

# RESUMMATION EFFECTS OF THE GAUGE BOSON PAIR PRODUCTION

Yan Wang

Department of Physics, PKU

In collaboration with Chong Sheng Li, Ze Long Liu,  
Ding Yu Shao and Hai Tao Li

13th Mini Workshop on the Frontier of LHC physics

Zhejiang University, Hangzhou

Nov. 8, 2014

# TESTING STANDARD MODEL -----TRIPLE GAUGE BOSON COUPLINGS

Probe **TGC** which are a fundamental prediction of the non-Abelian  $SU(2) \times U(1)$  gauge structure of electroweak theory.

$$\begin{aligned} \mathcal{L}_{WWV}/g_{WWV} &= ig_1^V (W_{\mu\nu}^\dagger W^\mu V^\nu - W_\mu^\dagger V_\nu W^{\mu\nu}) + i\kappa_V W_\mu^\dagger W_\nu V^{\mu\nu} \\ &+ i\frac{\lambda_V}{m_W^2} W_{\lambda\mu}^\dagger W^\mu V^{\nu\lambda} - g_4^V W_\mu^\dagger W_\nu (\partial^\mu V^\nu + \partial^\nu V^\mu) \\ &+ g_5^V \epsilon^{\mu\nu\lambda\rho} (W_\mu^\dagger \partial_\lambda W_\nu - \partial_\lambda W_\mu^\dagger W_\nu) V_\rho \\ &+ i\tilde{\kappa}_V W_\mu^\dagger W_\nu \tilde{V}^{\mu\nu} + i\frac{\tilde{\lambda}_V}{m_W^2} W_{\lambda\mu}^\dagger W^\mu V^{\nu\lambda}, \end{aligned}$$

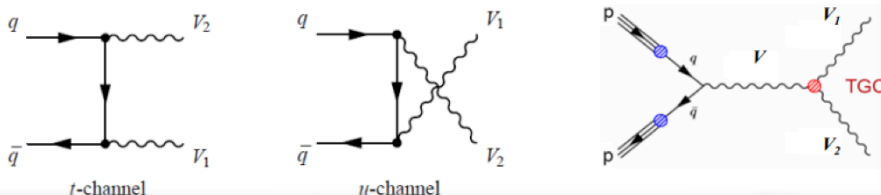
$$\begin{aligned} \mathcal{L}_{Z\gamma V} &= -ie \left[ \left( h_1^V F^{\mu\nu} + h_3^V \tilde{F}^{\mu\nu} \right) Z_\mu \frac{(\square + m_V^2)}{m_Z^2} V_\nu \right. \\ &\left. + \left( h_2^V F^{\mu\nu} + h_4^V \tilde{F}^{\mu\nu} \right) Z^\alpha \frac{(\square + m_V^2)}{m_Z^4} \partial_\alpha \partial_\mu V_\nu \right], \end{aligned}$$

coupling	parameters	channel
$WW\gamma$	$\lambda_\gamma, \Delta\kappa_\gamma$	WW, $W\gamma$
$WWZ$	$\lambda_Z, \Delta\kappa_Z, \Delta g_1^Z$	WW, WZ
$ZZ\gamma$	$h_3^Z, h_4^Z$	$Z\gamma$
$Z\gamma\gamma$	$h_3^\gamma, h_4^\gamma$	$Z\gamma$
$Z\gamma Z$	$f_{40}^Z, f_{50}^Z$	ZZ
$ZZZ$	$f_{40}^\gamma, f_{50}^\gamma$	ZZ

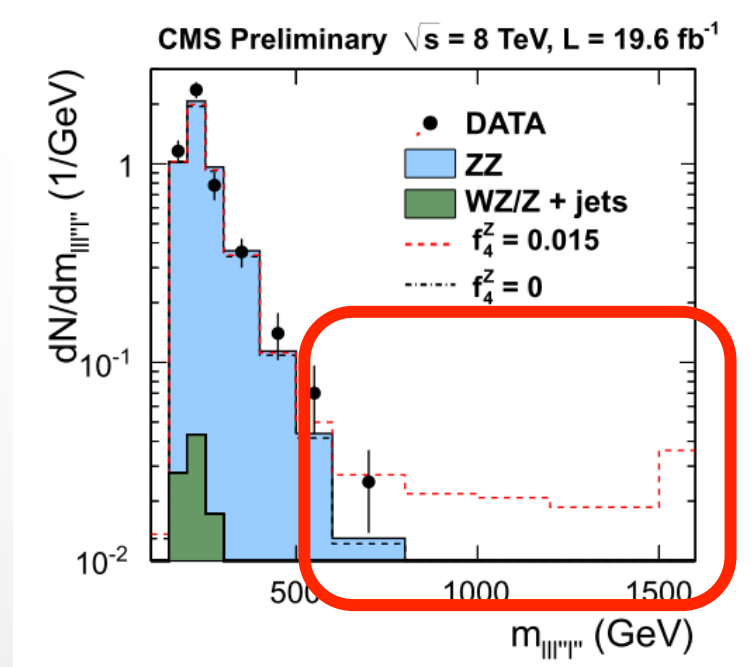
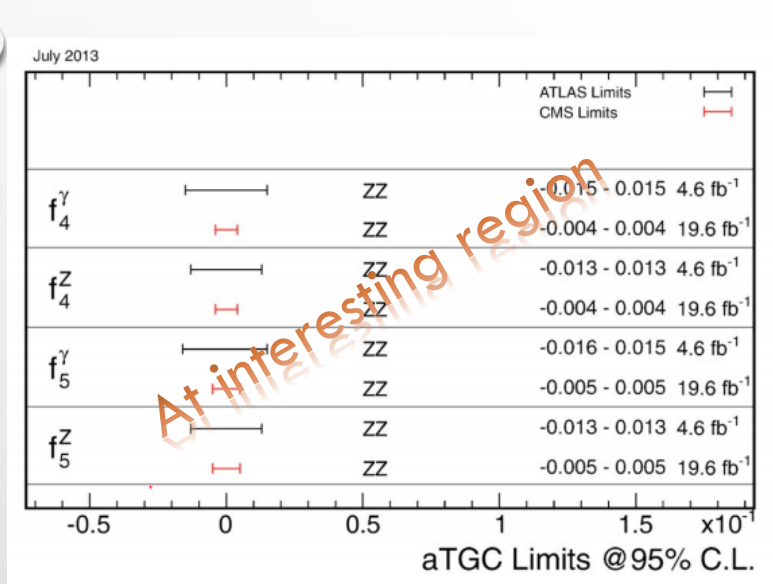
In SM,  $SU(2) \times U(1) \downarrow Y$  gauge symmetry,

- no neutral TGC vertex at LO.
- Charged TGC vertex at LO are only  $\lambda\downarrow\gamma = \lambda\downarrow Z = 0, g\downarrow Z\uparrow\uparrow = \kappa\downarrow\gamma = \kappa\downarrow Z = 1$ .

LO production diagram



# TESTING STANDARD MODEL ----TRIPLE GAUGE BOSON COUPLINGS



At the one-loop level,

fermion triangles generate nTGCs :  $10^{-4}$ ,

G. J. Gounaris, et. al. Phys. Rev. D 62, 073013 (2000)

Many new physics models

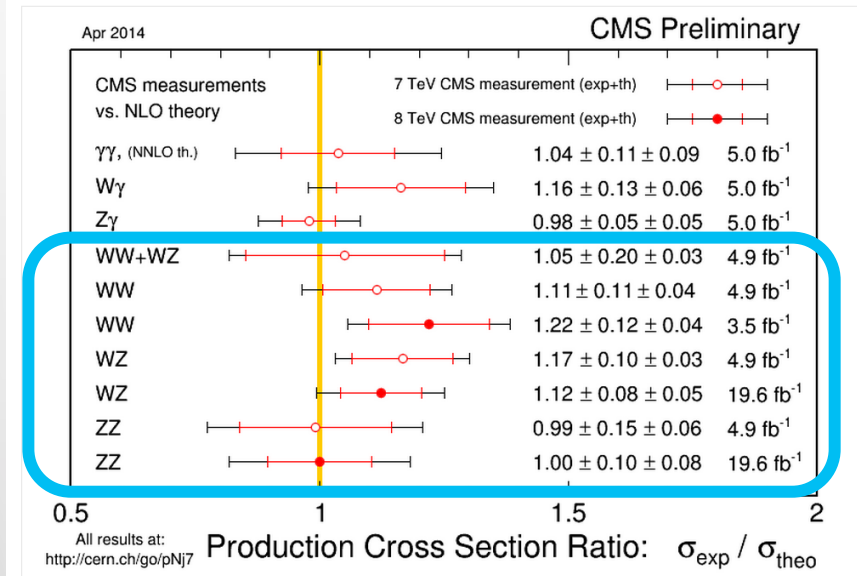
predict values of nTGCs :  $10^{-4} \sim 10^{-3}$ .

J. Ellison and J.Wudka, Annu. Rev. Nucl. Part. Sci. 48,33 (1998).

nTGC effects: often increase cross sections at high invariant mass ( $M_{VV}$ ) and its proxies ( $qT$ )

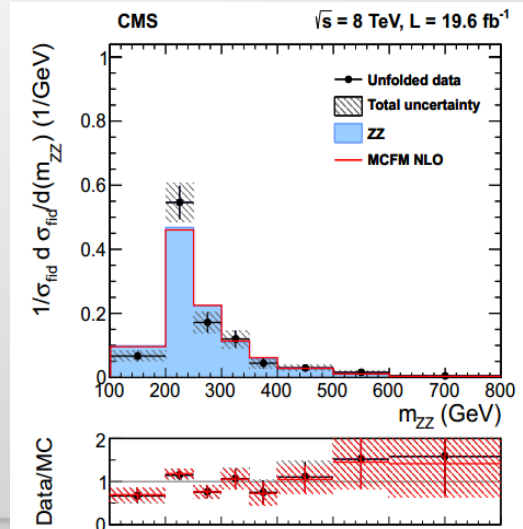
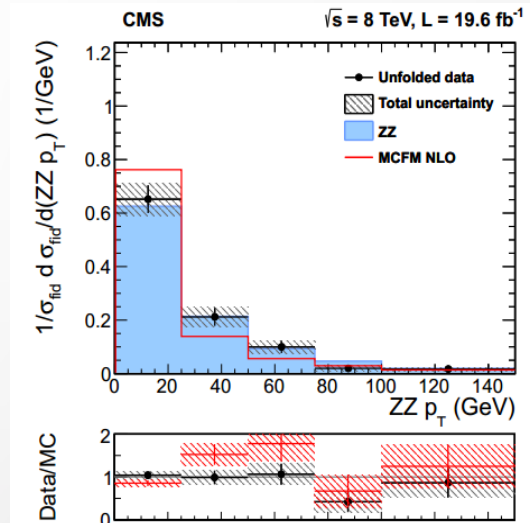
# EXPERIMENTS

The SM has been tested at a new energy frontier by the LHC **at 7 and 8 TeV**.



**For the total cross section, the discrepancies in  $W\uparrow + W\uparrow-$  channel between the measured data and the SM NLO calculation are about 20%. For  $W\uparrow \pm Z$  channel, they are about 10%.**

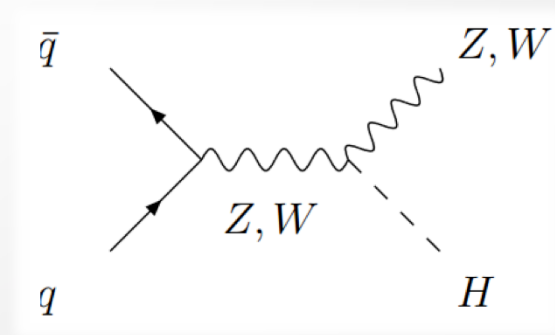
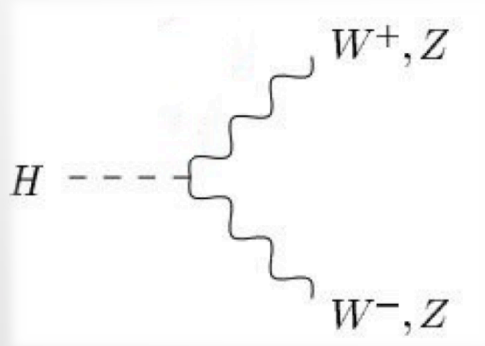
**Differential measurements are also different to some extent.**





# IRREDUCIBLE BACKGROUND

**Diboson production is a significant and irreducible background to Higgs production**



**It is sensitive to the production and decay of new particles predicted in models with extended Higgs sectors, extra vector bosons, extra dimensions or models such as Supersymmetry and Technicolor.**

# GAUGE BOSON PAIR PRODUCTION

- **The efforts of obtaining accurate theoretical prediction for this process has been for a long times.**
- **BEYOND NLO QCD**
  - **G. Chachamis, M. Czakon, and D. Eiras, JHEP 12 (2008) 003.**
  - **F. Campanario and S. Sapeta, Phys. Lett. B 718, 100 (2012).**
  - **M. Grazzini, JHEP 01, 15 (2006)**
  - **R. Frederix, M. Grazzini, PLB 662, 353 (2008)**
  - **S. Dawson, I.M. Lewis, and M. Zeng, Phys. Rev. D 88, 054028 (2013).**
  - **P. Meade, H. Ramani, and M. Zeng, Arxiv: 1407.4481**
- **NNLO QCD**
  - **T. Gehrmann, L. Tancredi and E. Weihs, JHEP 1308 (2013) 070**
  - **J. M. Henn, K. Melnikov and V. A. Smirnov, JHEP 05 (2014) 090**
  - **T. Gehrmann, A. Von Manteuffel, L. Tancredi and E. Weihs, JHEP 06 (2014) 032.**
  - **F. Caola, J. M. Henn, K. Melnikov and V. A. Smirnov, JHEP 1409 (2014) 043**
  - **F. Cascioli, T. Gehrmann, M. Grazzini, and S. Kallweit, et al, PLB 735 (2014) 311**

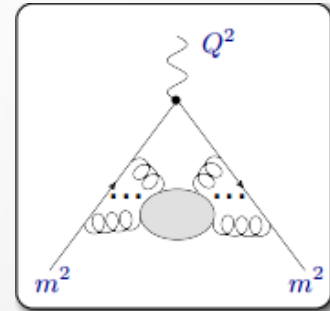
# WHY RESUMMATION

Generally, there will be large logarithms  $L = \ln Q/m$ , arising from hierarchy between small variable  $m$  and large scale  $Q$ , where  $Q \gg m$ .

So, the convergence is poor, and the fixed order predictions are unreliable.

Thus, these logarithms should be resummed to all order.

a short-distance scale  $Q$



a long-distance scale  $m$

LO	NLO	NNLO	NNNLO	
$1$	$+\alpha_s L^2$	$+\alpha_s^2 L^4$	$+\alpha_s^3 L^6 + \dots$	LL
	$+\alpha_s L$	$+\alpha_s^2 L^3$	$+\alpha_s^3 L^5 + \dots$	NLL
	$+\alpha_s$	$+\alpha_s^2 L^2$	$+\alpha_s^3 L^4 + \dots$	<b>NLL</b> <b>Resummation</b>
		$+\alpha_s^2 L$	$+\alpha_s^3 L^3 + \dots$	NNLL
		$+\alpha_s^2$	$+\alpha_s^3 L^2 + \dots$	...
			$+\alpha_s^3 L + \dots$	

**Fixed order**


# THRESHOLD RESUMMATION : WHY RESUMMATION

Generic observable in hadron collisions at energy  $\sqrt{s}$ :

$$\sigma(\tau, M^2) = \sigma_0 \int_{\tau}^1 dz/z \mathcal{L}(\tau/z) C(z, \alpha_s(M^2));$$

$$\tau = M^2/s$$

Parton luminosity.



$$\mathcal{L}(y, \mu_f) = \sum_{q, q'} \int_{\tau}^1 dx/x [f_q(x, \mu_f) f_{q'}(y/x, \mu_f)]$$

For the parton cross section  $C(z, \alpha_s)$ , it can be expanded as

$$C(z, \alpha_s) = \delta(1-z) + \sum_{n=1}^{\infty} C_n(z) \alpha_s^n; \quad z = M^2/s$$

When  $s$  is close to  $M^2$ ,  $\tau \rightarrow 1$ , since  $z \geq \tau$  is also close to 1.

$$C_n(z) \sim \log^{2n-1}(1-z)/(1-z)^{n+1}$$

The perturbative expansion is unreliable in this region.

The effect of soft-gluon resummation can be relevant even relatively far from the hadronic threshold.

# THRESHOLD RESUMMATION : FACTORIZATION FORMULAS IN SCET

YW, Chong Sheng Li, Ze Long Liu, Ding Yu Shao, Phys. Rev. D 90, 034008 (2014)

We can factorize the resummed cross section as

$$d\sigma/dM \downarrow VZ \uparrow 2 \sim H(\mu \downarrow h) \cdot S(\mu \downarrow s) \otimes \phi(\mu \downarrow f)$$

The renormalization-group equation for the hard function is

$$\frac{d}{d \ln \mu} \mathcal{H}_{VZ}(M_{VZ}, \mu) = 2 \left[ \Gamma_{\text{cusp}}^F(\alpha_s) \ln \frac{-M_{VZ}^2}{\mu^2} + 2\gamma^q(\alpha_s) \right] \mathcal{H}_{VZ}(M_{VZ}, \mu),$$

defining

$$\mathcal{H}_{V_i Z} = \mathcal{H}_{V_i Z}^{(0)} + \frac{\alpha_s}{4\pi} \mathcal{H}_{V_i Z}^{(1)} + \dots$$

The exact solution to

$$H(-M^2, \mu \downarrow f) = \exp(4S(\mu \downarrow h, \mu \downarrow f) - 4a \downarrow \gamma(\mu \downarrow h, \mu \downarrow f)) (-M^2 / \mu \downarrow h^2)^{\uparrow - a \downarrow \Gamma(\mu \downarrow f)}$$

# THRESHOLD RESUMMATION : FACTORIZATION FORMULAS IN SCET

We choose  $\mu \ll \Lambda \ll M$  to eliminate  $\pi^2$  terms arising from  $\text{Log}[-\mu \ll \Lambda \ll M]$ .

Meantime we need evaluated  $\alpha_s(-\mu \ll \Lambda \ll M)$  to  $\alpha_s(\mu \ll \Lambda \ll M)$  by the equation

$$\frac{\alpha_s(\mu^2)}{\alpha_s(-\mu^2)} = 1 - ia(\mu^2) + \frac{\alpha_s(\mu^2)}{4\pi} \left[ \frac{\beta_1}{\beta_0} \ln[1 - ia(\mu^2)] \right] + \mathcal{O}(\alpha_s^2),$$

The soft function is defined as

$$\mathcal{S}(s(1-z)^2, \mu) = \sqrt{s} W(s(1-z)^2, \mu),$$

The momentum-space Wilson loop obeys the integro-differential evolution equation

$$dW(\omega, \mu)/d\ln\mu = -(4\Gamma_{\text{cusp}}(\alpha_s) \ln\omega/\mu + 2\gamma(\alpha_s))W(\omega, \mu)$$

$$-4\Gamma_{\text{cusp}}(\alpha_s) \int_0^\omega d\omega' W(\omega', \mu) - W(\omega, \mu)/(\omega - \omega')$$

# THRESHOLD RESUMMATION : FACTORIZATION FORMULAS IN SCET

the exact solution can be written in the form

$$\omega W(\omega^2, \mu_f) = \exp(-4S(\mu_s, \mu_f) + 2a_{\gamma W}(\mu_s, \mu_f)) \tilde{s}(\partial_\eta, \mu_s) \left(\frac{\omega^2}{\mu_s^2}\right)^\eta \frac{e^{-2\gamma\eta}}{\Gamma(2\eta)},$$

After combining the soft and hard function, the differential cross section can be factorized as

$$\frac{d\sigma}{dM_{VZ}^2} = \frac{\sigma_0}{S} \int_\tau^1 \frac{dz}{z} \mathcal{L}\left(\frac{\tau}{z}, \mu_f\right) \mathcal{H}_{VZ}(M_{VZ}, \mu_h) C(M_{VZ}, \mu_h, \mu_s, \mu_f),$$

where

$$C(M, \mu_h^2, \mu_s^2, \mu_f^2) = \exp[4S(\mu_h, \mu_s) - 2a_{\gamma V}(\mu_h, \mu_s) + 4a_{\gamma\phi}(\mu_s, \mu_f)] \left(\frac{M^2}{\mu_h^2}\right)^{-2a_\Gamma(\mu_s, \mu_h)} \frac{(1-z)^{2\eta-1}}{z^\eta} \tilde{s}\left[\log\left(\frac{(1-z)^2 M^2}{z\mu_s^2}\right) + \partial_\eta, \mu_s\right] \frac{e^{-2\gamma\eta}}{\Gamma(2\eta)}$$

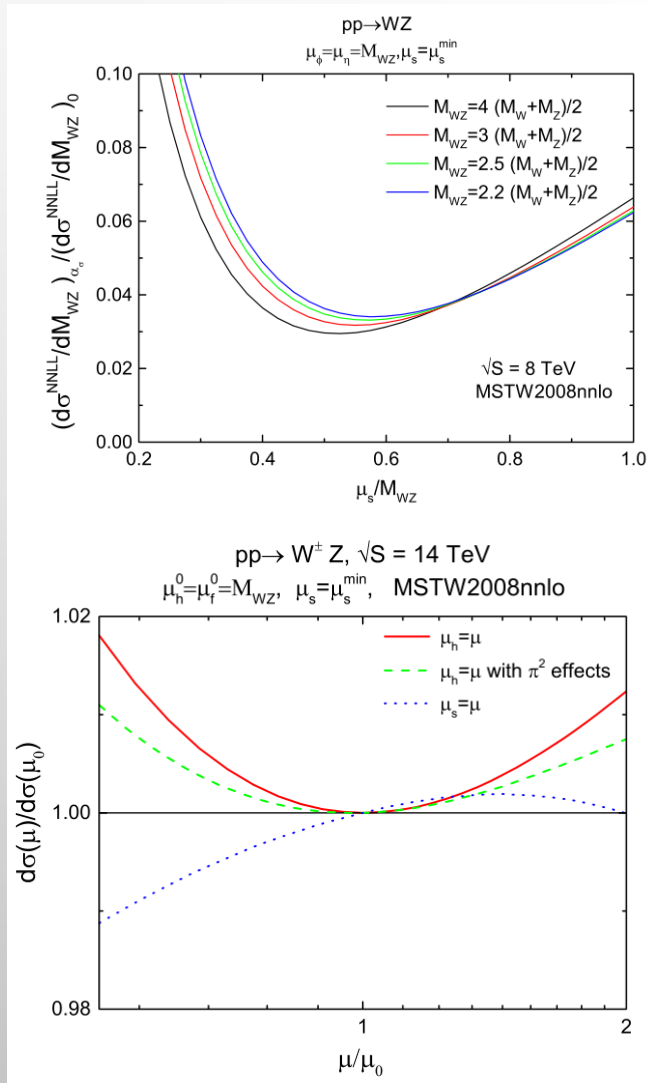


# THRESHOLD RESUMMATION : THE SCALE SETTINGS

## --- $W^\pm Z$ FOR EXAMPLE

In the following, we take  $W^\pm Z$  production as an example.

The behavior of  $ZZ$  is very similar.



The contribution of the one-loop corrections of the soft functions as a function of  $\mu_s / M_{WZ}$ .

The requirement: have a well-behaved stability.

$$\mu_{s,W^\pm Z}^{\min} = M_{W^\pm Z} \frac{1 - \tau}{(3.004\sqrt{\tau} + 1.339)^{2.134}},$$

$$\mu_{s,ZZ}^{\min} = M_{ZZ} \frac{1 - \tau}{(3.013\sqrt{\tau} + 1.323)^{2.356}}.$$

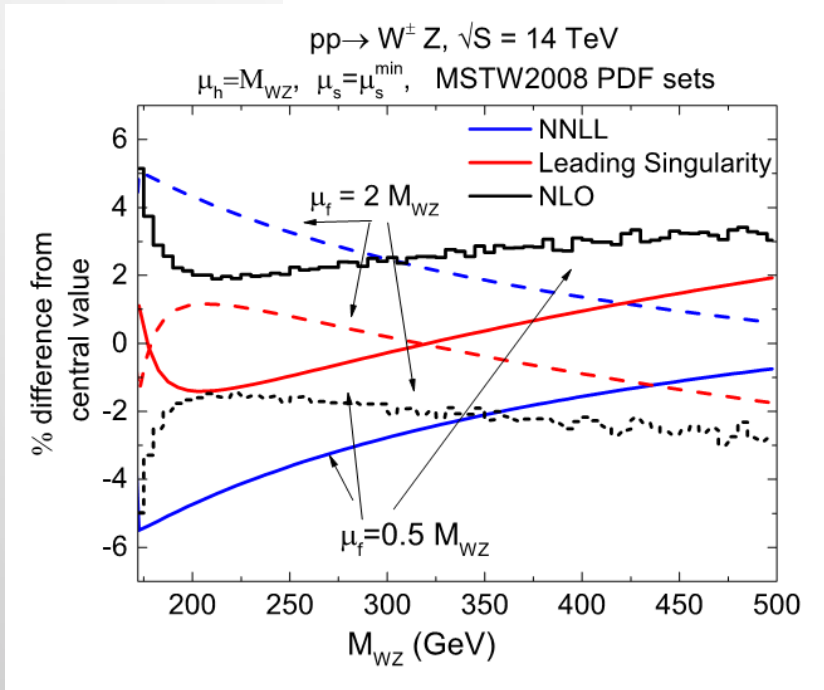
Scale dependence of the resummed cross section on  $\mu_s$  and  $\mu_h$

# THRESHOLD RESUMMATION : FACTORIZATION SCALE DEPENDENCE

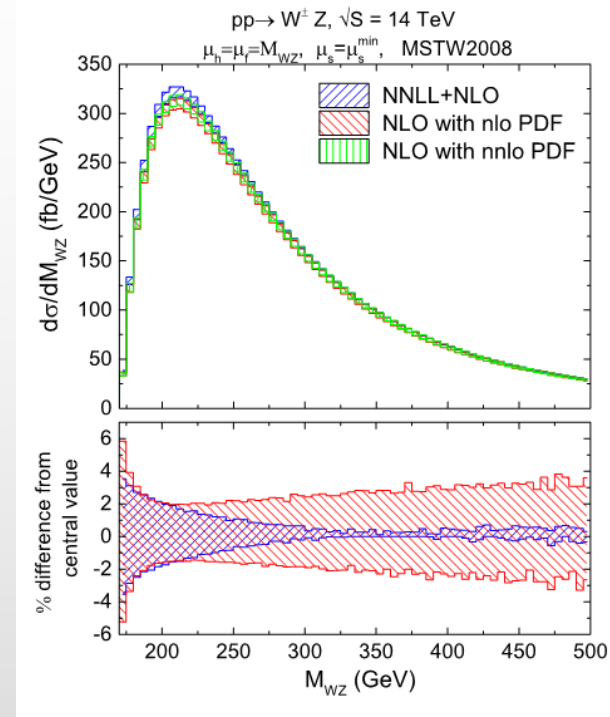
--- $W^\pm Z$  FOR EXAMPLE

In order to get the total cross section, we should including the nonsingular terms :

$$\frac{d\sigma^{\text{NNLL+NLO}}}{dq_T} = \frac{d\sigma^{\text{NNLL}}}{dq_T} + \left[ \frac{d\sigma^{\text{NLO}}}{dq_T} - \frac{d\sigma^{\text{NNLL}}}{dq_T} \right]_{\text{expanded to NLO}}$$



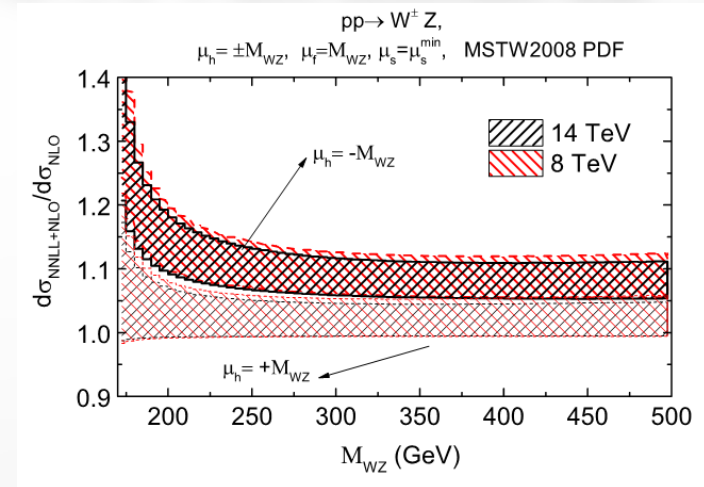
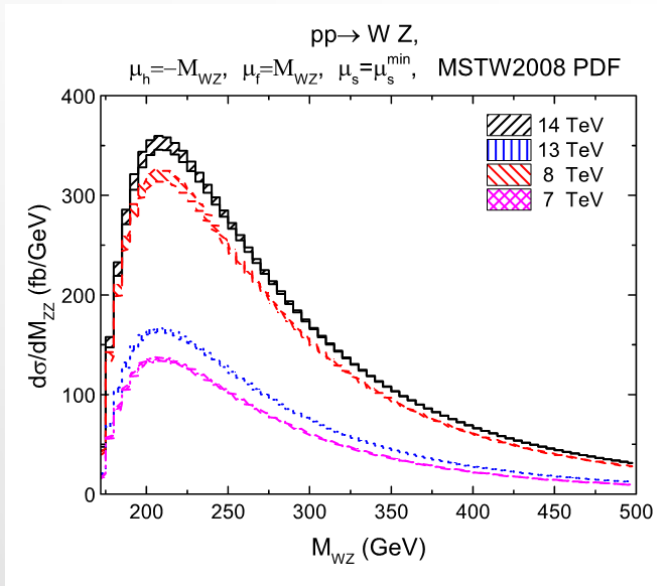
The factorization scale dependences of the three part cancel each other



The final NNLL+NLO results have a factorization scale dependence.

# THE INVARIANT MASS DISTRIBUTION

## --- $W^{\pm}Z$ FOR EXAMPLE

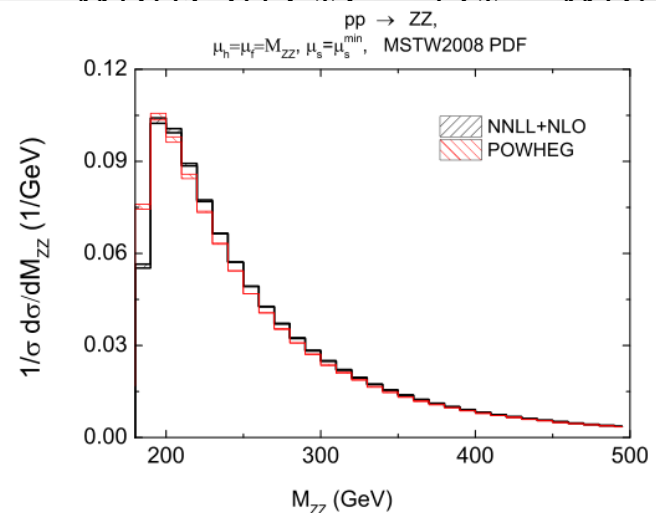


The invariant mass distributions with

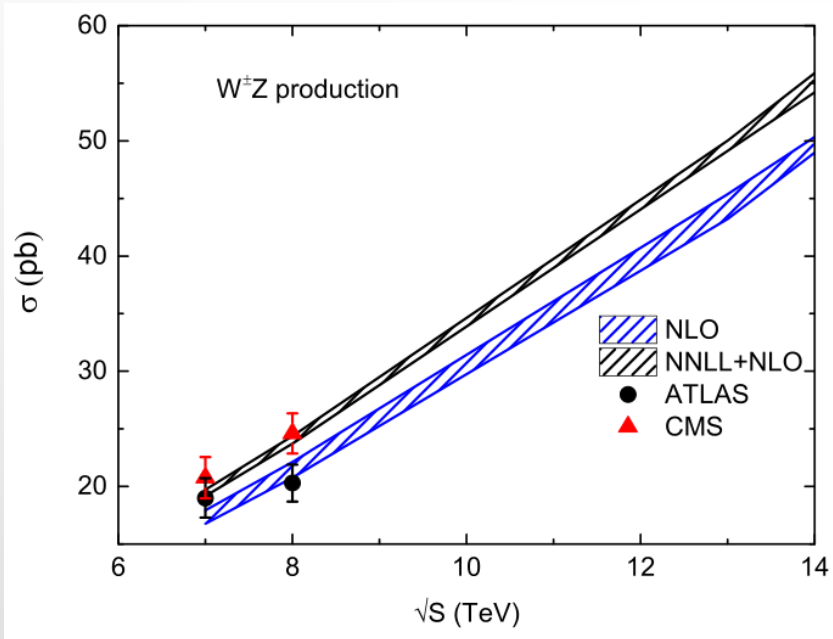
$\mu_h = \pm M_{WZ}$   
 $\mu_f = M_{WZ}$   
 $\mu_s = \mu_s^{\min}$

We compare the normalized invariant mass distribution with the predictions by POWHEG

They agree with each other very well.

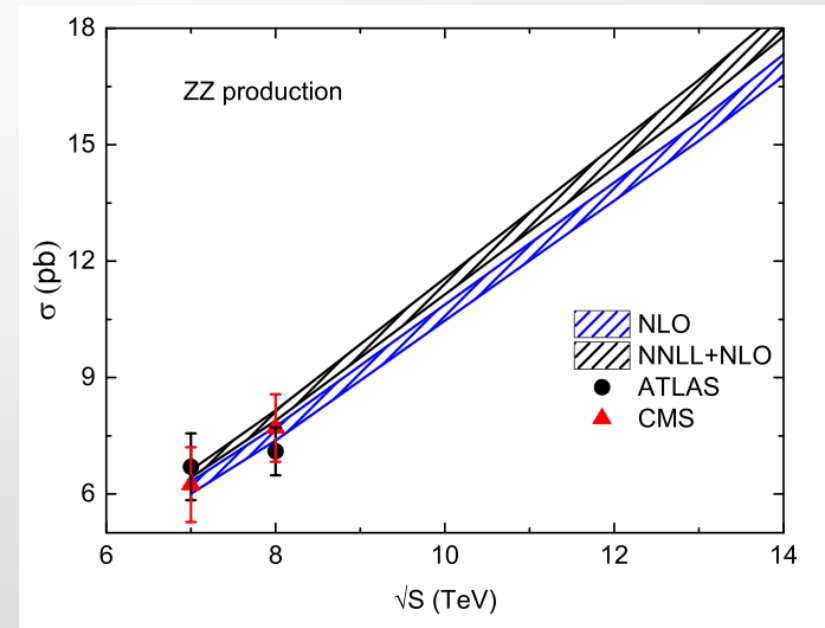


# RESUMMED PREDICTION: THE TOTAL CROSS SECTION



The total cross sections with different center-of-mass energies for gauge boson pair production at the LHC.

**They agree to the experiment data very well.**

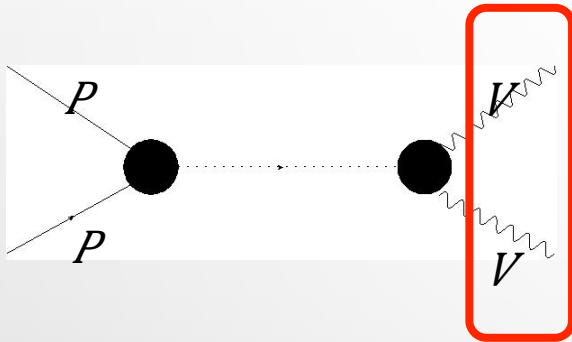


# CONCLUSION

- Presenting NLO + NNLL threshold resummations for  $W^{\pm}Z$  and  $ZZ$  productions, with  $\pi^2$  enhancement effects
- The results decrease the scale dependences, especially for the  $W^{\pm}Z$  production .
- Resummation results increase the NLO cross section by about 8% for  $ZZ$  and 12% for  $WZ$ .
- Results agree with powheg and experimental data very well.

# $q \downarrow T$ DISTRIBUTION : WHY RESUMMATION

bind together  $\rightarrow q \downarrow T$



The large logarithms  $L = \ln \mu \downarrow h / q \downarrow T$  arise from the hierarchy of the small transvers momentum of the gauge boson pair and hard scattering scale.



- No resummation predictions for the  $W \uparrow \pm Z$  production before.
- The resummation for  $W \uparrow + W \uparrow -$  and  $ZZ$  are calculated to NLO + NLL in the CSS framework.
- We performed the NLO + NNLL resummation for  $W \uparrow + W \uparrow -$ ,  $W \uparrow \pm Z$  and  $ZZ$  production at the LHC.

# $q \downarrow T$ RESUMMATION : FACTORIZATION FORMULAS IN SCET

YW, Chong Sheng Li, Ze Long Liu, Ding Yu Shao and Hai Tao Li, Phys. Rev. D 88, 114017 (2013)

**We can factorize the total cross section as :**

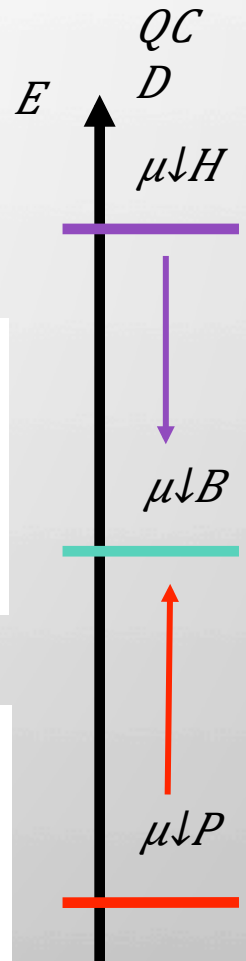
$$d\sigma = \underbrace{\phi_{i,j}}_{\mu \downarrow H} \times \underbrace{I_{i,j}}_{\Lambda \downarrow QCD} \times \underbrace{H}_{\mu \downarrow B}$$

**Combining the evolution effects of the hard function and beam function, we get**

$$\frac{d^2\sigma}{dq_T^2 dy} = \frac{1}{S} \sum_{i,j=q,q',g} \mathcal{H}_{VV}(M, \mu_f) \int_{\xi_1}^1 \frac{dz_1}{z_1} \int_{\xi_2}^1 \frac{dz_2}{z_2} \bar{C}_{qq' \rightarrow ij}(z_1, z_2, q_T^2, \mu_f) \times \phi_{i/N_1}(\xi_1/z_1, \mu_f) \phi_{j/N_2}(\xi_2/z_2, \mu_f) + (q, i \leftrightarrow q', j).$$

**where**

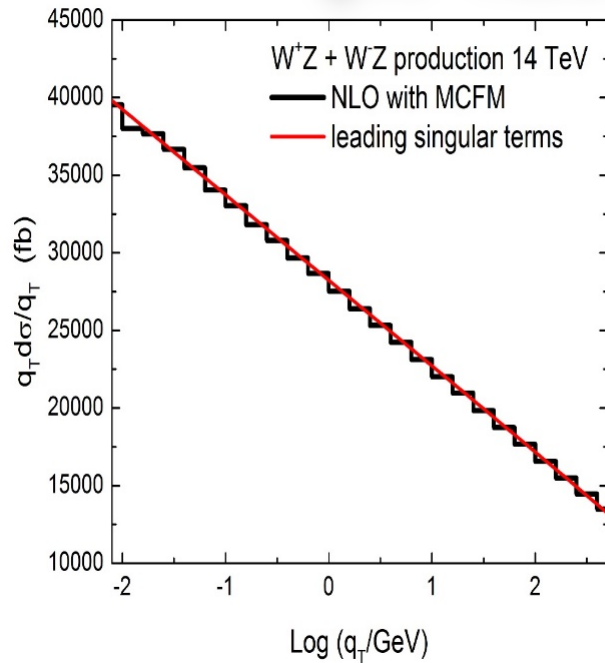
$$\bar{C}_{qq' \rightarrow ij}(z_1, z_2, q_T^2, \mu_f) = \frac{1}{2} \int_0^\infty dx_T x_T J_0(x_T q_T) \exp[g_F(\eta, L_\perp, \alpha_s)] \times [\bar{I}_{q \leftarrow i}(z_1, L_\perp, \alpha_s) \bar{I}_{q' \leftarrow j}(z_2, L_\perp, \alpha_s)],$$





# $q \downarrow T$ RESUMMATION : PREDICTION

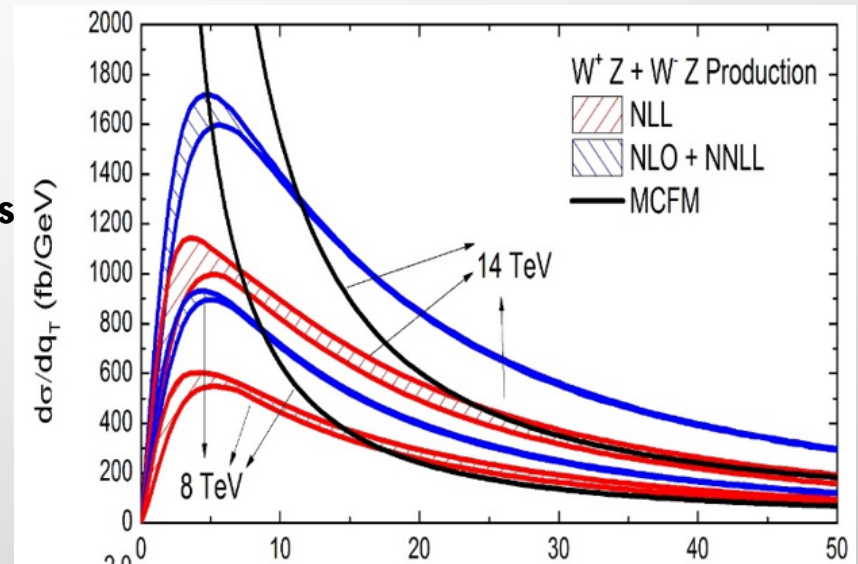
---  $W^{\pm} Z$  FOR EXAMPLE



Comparison of leading singular terms and exact NLO cross section in the small  $q \downarrow T$  region.

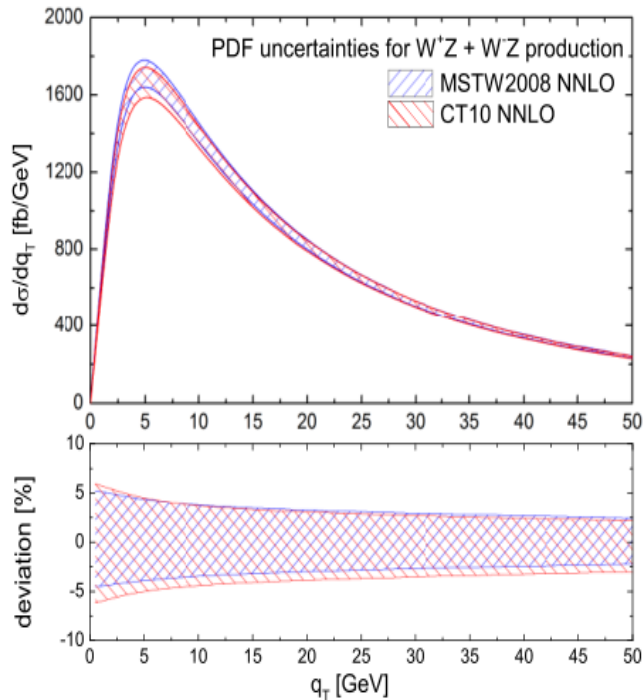
Compare the NNLL  $q \downarrow T$  distribution predictions with the NLL and NLO results.

The uncertainties of the NNLL prediction are much smaller than those of the NLL. Scale uncertainties  $\Delta\sigma \leq 1\%$ , when  $q \downarrow T > 10$  GeV.  $\Delta\sigma \leq 4\%$ , at peak position.



# $q \downarrow T$ RESUMMATION : PREDICTION

---  $W \uparrow_{\pm} Z$  FOR EXAMPLE



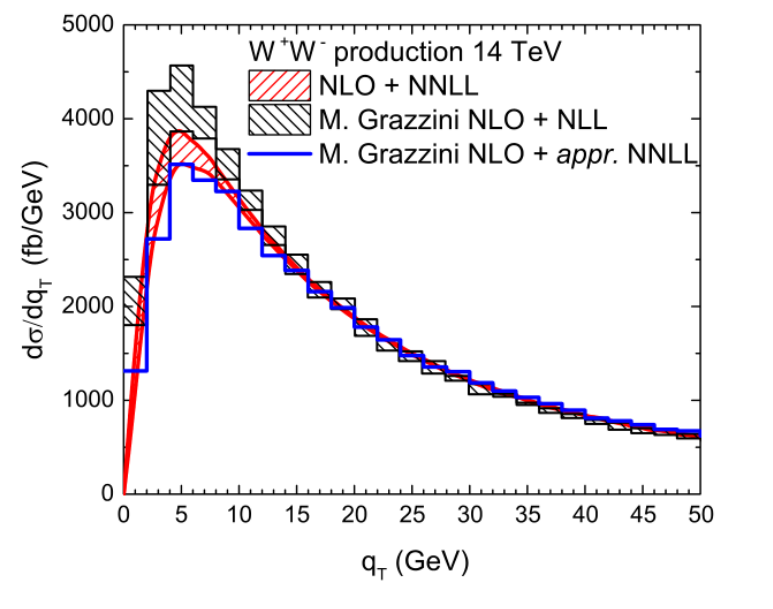
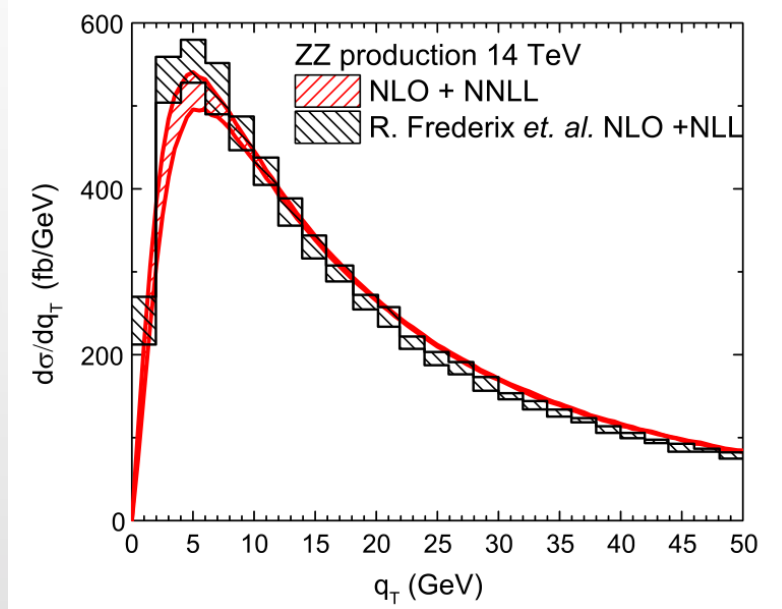
**PDF uncertainties with MSTW2008 NNLO 90cl and CT10 NNLO 90cl.**

**In the large  $q \downarrow T$  region:  $< 2.5\%$**

**In the peak position:  $< 4\%$ ,**

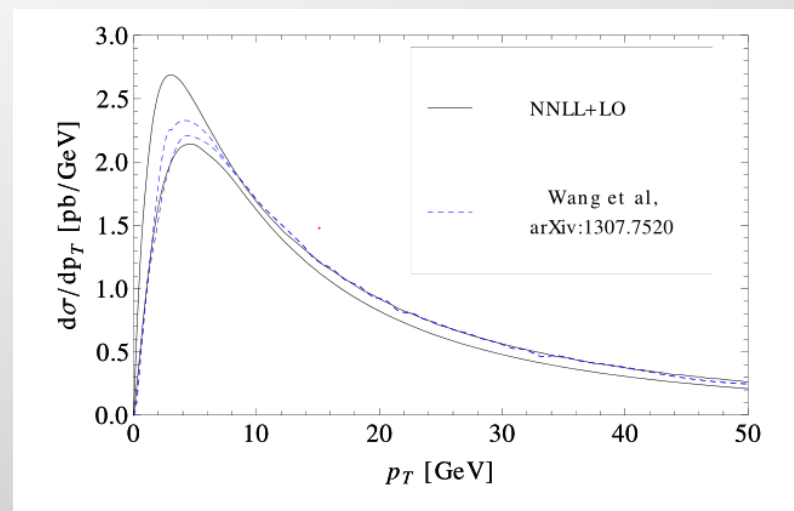
**which are comparable with the scale uncertainties.**

# $q\downarrow T$ RESUMMATION : COMPARE OTHER'S WORK



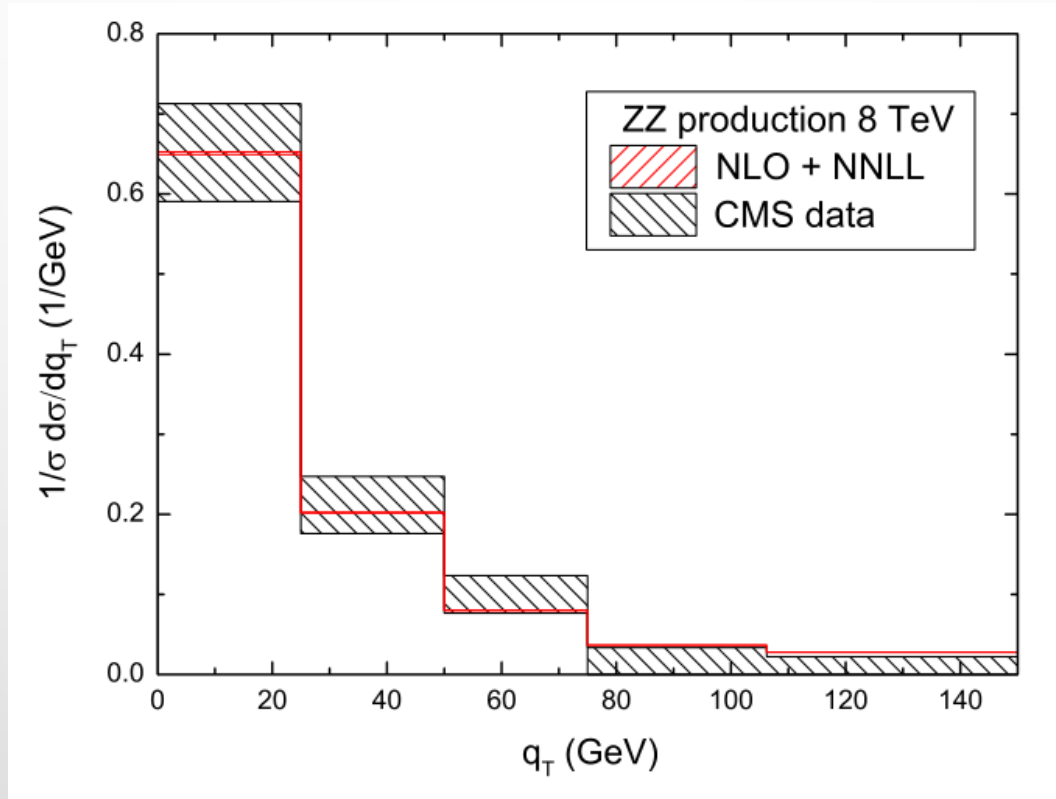
**Compare the results in the SCET framework with the prediction in CSS framework. They agree with each other**

Patrick Meade, Harikrishnan Ramani, Mao Zeng, [arXiv:1407.4481](https://arxiv.org/abs/1407.4481)



$q \downarrow T$

# RESUMMATION : COMPARE WITH EXPERIMENT



Compare with the data with  $19.6 \text{ fb}^{-1}$  at  $\sqrt{s} = 8 \text{ TeV}$  at the LHC by the CMS collaboration (CMS PAS SMP-13-005 ).

# CONCLUSION

- Presenting **NLO + NNLL transverse momentum resummations for  $W\uparrow$  +  $W\uparrow^-$ ,  $W\uparrow_{\pm} Z$  and  $ZZ$  productions, including  $\pi^{\uparrow 2}$  enhancement effects.**
- **Scale dependences are decreased obviously.**
- **Results agree with the experimental data, as well as the the prediction in the traditional method very well .**