMEs: fit yield of CDF and LHC data (especially large  $p_T$  data); **consistent with CDF data**.
  3. Gong, Wan, Wang and Zhang: **prompt**; LDMEs: fit yield of CDF and LHCb; **agree with Run-I data (except two points), but conflict with Run-II data**.
- Prompt polarization by GWWZ is not much different from their direct polarization.
  - For direct polarization, the only difference between the three groups is the choice of LDMEs.
  - **How to fit LDMEs ???**
  - **Polarization data from LHC for larger  $p_T$**



BK

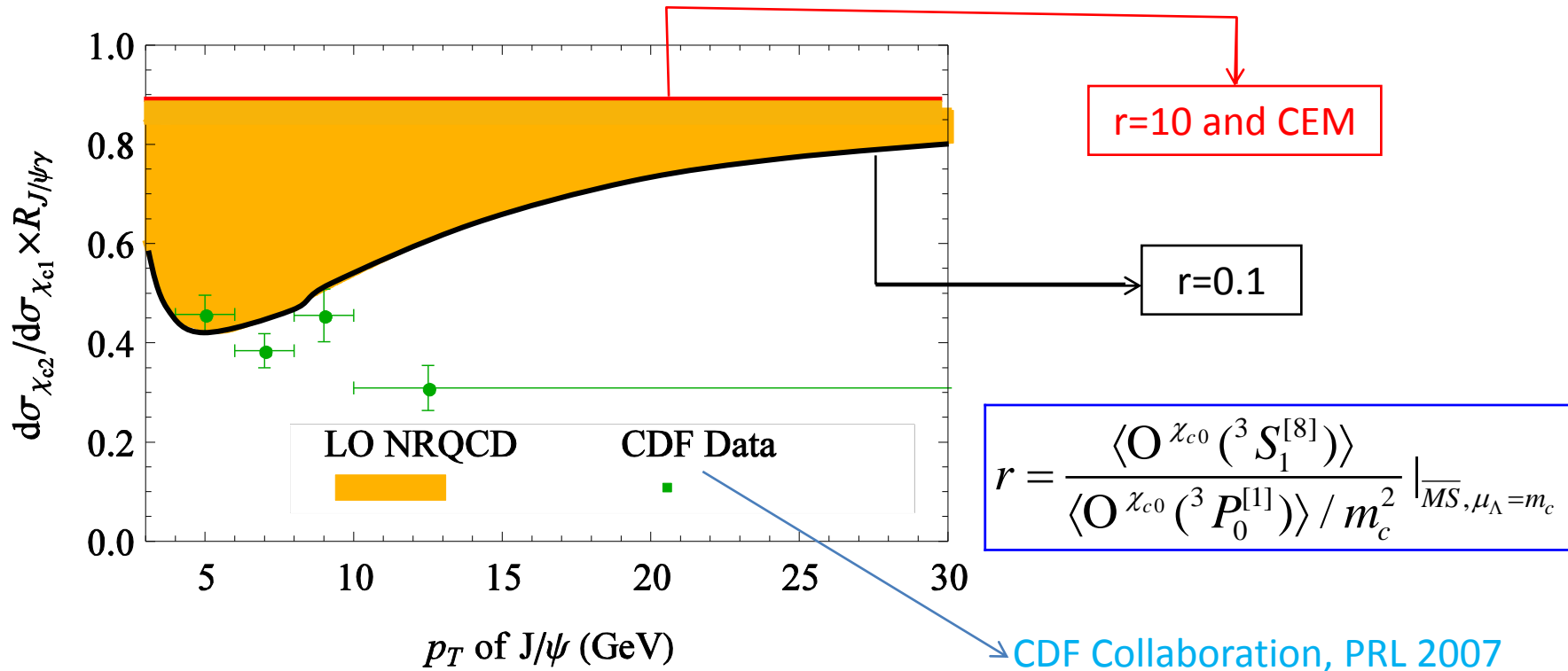


CMSWZ



GWWZ

# $\chi_{cJ}$ ratio puzzle

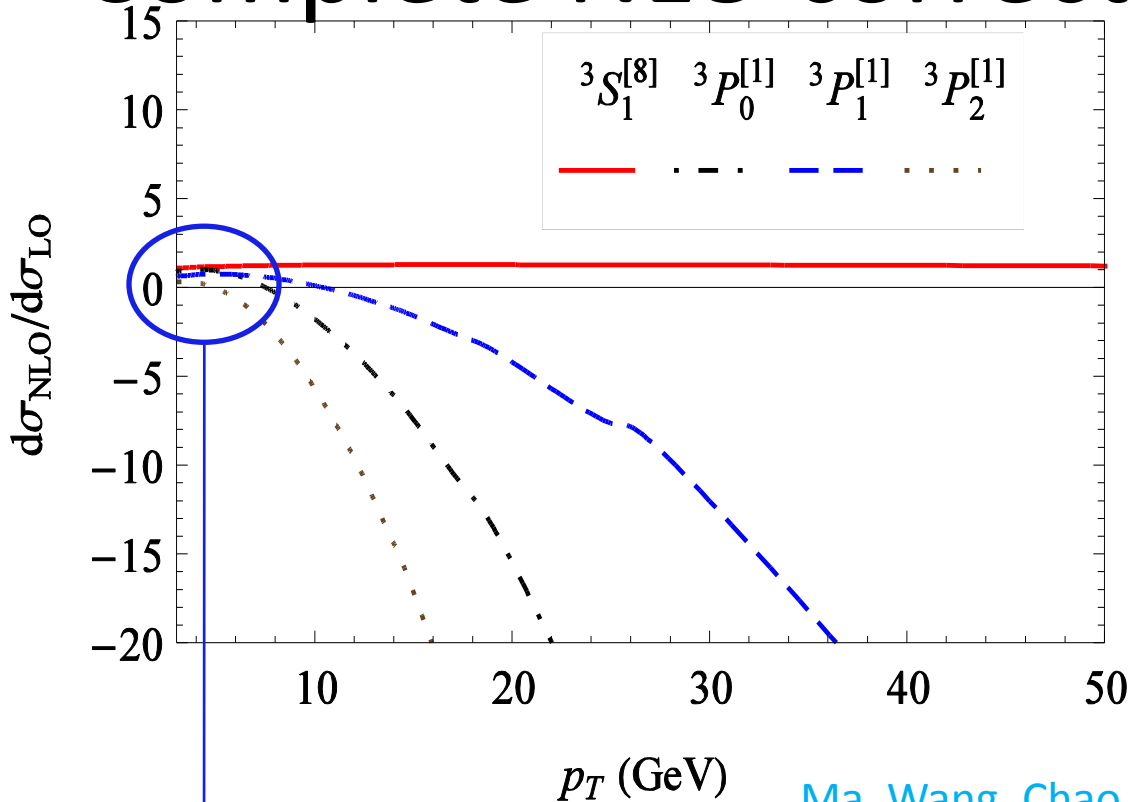


• **LO NRQCD** prediction, dominated by CO channel at high  $p_T$ , is far away from the experiment data even though  $0.1 < r < 10$  ( $r \approx 1$  based on NRQCD).

$$\frac{d\sigma_{\chi_{c2}}}{d\sigma_{\chi_{c1}}} \xrightarrow{p_T \gg m_c} \frac{5}{3}$$

• **CEM** is even worse:  $d\sigma_{\chi_{c2}}/d\sigma_{\chi_{c1}} \equiv 5/3$

# Complete NLO correction for $\chi_{cJ}$ (1)



K factor of each channel.

Ma, Wang, Chao, PRD(R) 2011

Large corrections originate from  $p_T / (2m_c)$

• Large but negative corrections are found.

• CS channel of  $\chi_{c2}$  declines much faster than  $\chi_{c1}$ .

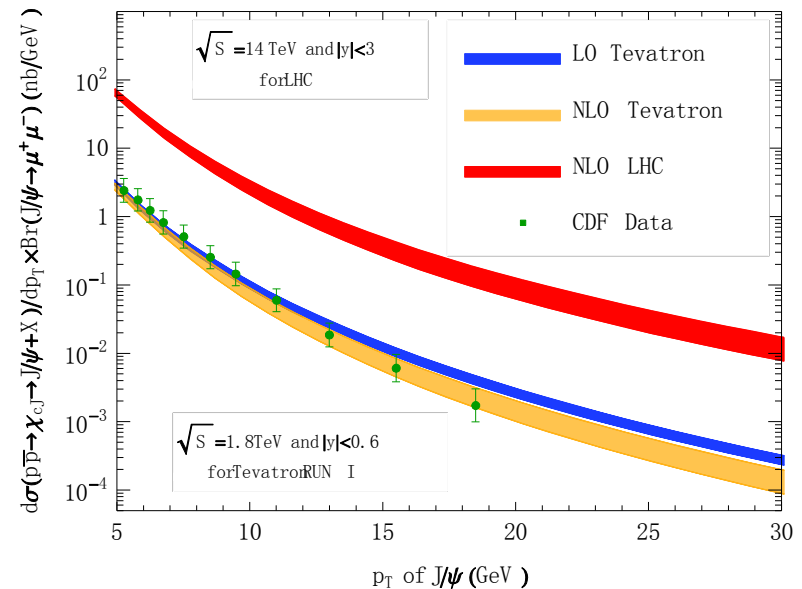
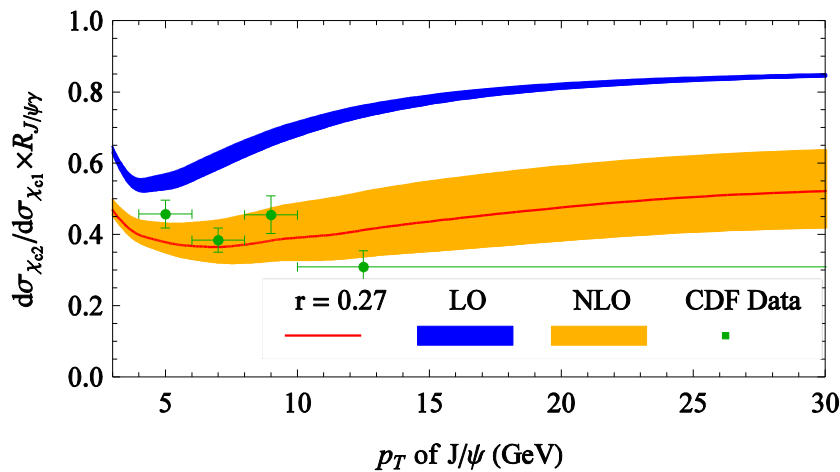
Different behavior from CO channel.

Subtraction scheme and NRQCD renormalization scale dependent.

# Complete NLO correction for $\chi_{cJ}$ (2)

- Ratio  $d\sigma_{\chi_{c2}}/d\sigma_{\chi_{c1}}$  can be explained in NLO;
- Differential cross section is also improved.

Ma, Wang, Chao, PRD(R) 2011



# Complete NLO

- Ratio  $\sigma_{\chi_{c2}} / \sigma_{\chi_{c1}}$ : good agreement with LHCb and CMS data;
- CMS data further confirm that  $\sigma_{\chi_{c2}} / \sigma_{\chi_{c1}} \neq 5/3$  even  $p_T$  is very large.

