

# Dynamical origin of $A_{FB}^t$ and $A_{FB}^\ell$ correlation

Qing-Hong Cao (曹庆宏)

Peking University

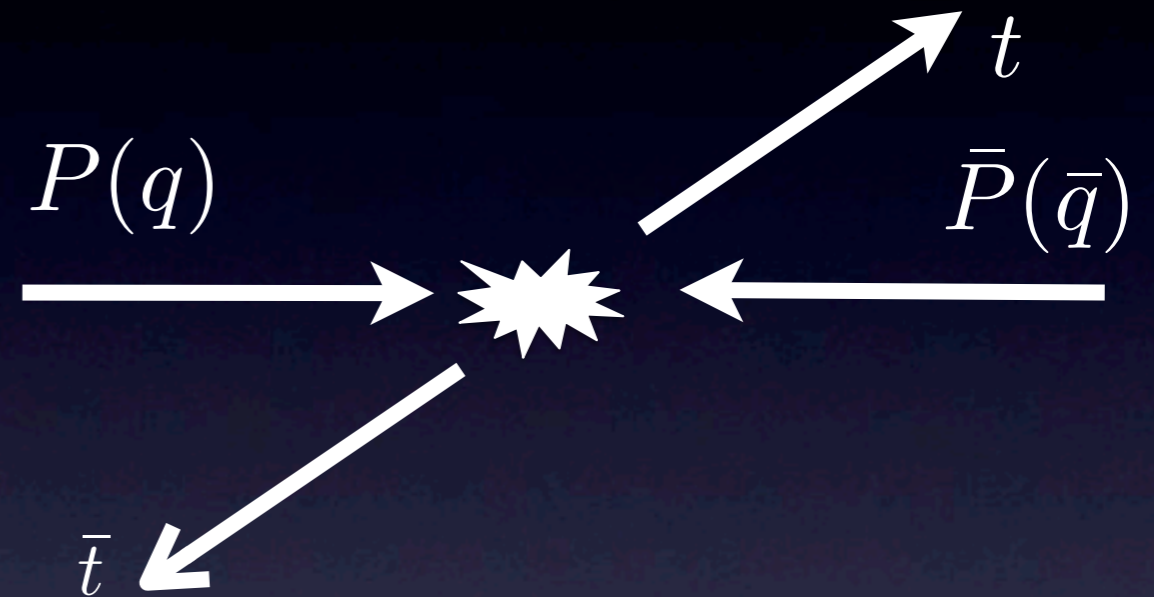
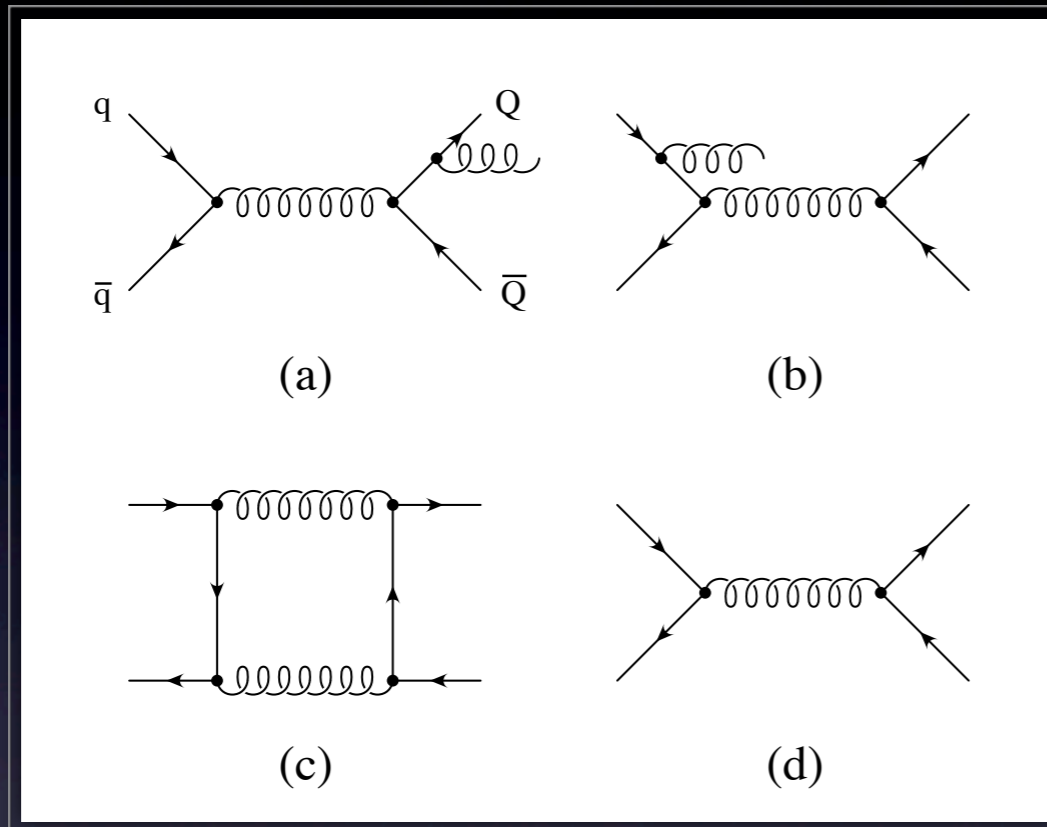
## References:

E. Berger, QHC, Chuan-Ren Chen, Jiang-Hao Yu and Hao Zhang,  
arXiv:1111.3641



# Top-quark F-B asymmetry in the SM

- A charge asymmetry arises at NLO



Top quarks are produced along the direction of the incoming quark

$$A^{p\bar{p}} = \frac{N_t(y > 0) - N_{\bar{t}}(y > 0)}{N_t(y > 0) + N_{\bar{t}}(y > 0)} = 0.051(6)$$

$$A^{t\bar{t}} = \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)} = 0.078(9) \quad \Delta y = y_t - y_{\bar{t}}$$

# Timeline of top-quark $A_{FB}$

SM theo. Prediction

Brown, Ellis, Rainwater  
 hep-ph/0509267  
 Collider simulation of  $tt+0(1)j$   
 Measuring AFB is very challenging

Almeida, Sterman, Vogelsang  
 0805.1885  
 NLL Threshold resum.  
 Asymmetry is robust

Melnikov, Schulze  
 1004.3284  
 Confirm Dittmaier et al

Kuhn, Rodrigo  
 hep-ph/9802268  
 SM NLO QCD  
 $A_{FB}^t = 5\%$

Dittmaier, Uwer, Weinzierl  
 hep-ph/0703120  
 NLO QCD corr. to  $t\bar{t}+j$

Ahrens, Ferroglia, Neubert,  
 Pecjak, Li Lin Yang,  
 1003.5827  
 SCET NNLL

1998

2005

2007

2008

2010

2011

Exp. Measurements

D0 (1.9 fb<sup>-1</sup>)  
 0712.0851  
 uncorrected  
 $A_{FB} = [12 \pm 8 \pm 1]\%$

CDF (1.9 fb<sup>-1</sup>)  
 0806.2472  
 $A_{FB} = [24 \pm 14]\%$   
 Consistent with SM

CDF (5.3fb<sup>-1</sup>)  
 1101.0034  
 $A_{FB} = 0.475 \pm 0.114$   
 for  $m_{t\bar{t}} \geq 450$  GeV

D0 (5.4fb<sup>-1</sup>)  
 1107.4995  
 $A_{FB}^t = [19.6 \pm 6.5]\%$   
 $A_{FB}^\ell = [15.2 \pm 4.0]\%$

# $A_{FB}^{\ell}$ versus $A_{FB}^t$

D0:  $A_{FB}^t = 0.196 \pm 0.065$

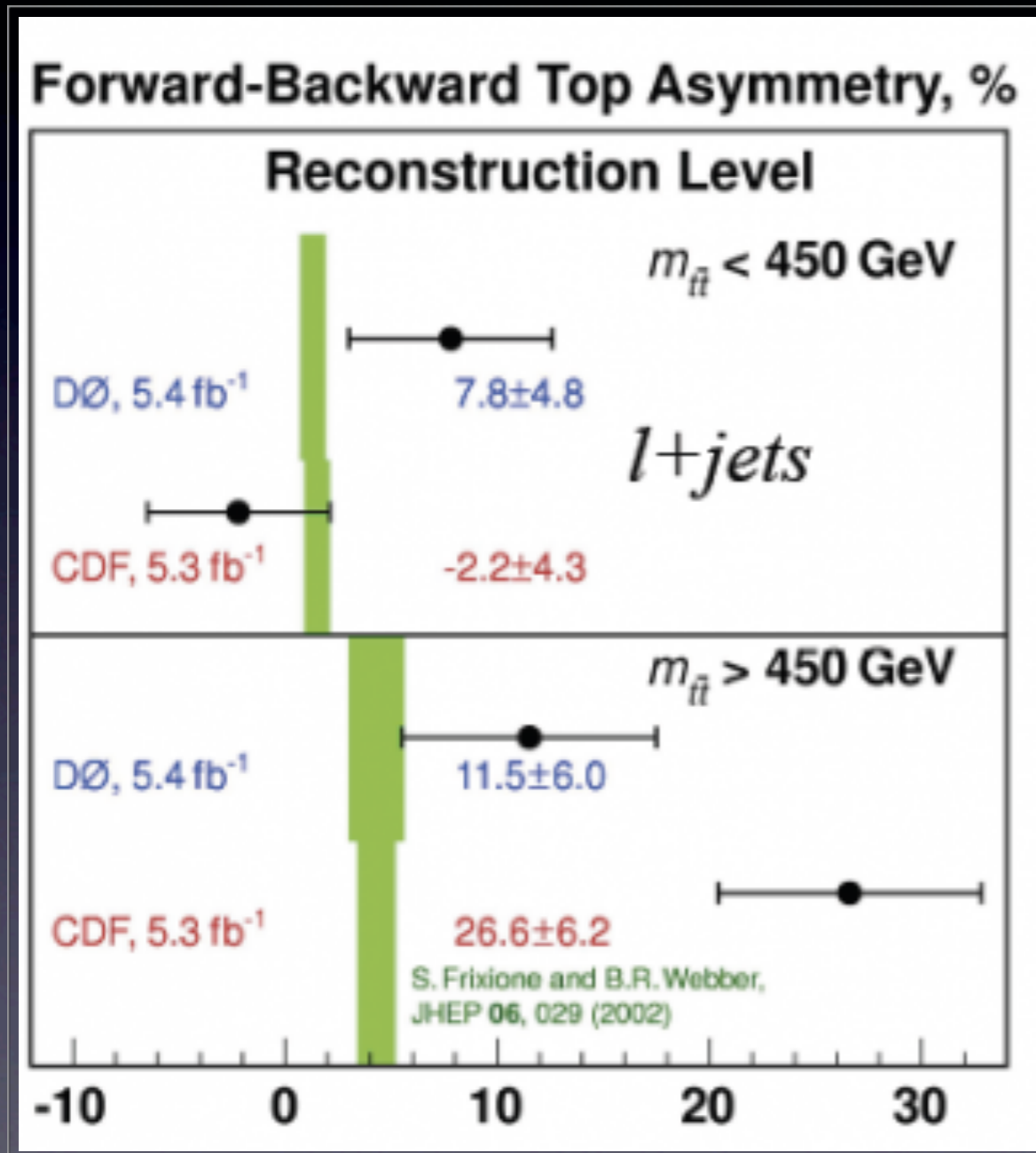
$A_{FB}^{\ell} = 0.152 \pm 0.040$

$$\left. \frac{A_{FB}^{\ell}}{A_{FB}^t} \right|_{D0} \sim \frac{3}{4}$$

SM:  $A_{FB}^t = 0.051 \pm 0.001$

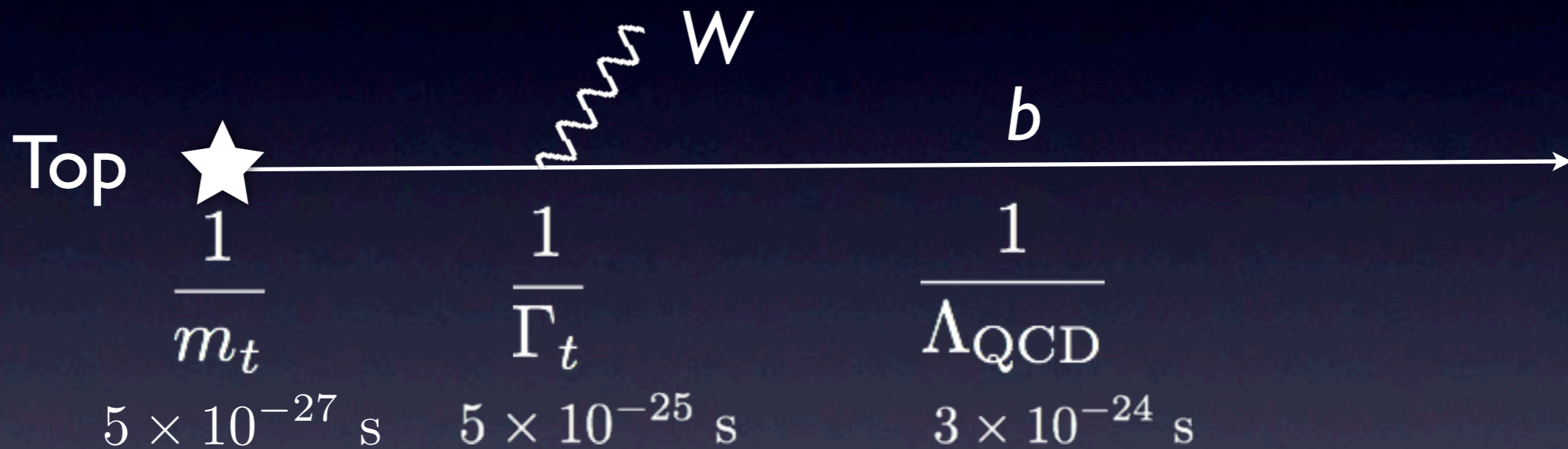
$A_{FB}^{\ell} = 0.021 \pm 0.001$

$$\left. \frac{A_{FB}^{\ell}}{A_{FB}^t} \right|_{SM} \sim \frac{1}{2}$$

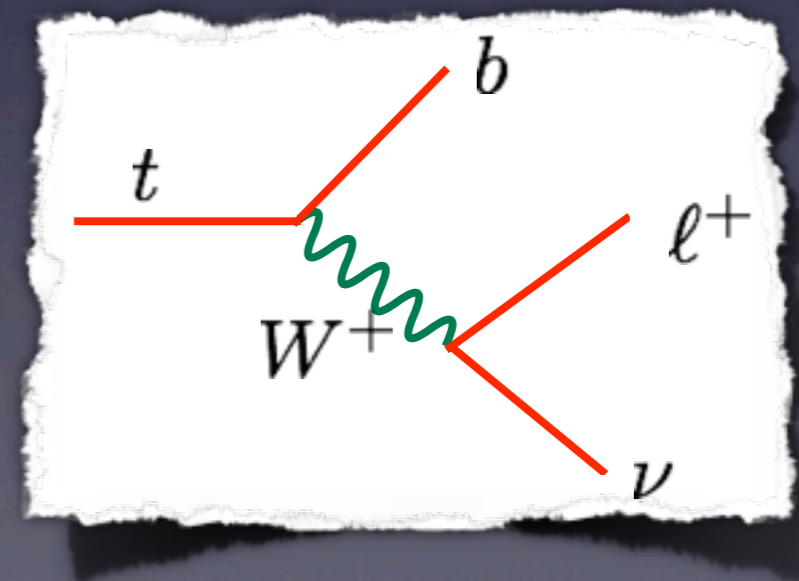


# Top-quark: king of the SM

- Large mass: 173 GeV
- Short lifetime:



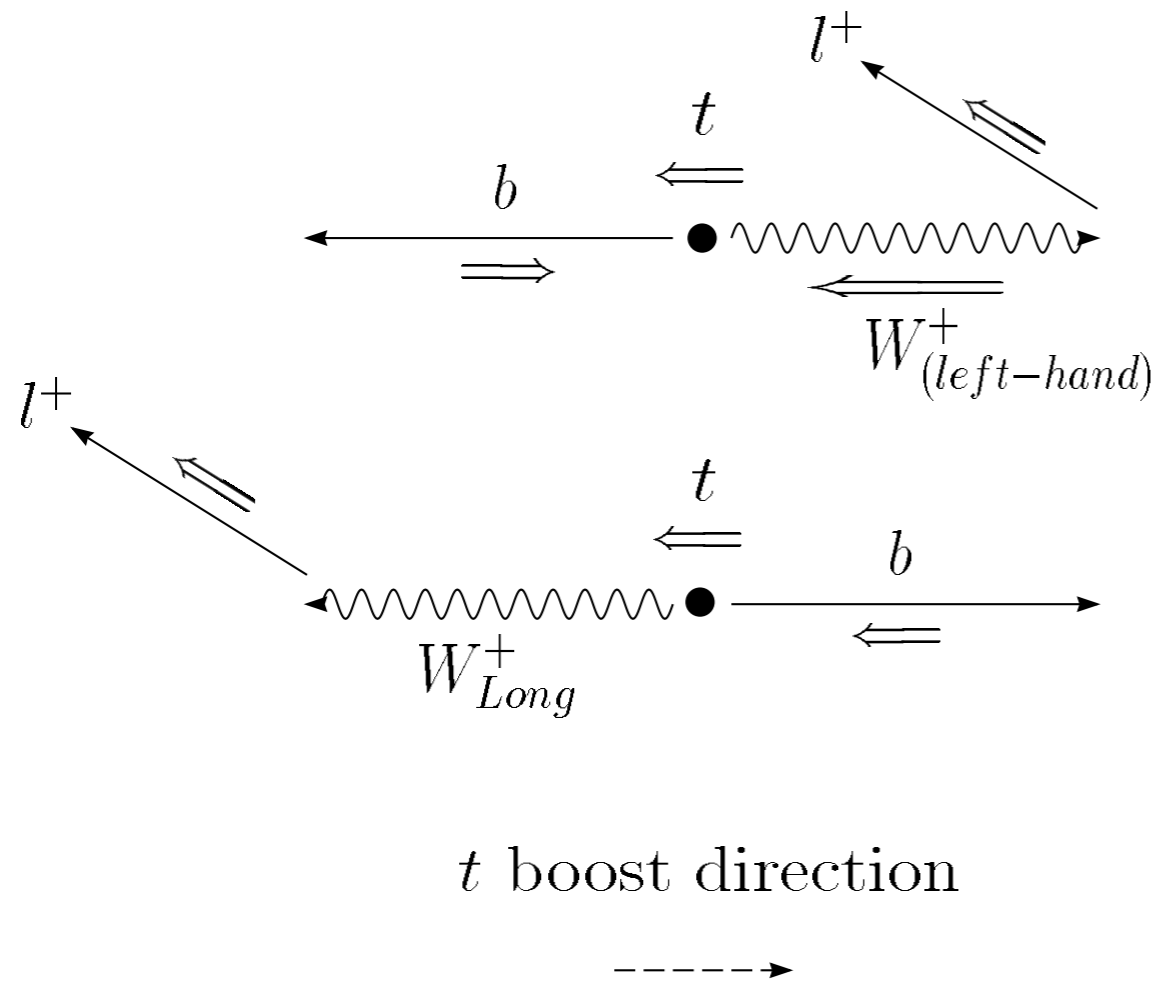
- “bare” quark:  
spin info well kept among  
its decay products



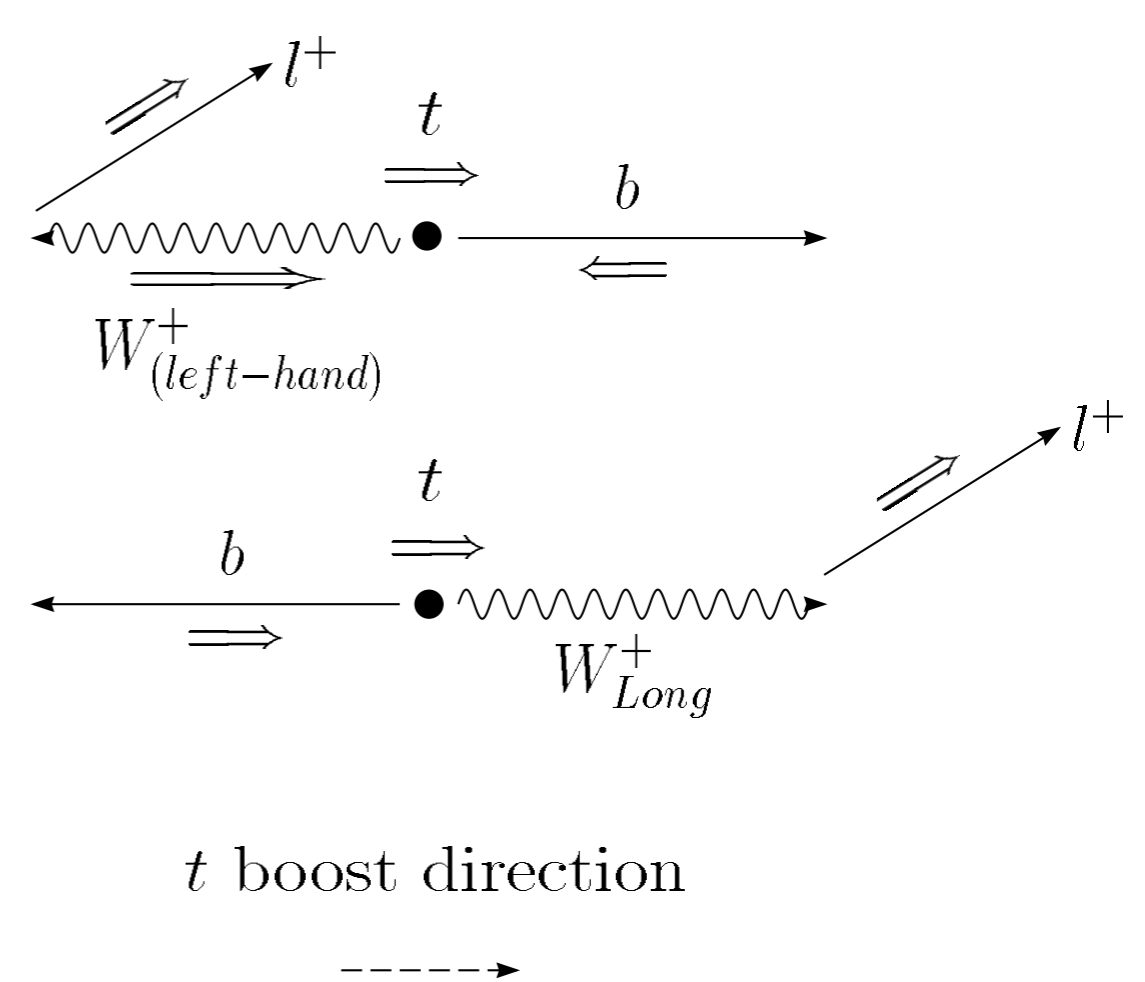
# Top-quark leptonic decay

- Charged lepton: top-quark spin analyzer

(a) left-handed top



(b) right-handed top



The charged-lepton tends to follow the top-quark spin direction.

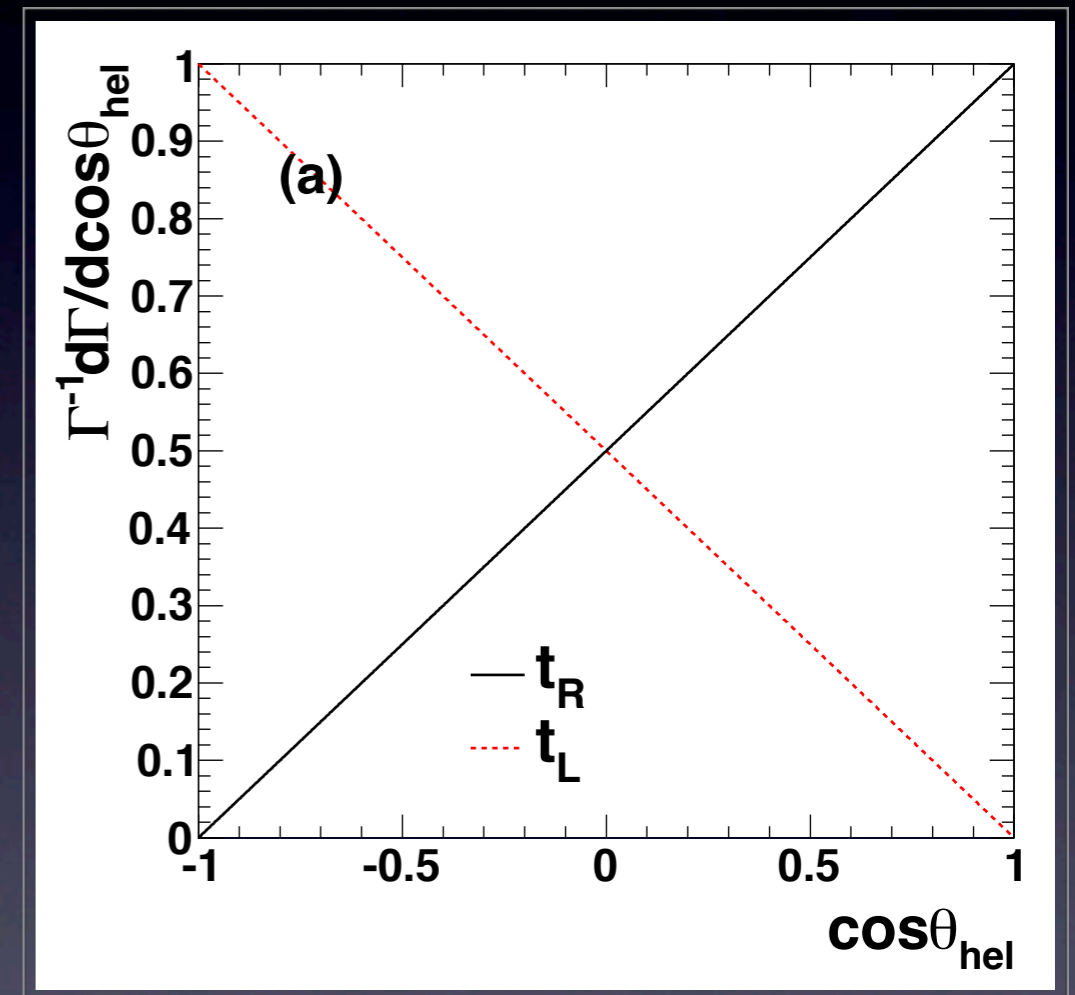
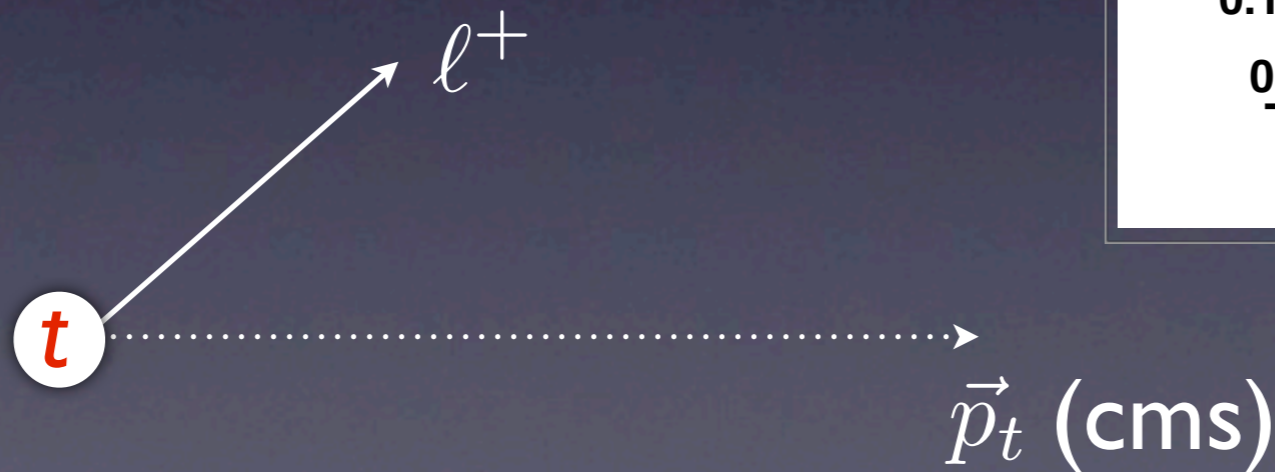
# Charged lepton distribution

- In top-quark rest frame

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{1 + \lambda_t \cos \theta_{\text{hel}}}{2}$$

$\lambda_t = +$  right-handed

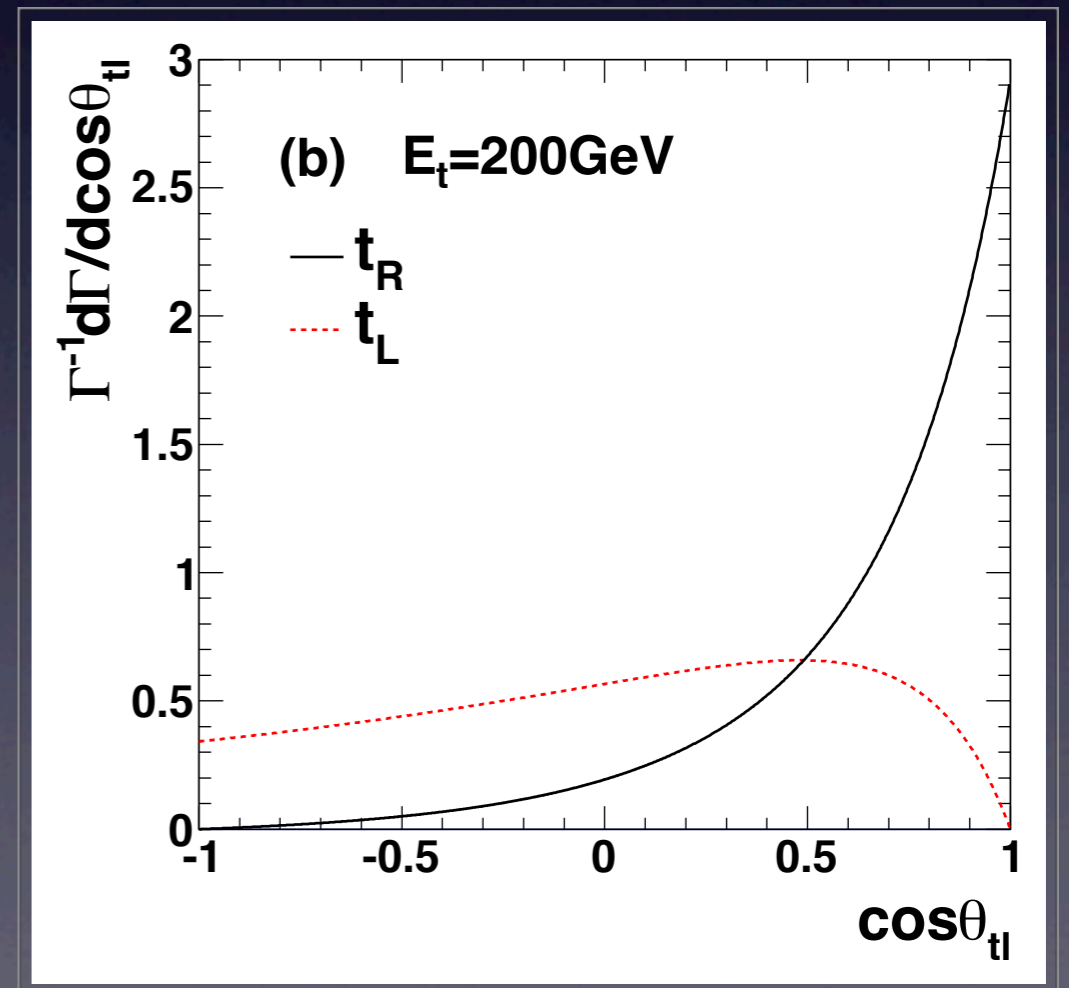
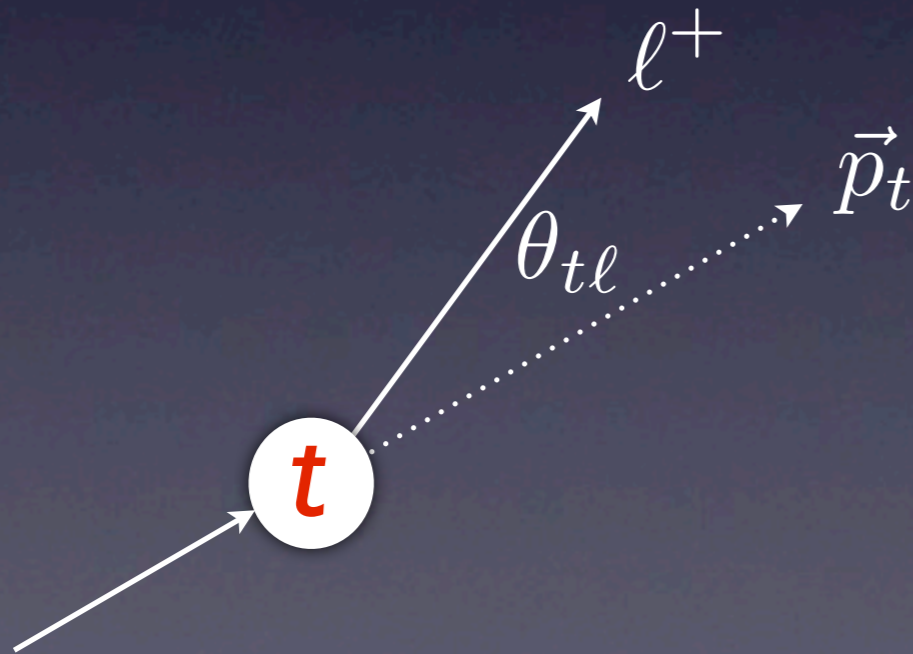
$\lambda_t = -$  left-handed



# Charged lepton distribution

- In the c.m. frame

$$\frac{d\Gamma}{\Gamma d\cos\theta_{t\ell}} = \frac{1 - \beta \cos\theta_{t\ell} + \lambda_t (\cos\theta_{t\ell} - \beta)}{2\gamma^2 (1 - \beta \cos\theta_{t\ell})^3}$$



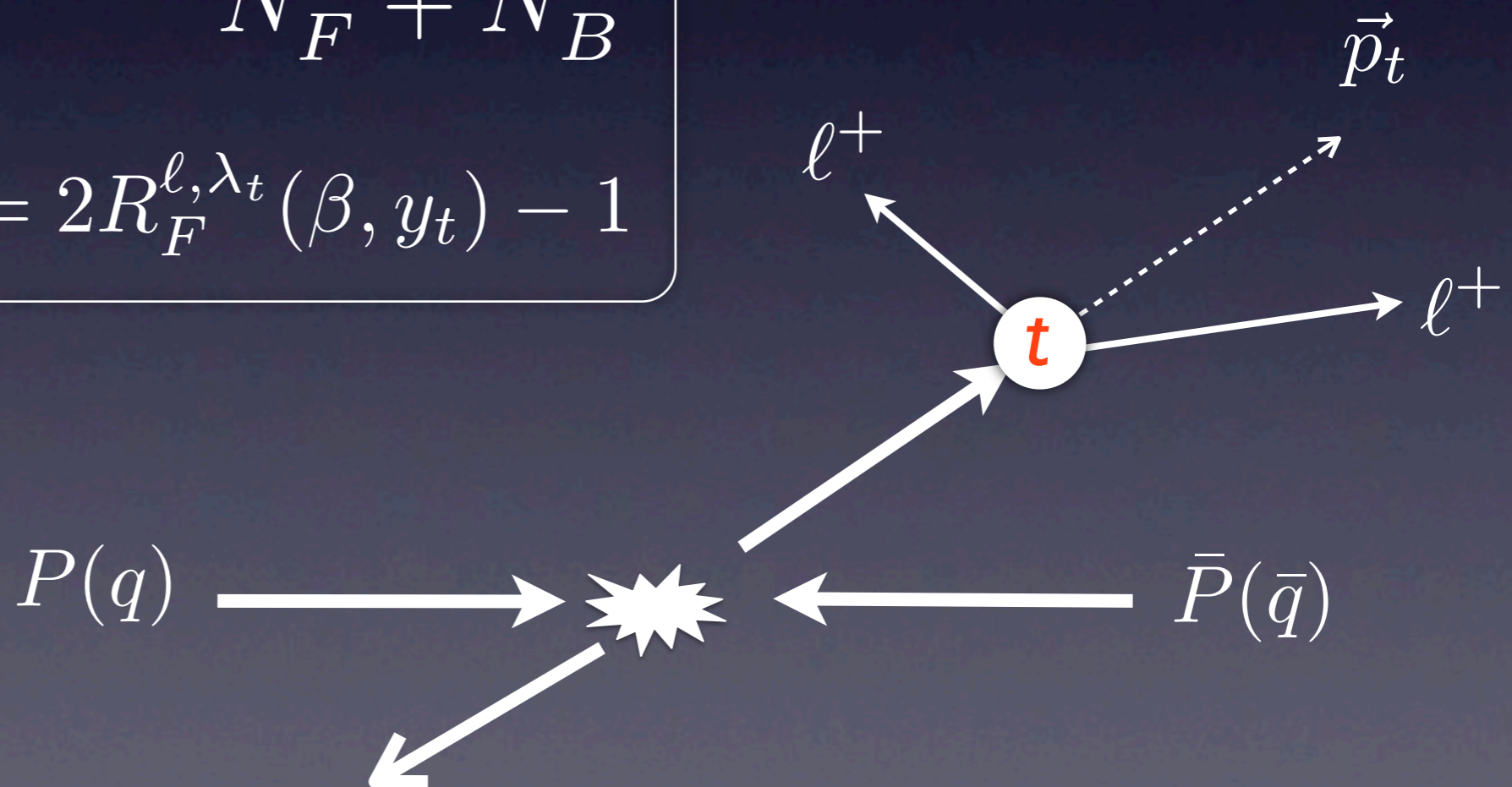


# $A_{FB}^\ell$ dependence on top kinematics

- Possibility of lepton in the forward region of detector for a top-quark  $(\beta, y_t, \lambda_t)$

$$R_F^{\ell, \lambda_t}(\beta, y_t) = \frac{N_F^\ell}{N_F^\ell + N_B^\ell}$$

$$A_{FB}^{\ell, \lambda_t}(\beta, y_t) = 2R_F^{\ell, \lambda_t}(\beta, y_t) - 1$$



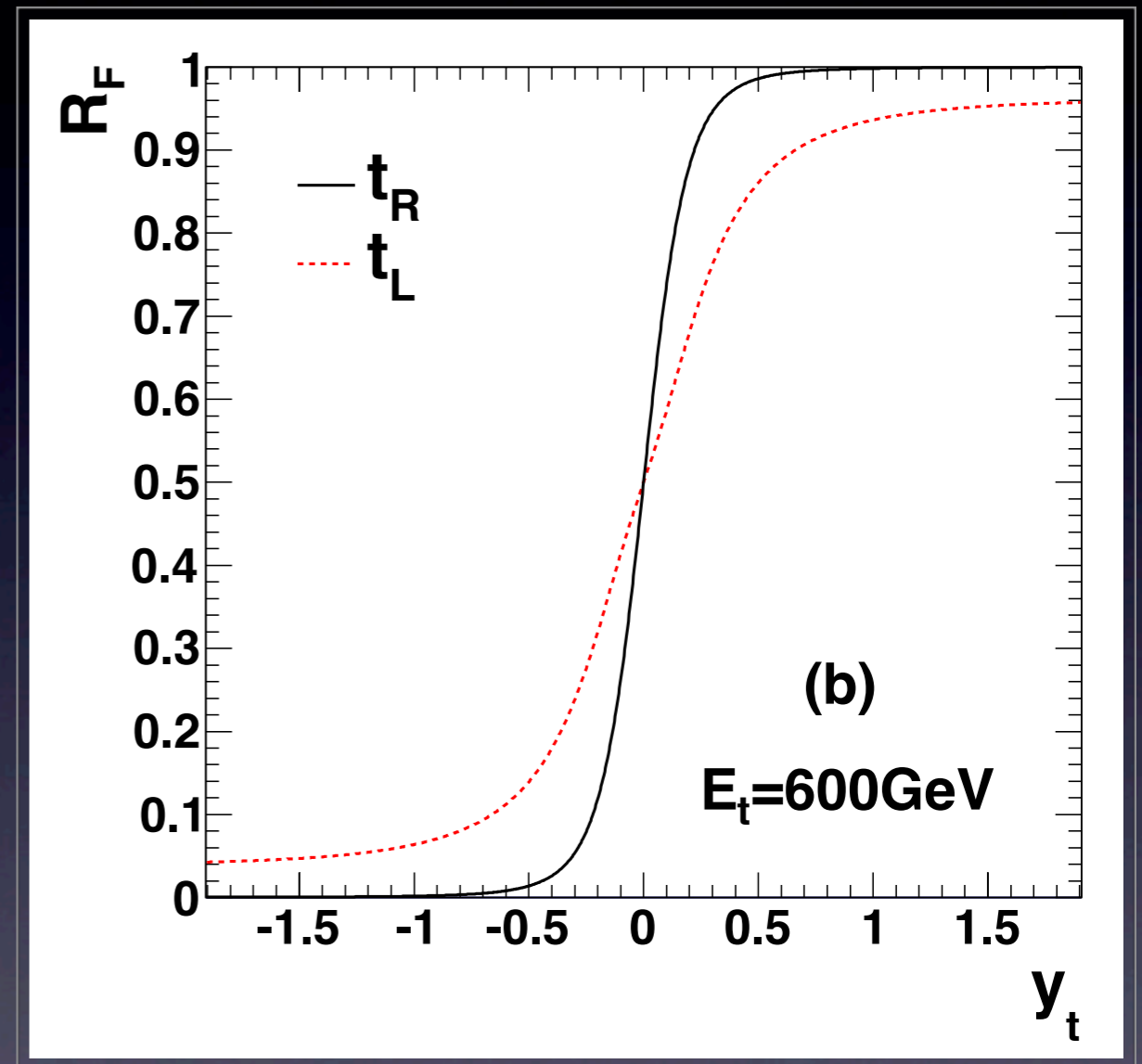
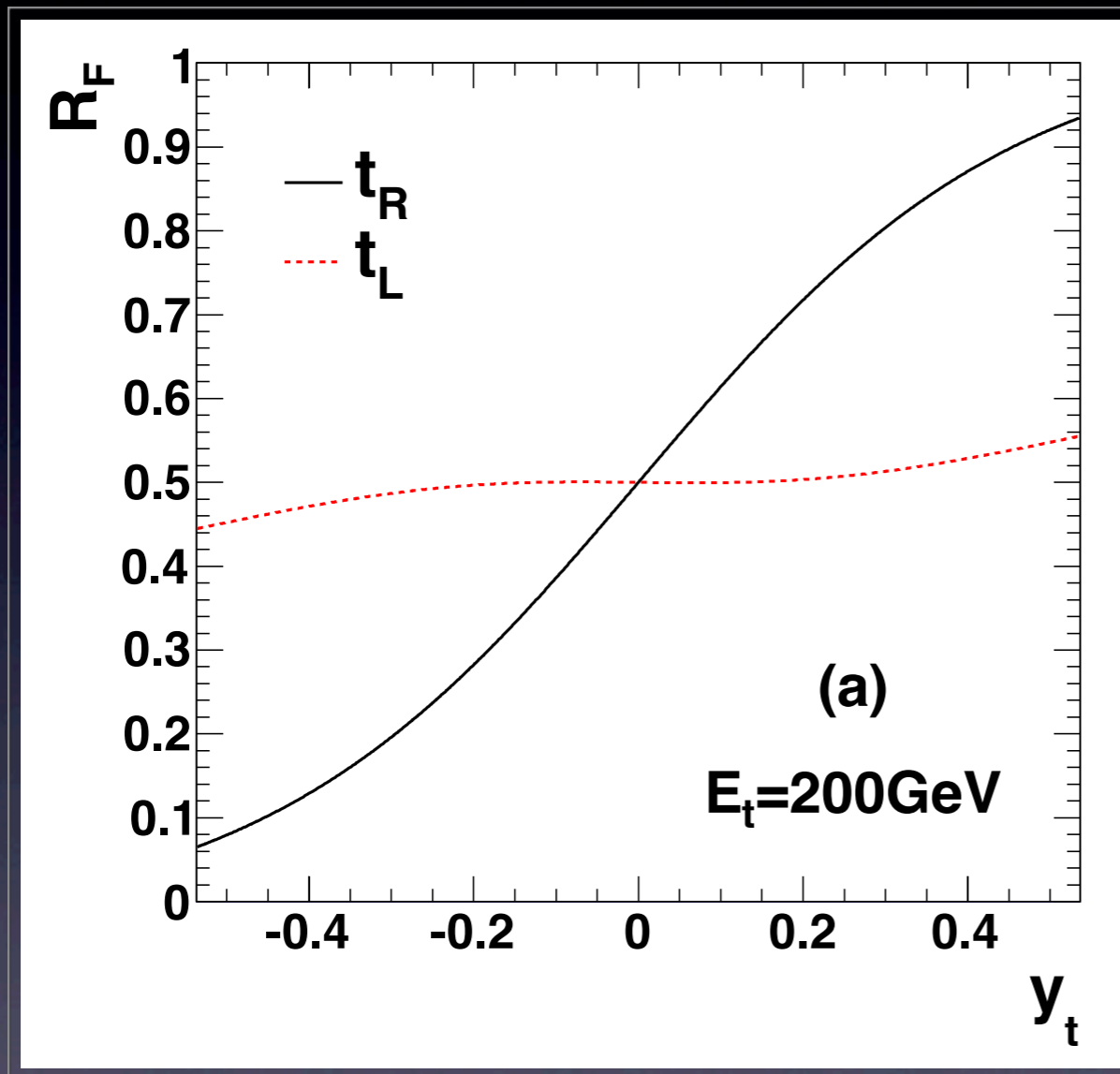
# It is easy to show ...

- Possibility of lepton in the forward region of detector for a top-quark ( $\beta, y_t, \lambda_t$ )

$$R_F^{\ell, \lambda_t}(\beta, y_t)$$

$$= \begin{cases} \frac{1}{2} + \frac{1}{2(1 + \gamma^{-2} \coth^2 y_t)^{1/2}} + \frac{\lambda_t \coth^2 y_t}{4\beta\gamma^2 (1 + \gamma^{-2} \coth^2 y_t)^{3/2}}, & (y_t > 0) \\ \frac{1}{2} - \frac{1}{2(1 + \gamma^{-2} \coth^2 y_t)^{1/2}} - \frac{\lambda_t \coth^2 y_t}{4\beta\gamma^2 (1 + \gamma^{-2} \coth^2 y_t)^{3/2}}, & (y_t < 0) \end{cases}$$

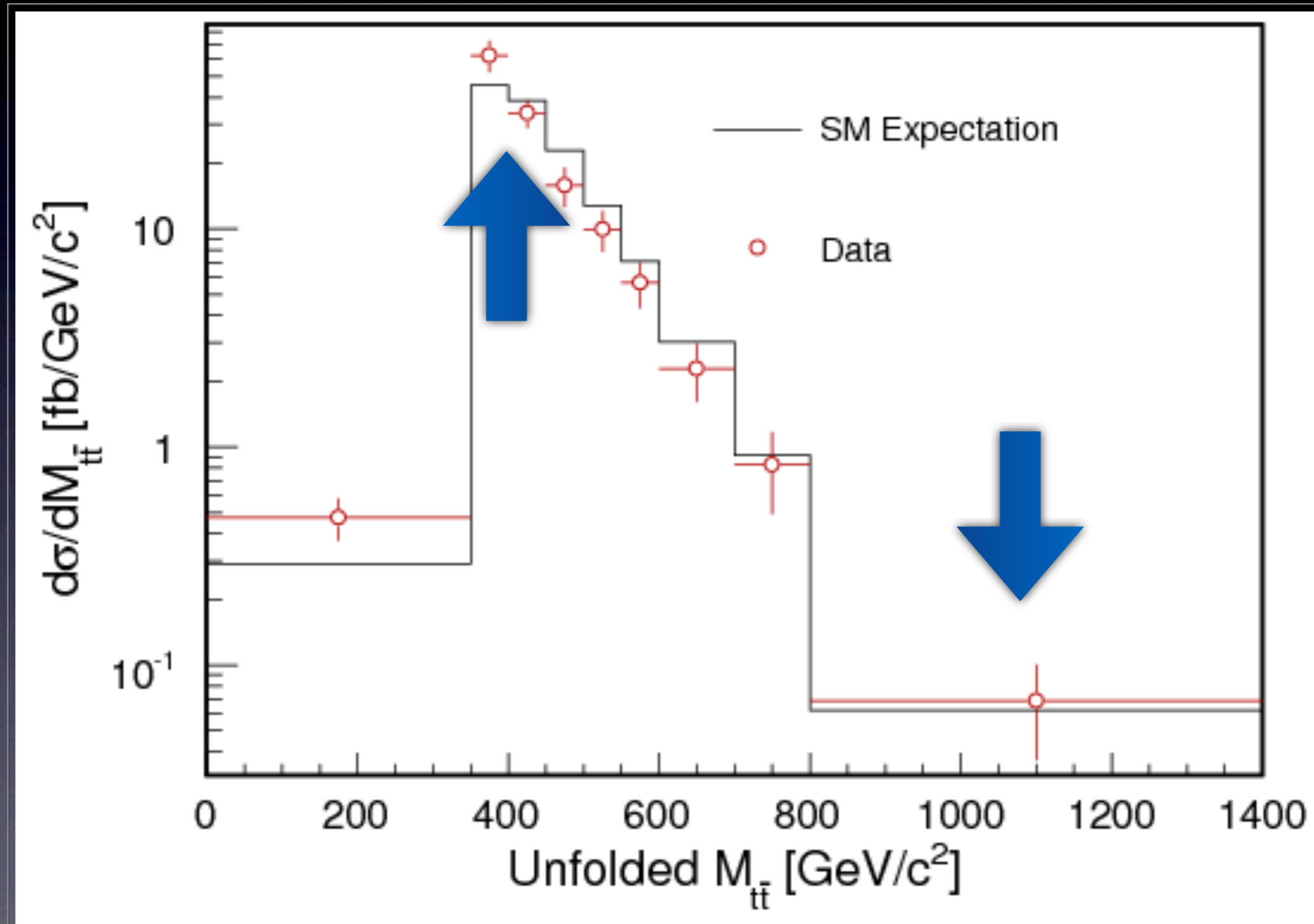
# $A_{FB}^{\ell}$ dependence on top kinematics



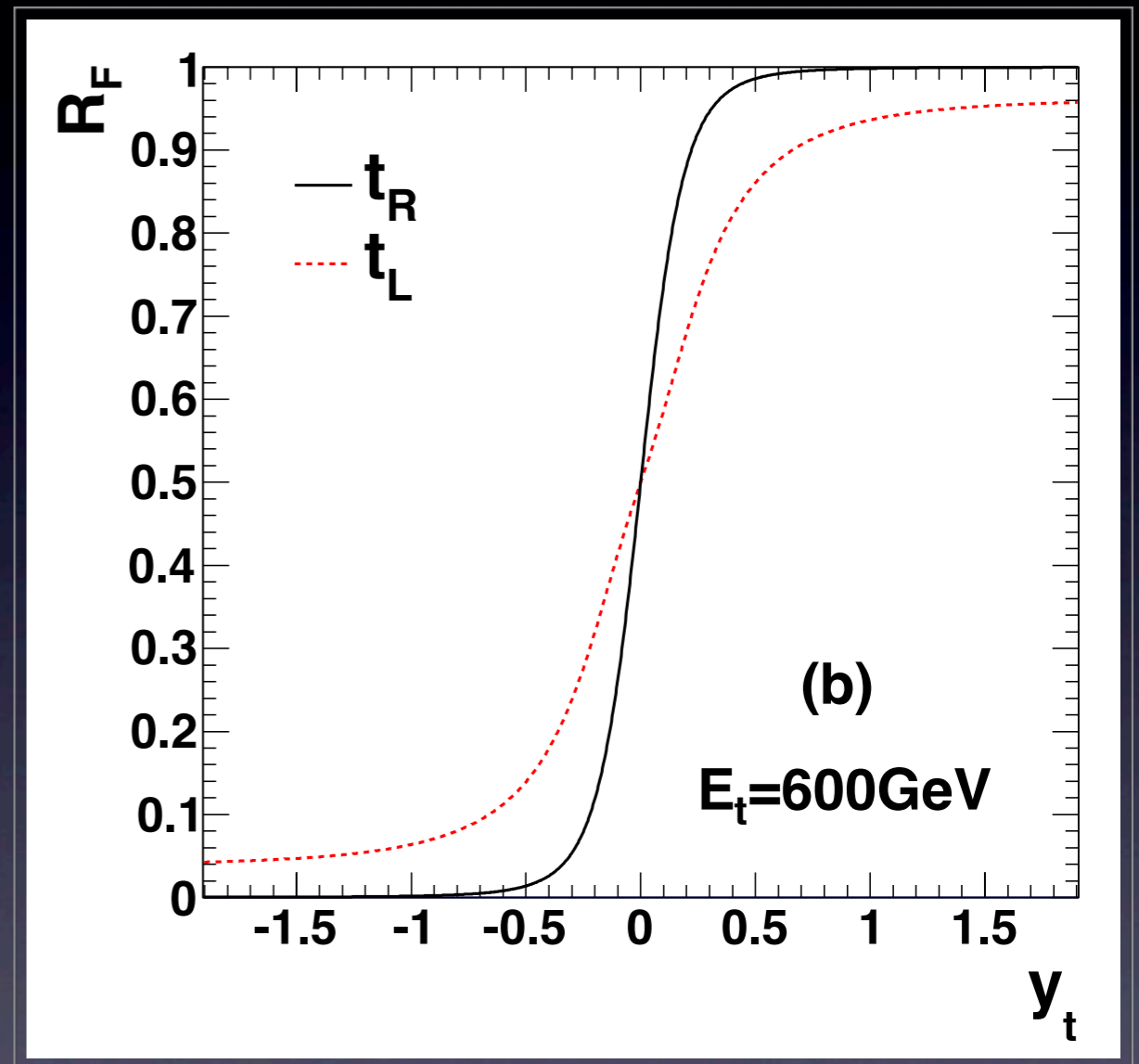
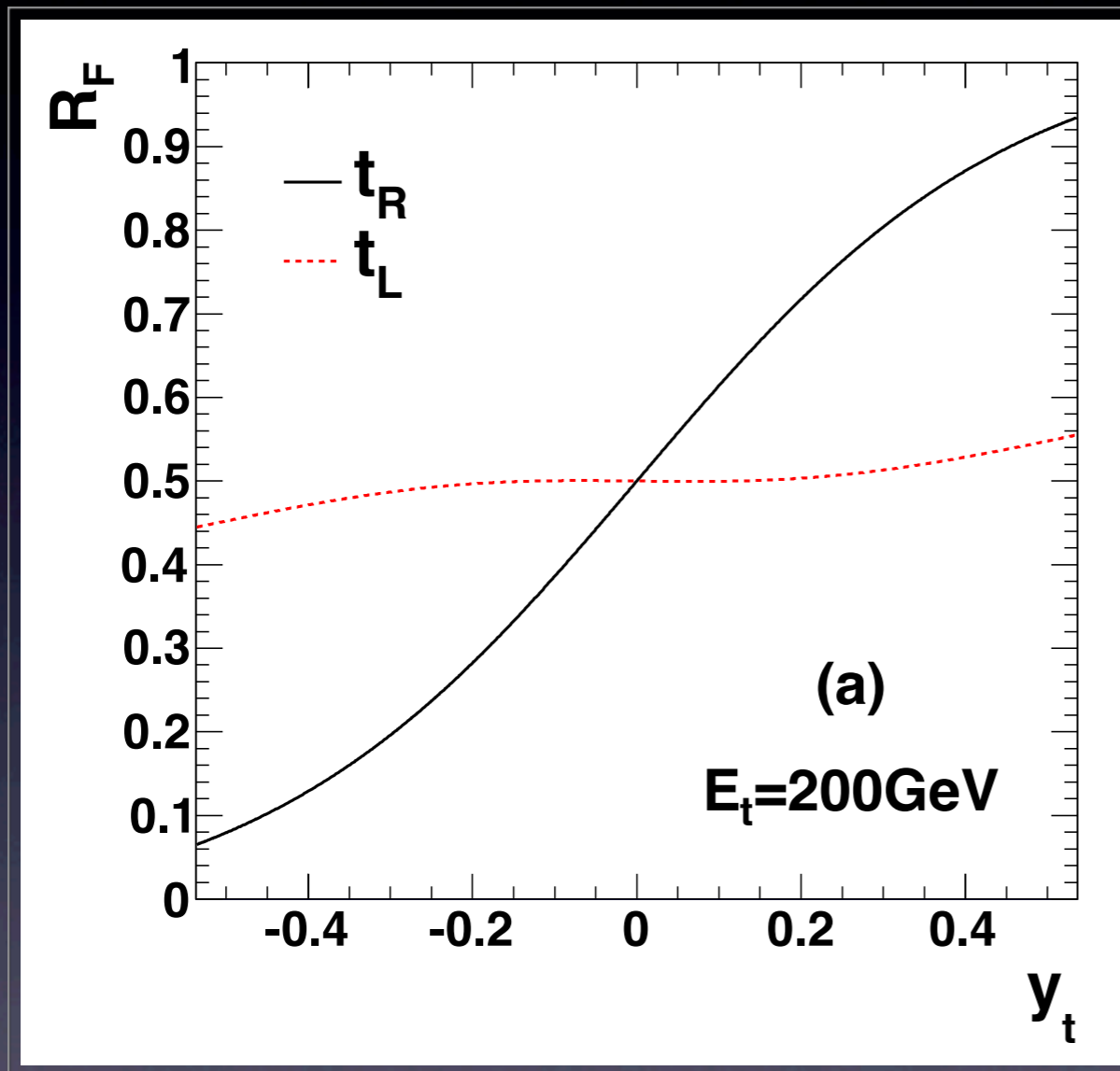
$$A_{FB}^{\ell, \lambda_t}(\beta, y_t) = 2R_F^{\ell, \lambda_t}(\beta, y_t) - 1$$

# Invariant mass spectrum of top quark pair

CDF, Phys.Rev.Lett. 102 (2009) 222003

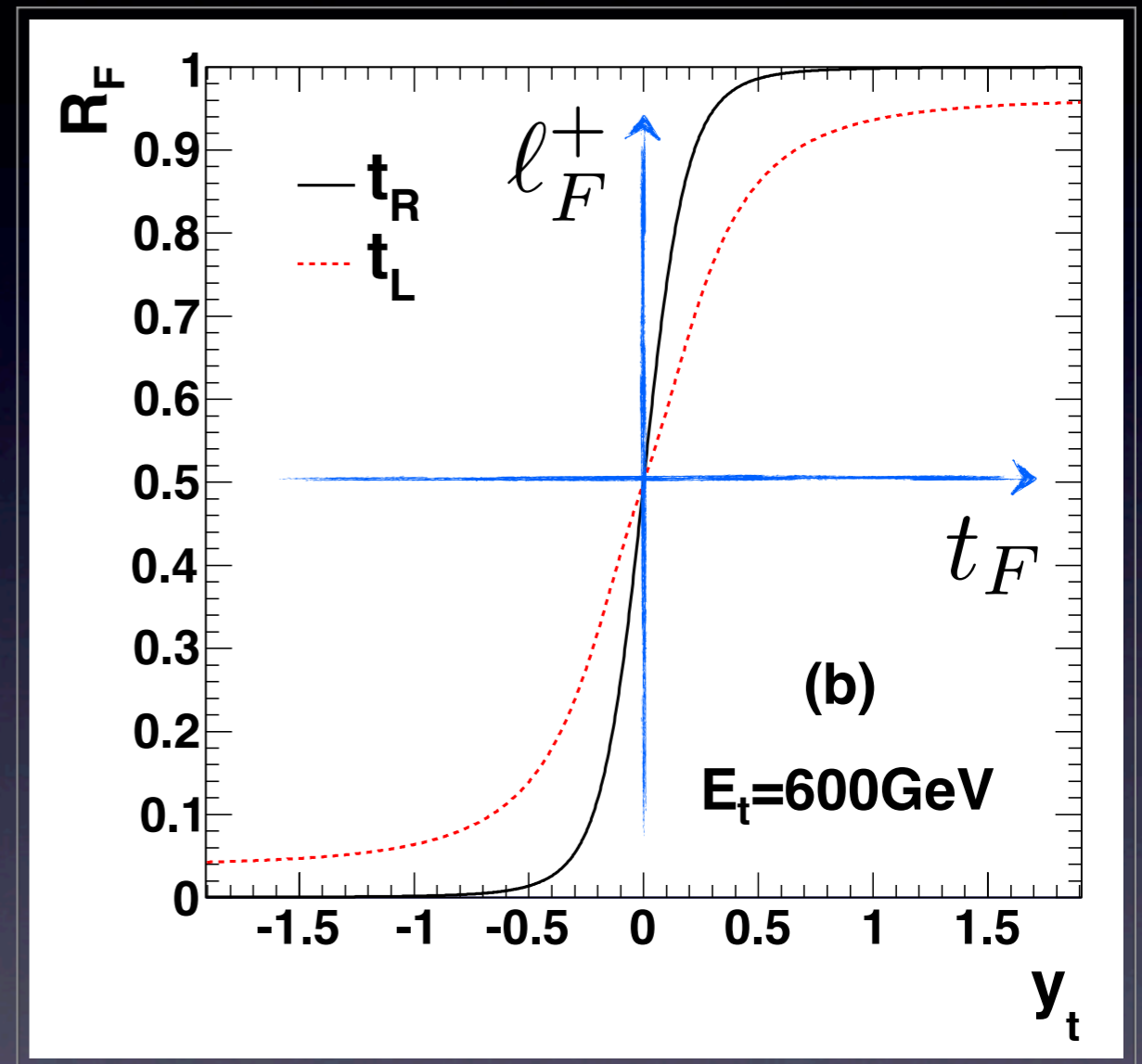
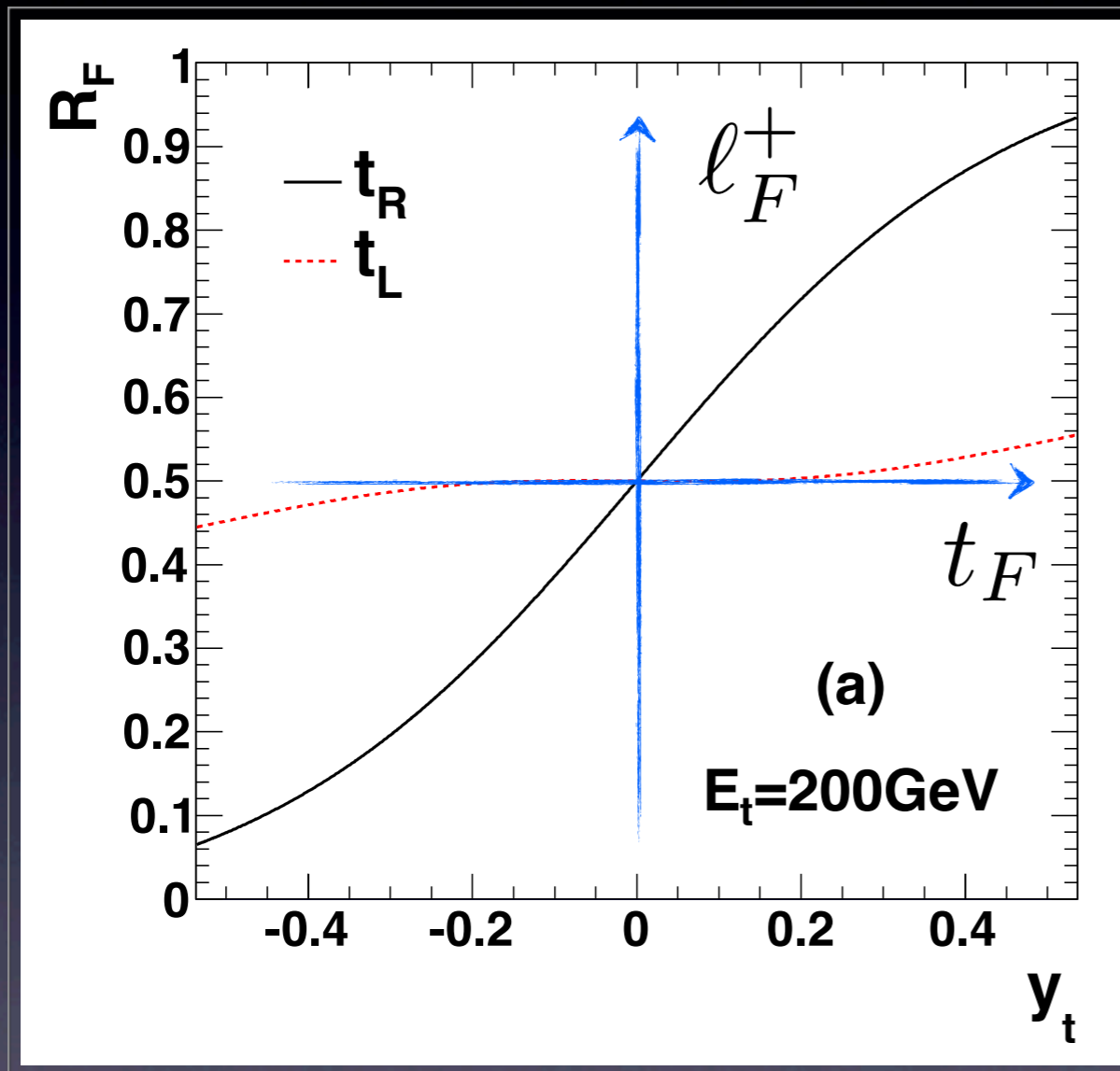


# $A_{FB}^{\ell}$ dependence on top kinematics



$$A_{FB}^{\ell, \lambda_t}(\beta, y_t) = 2R_F^{\ell, \lambda_t}(\beta, y_t) - 1$$

# $A_{FB}^{\ell}$ dependence on top kinematics



$$A_{FB}^{\ell, \lambda_t}(\beta, y_t) = 2R_F^{\ell, \lambda_t}(\beta, y_t) - 1$$

# $A_{FB}^t$ and $A_{FB}^\ell$ correlation

- When  $R_F \sim \text{constant}$  ( $\mathcal{R}_C^{t_L}, \mathcal{R}_C^{t_R}$ )

$$A_{FB}^\ell \approx \rho_{t_L} A_{FB}^{t_L} \times (2\mathcal{R}_C^{t_L} - 1) \\ + \rho_{t_R} A_{FB}^{t_R} \times (2\mathcal{R}_C^{t_R} - 1)$$

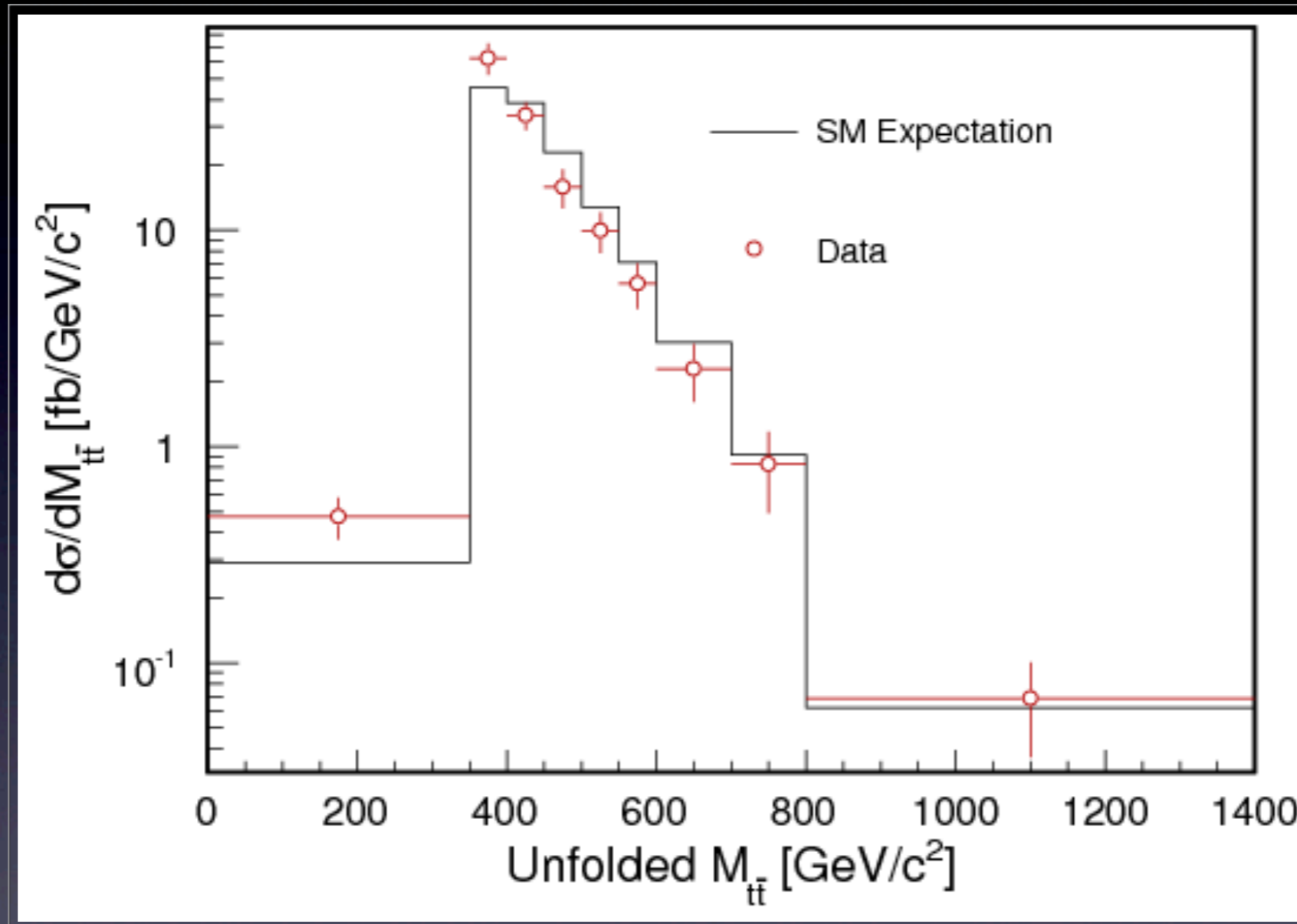
$$A_{FB}^t \approx [\rho_{t_L} A_{FB}^{t_L} + \rho_{t_R} A_{FB}^{t_R}]$$

$$\rho_{\lambda_t} = \frac{N^{\lambda_t}}{N_{\text{tot}}}$$

- The simple approximation helps in understanding the NP prediction obtained from a complete numerical calculation.

# Invariant mass spectrum of top quark pair

CDF, Phys.Rev.Lett. 102 (2009) 222003

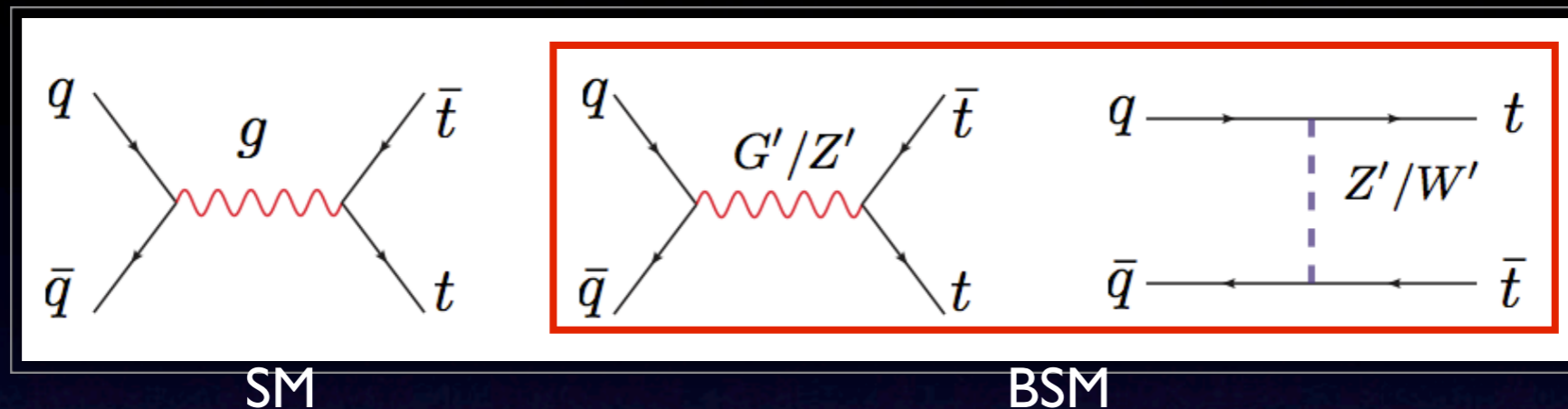


It provides upper bounds on NP resonance.  
The large bin (800GeV-1400GeV) is  
the most sensitive to a heavy resonance



# New physics models

NP models are divided into two classes



- **s-channel: extra octet vector gluon (axigluon is the best)**

Small couplings to the first two generations: dijet constraints at 7 TeV

Large couplings to third generation: to generate large  $A_{FB}$

Heavy resonances:  $t\bar{t}$  invariant mass spectrum

Very broad width: to interfere with the SM channel

- **t-channel: flavor changing interaction**

color singlet:  $Z'$ -u-t ( $\phi$ -u-t)

$W'^+$ -d-t ( $\phi^+$ -d-t)

color sextet or triplet

# Timeline of $A_{FB}^t$ and NP models

s-channel

EFT

Ferrario, Rodrigo  
Axigluon  
0809.3353

Frampton, Shu, Wang  
Axigluon  
0911.2955

QHC et al  
Effective coupling  
( $G', Z', W', H^0, H^+$ )  
1003.3461

Ferrario, Rodrigo  
chiral  $G'$   
0906.5541

Antunan, Kuhn, Rodrigo  
Axigluon  
0709.1652

Djouadi, Moreau, Richard, Singh  
KK Gluon  
0906.0604

Jung, Ko, Lee, Nam  
EFT  
0912.1105

2007, 2008

2009

2010, 2011

Jung, Murayama, Pierce, Wells  
FCNC Z-prime  
0907.4112

Shu, Tait, Wang  
Color Sextet/triplet scalar  
0911.3237

Xiao, Wang, Zhu,  
NLO QCD to Z-prime  
1006.2510

Cheung, Keung, Yuan  
FC W-prime  
0908.2589

Arhrib, Benbrik, Chen  
Color Sextet/triplet scalar  
0911.4875

Yan, Wang, Shao, Li  
NLO QCD to W-prime  
1110.6684

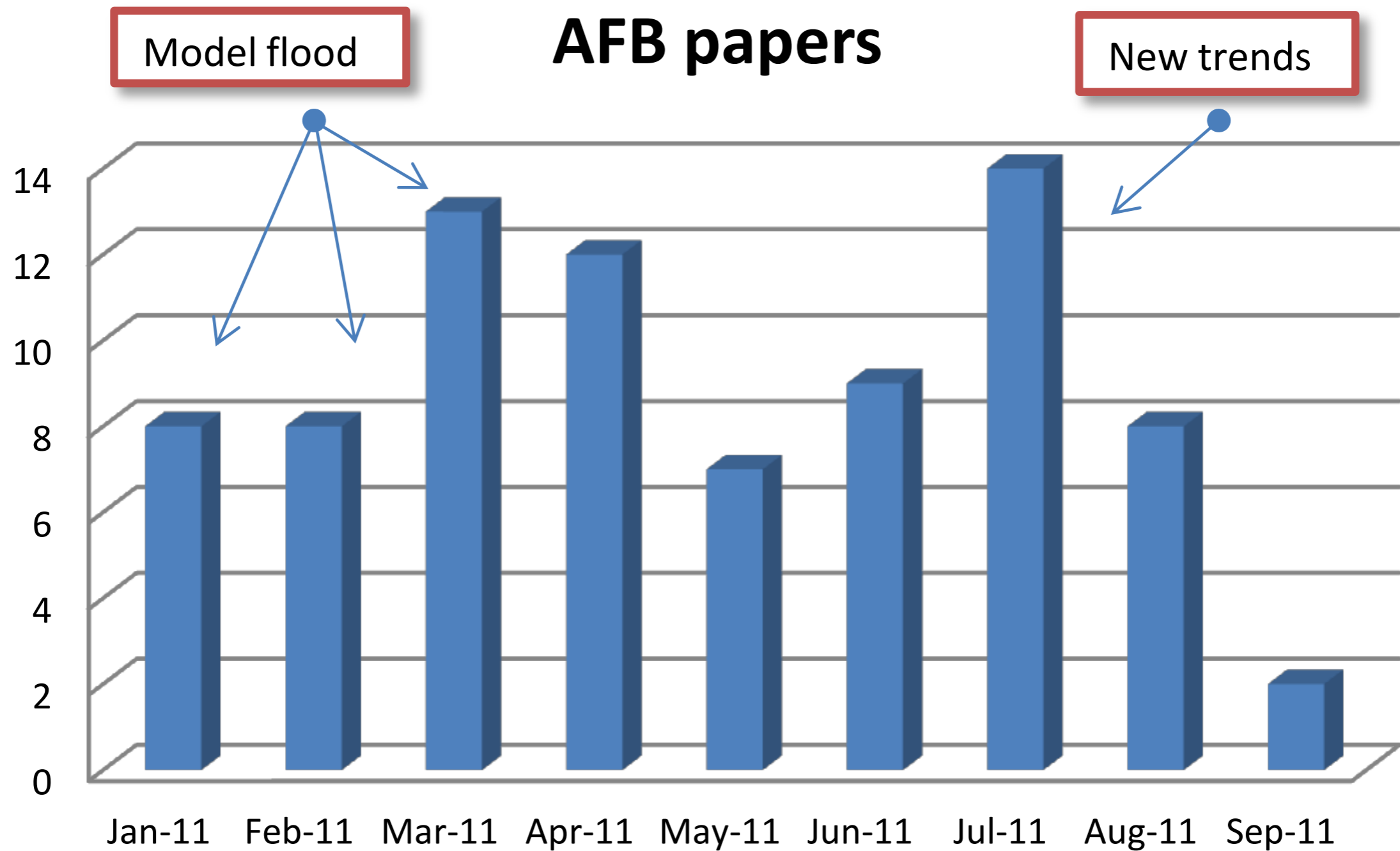
J. Cao, Heng, Wu, Yang  
 $\mathcal{R}$ -SUSY and TC2  
0912.1447

Shao, Li, et al  
NLO QCD to EFT  
1107.4012

t-channel

NLO QCD

# Timeline of $A_{FB}^t$ and NP models

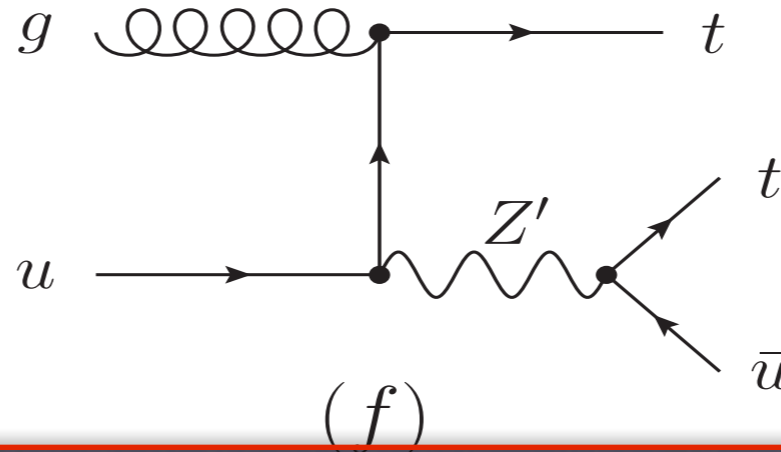
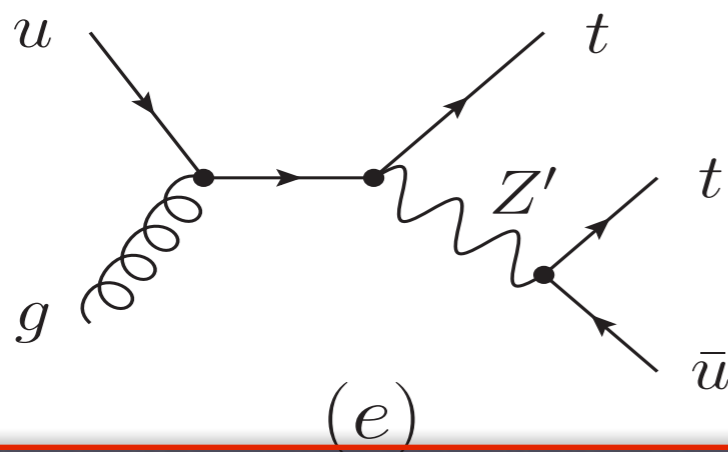
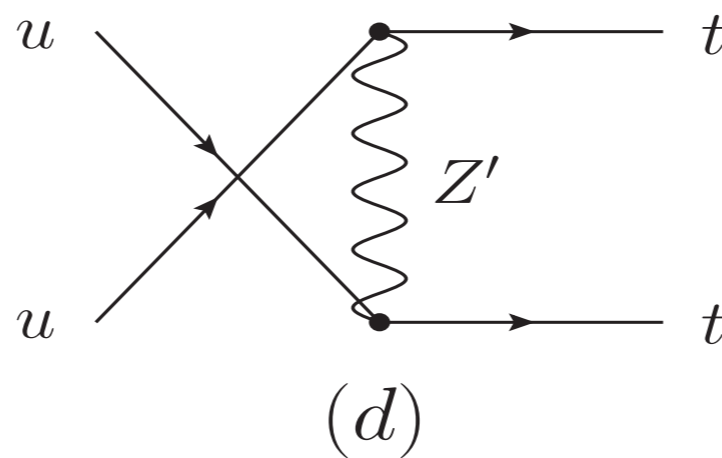
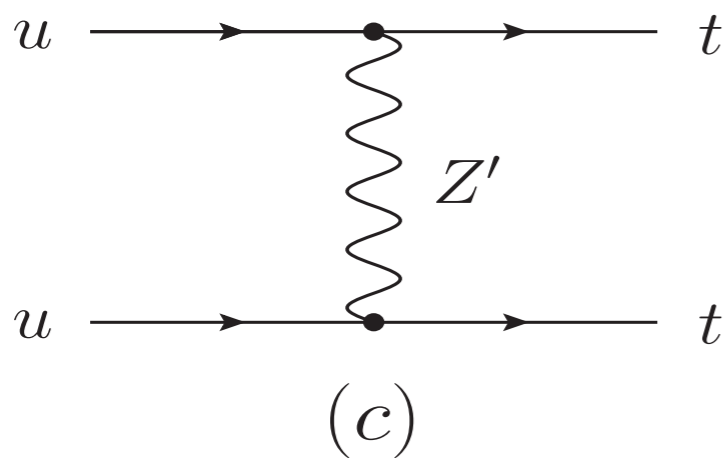
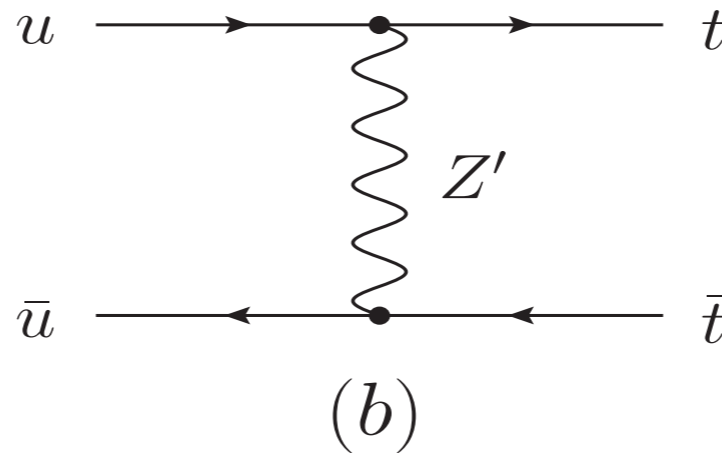
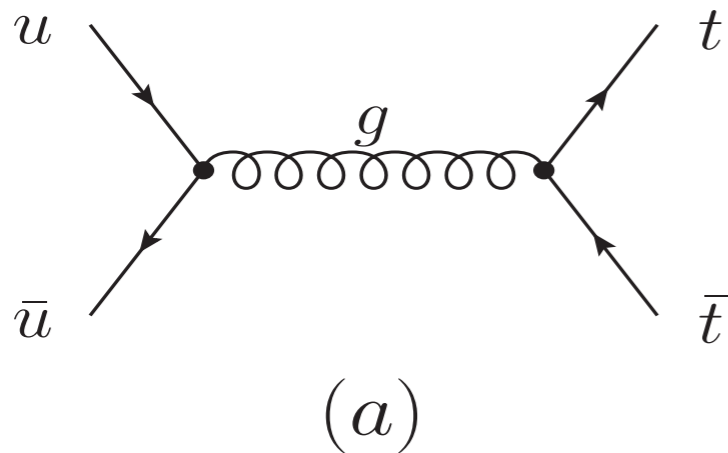


Adopted from J.A.Aguilar Saavedra's talk at TOP 2011, Sept. 2011

# FCNC Z-prime: $t$ -channel

- produce same-sign top-quark pair at the LHC

J. Cao et al  
hep-ph/0703308  
hep-ph/0409334



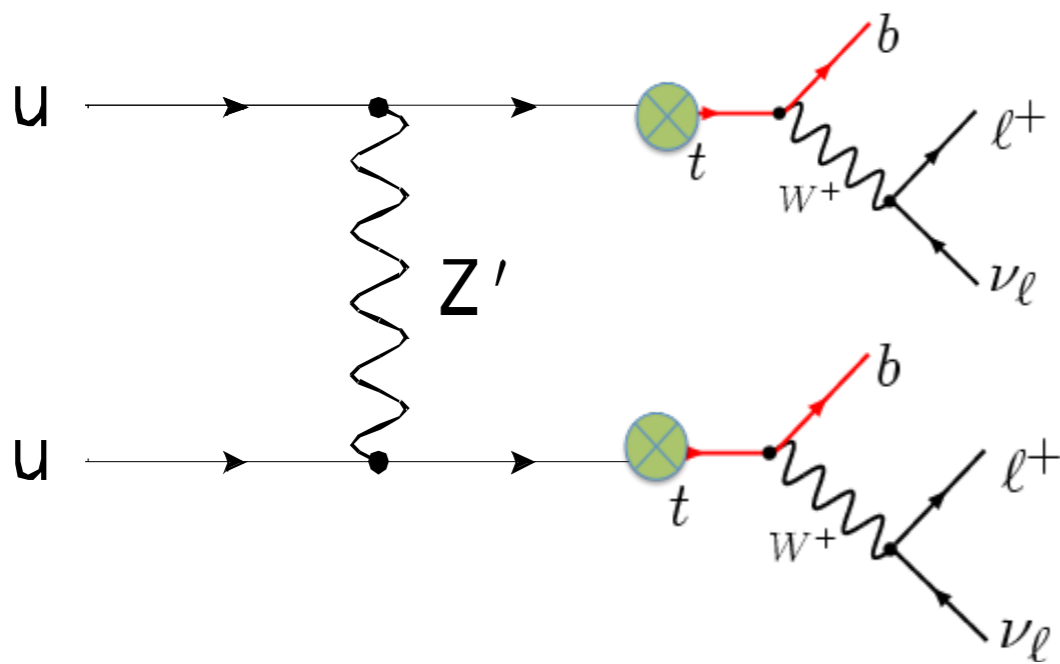
Same-sign  
top pair

$t\bar{t}$  + jet

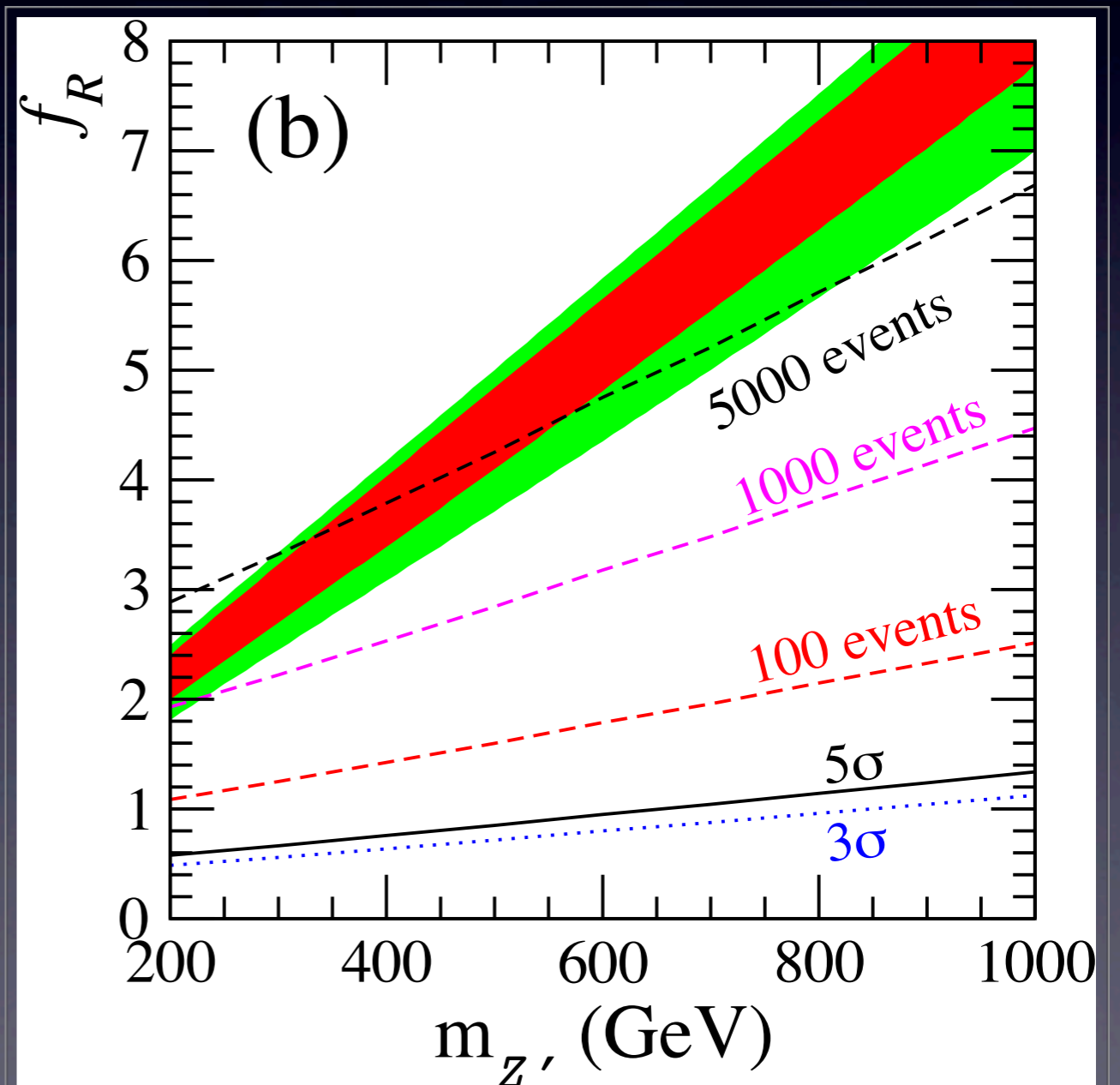
# FCNC Z-prime: $t$ -channel

- produce same-sign top-quark pair at the LHC

Ed Berger, QHC, Chuan-Ren Chen, Chong Sheng Li, Hao Zhang,  
Phys. Rev. Lett. 106 (2011) 201801, arxiv:1101.5625



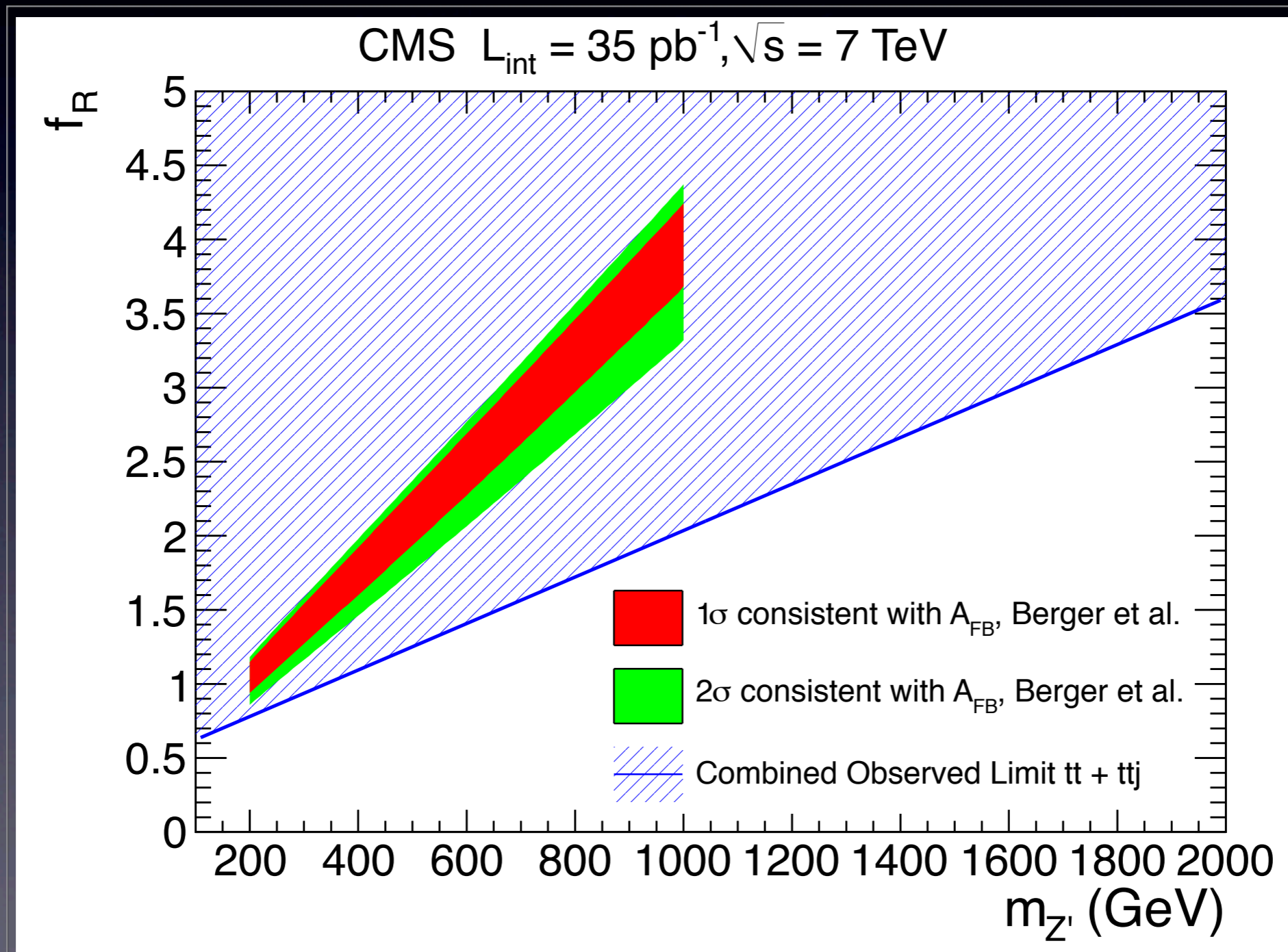
Same-sign dileptons  
are predicted.



# FCNC Z-prime: $t$ -channel

- Disfavored by CMS direct search of same-sign top pair

CMS, JHEP 1108 (2011) 005, arXiv:1106.2142



# Axigluon: s-channel

- Purely pseudo-vector coupling

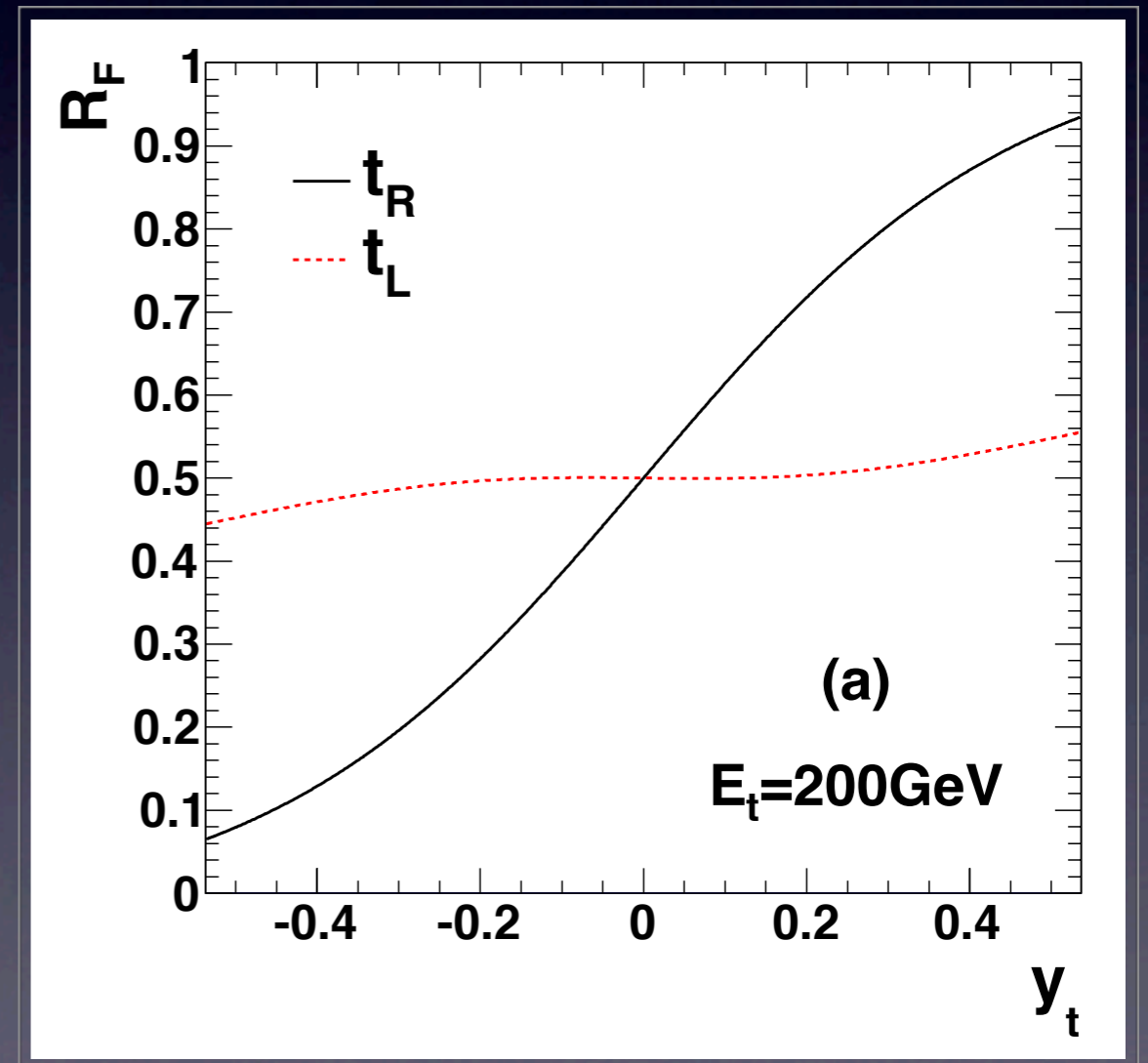
$$\mathcal{L} = g_s (g_l \bar{q} \gamma^\mu \gamma_5 q + g_h \bar{Q} \gamma^\mu \gamma_5 Q) G'_\mu$$

$$\rho_{t_L} = \rho_{t_R} = \frac{1}{2}$$

$$A_{FB}^{t_L} = A_{FB}^{t_R} = A_{FB}^t$$

$$A_{FB}^\ell \approx \rho_{t_L} A_{FB}^{t_L} \times (2\mathcal{R}_C^{t_L} - 1) \\ + \rho_{t_R} A_{FB}^{t_R} \times (2\mathcal{R}_C^{t_R} - 1)$$

$$A_{FB}^\ell \lesssim \frac{1}{2} A_{FB}^t$$



# Axigluon: s-channel

- Purely pseudo-vector coupling

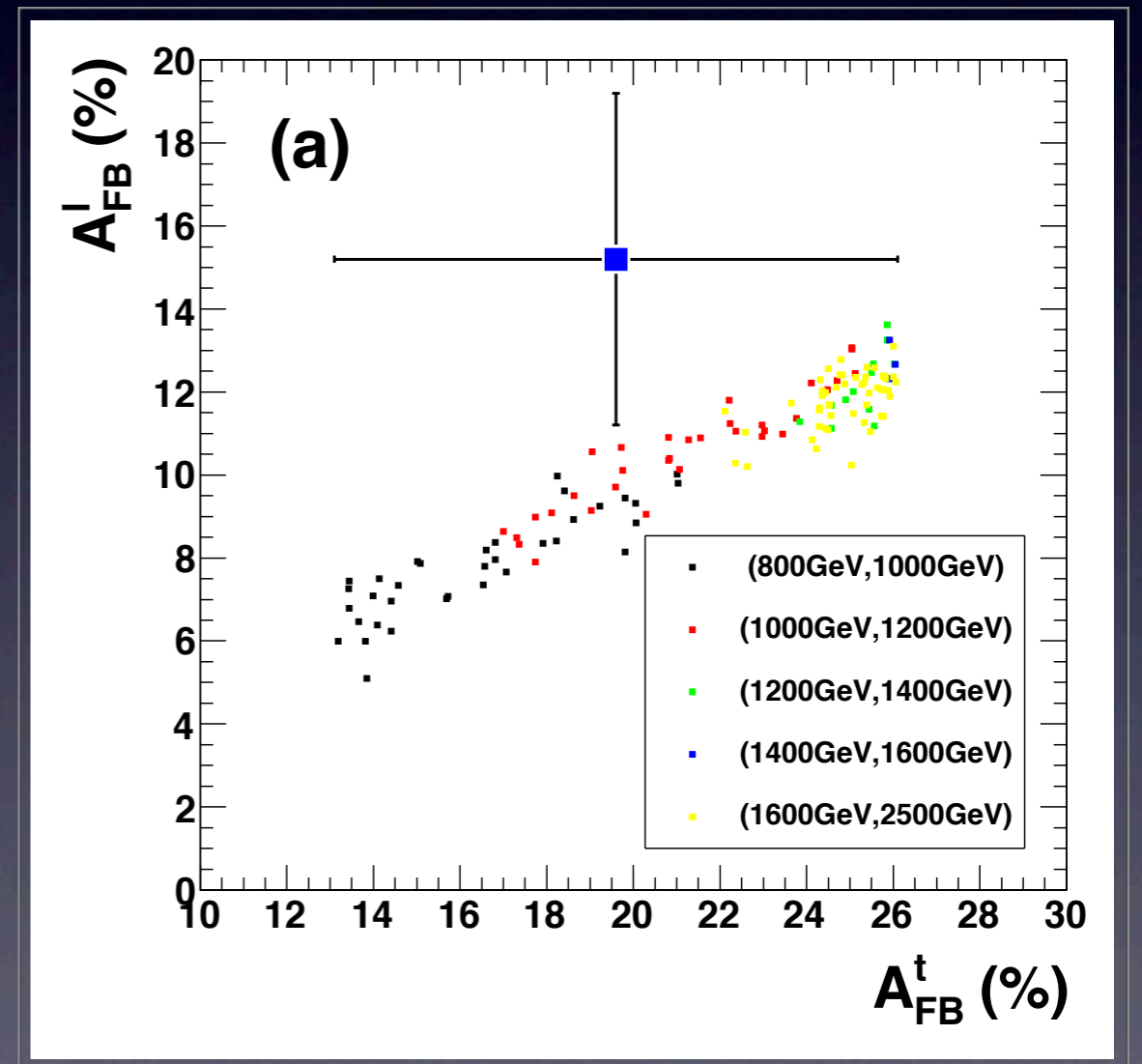
$$\mathcal{L} = g_s (g_l \bar{q} \gamma^\mu \gamma_5 q + g_h \bar{Q} \gamma^\mu \gamma_5 Q) G'_\mu$$

$$\rho_{t_L} = \rho_{t_R} = \frac{1}{2}$$

$$A_{FB}^{t_L} = A_{FB}^{t_R} = A_{FB}^t$$

$$A_{FB}^\ell \approx \rho_{t_L} A_{FB}^{t_L} \times (2\mathcal{R}_C^{t_L} - 1) + \rho_{t_R} A_{FB}^{t_R} \times (2\mathcal{R}_C^{t_R} - 1)$$

$$A_{FB}^\ell \lesssim \frac{1}{2} A_{FB}^t$$





# Axigluon: s-channel

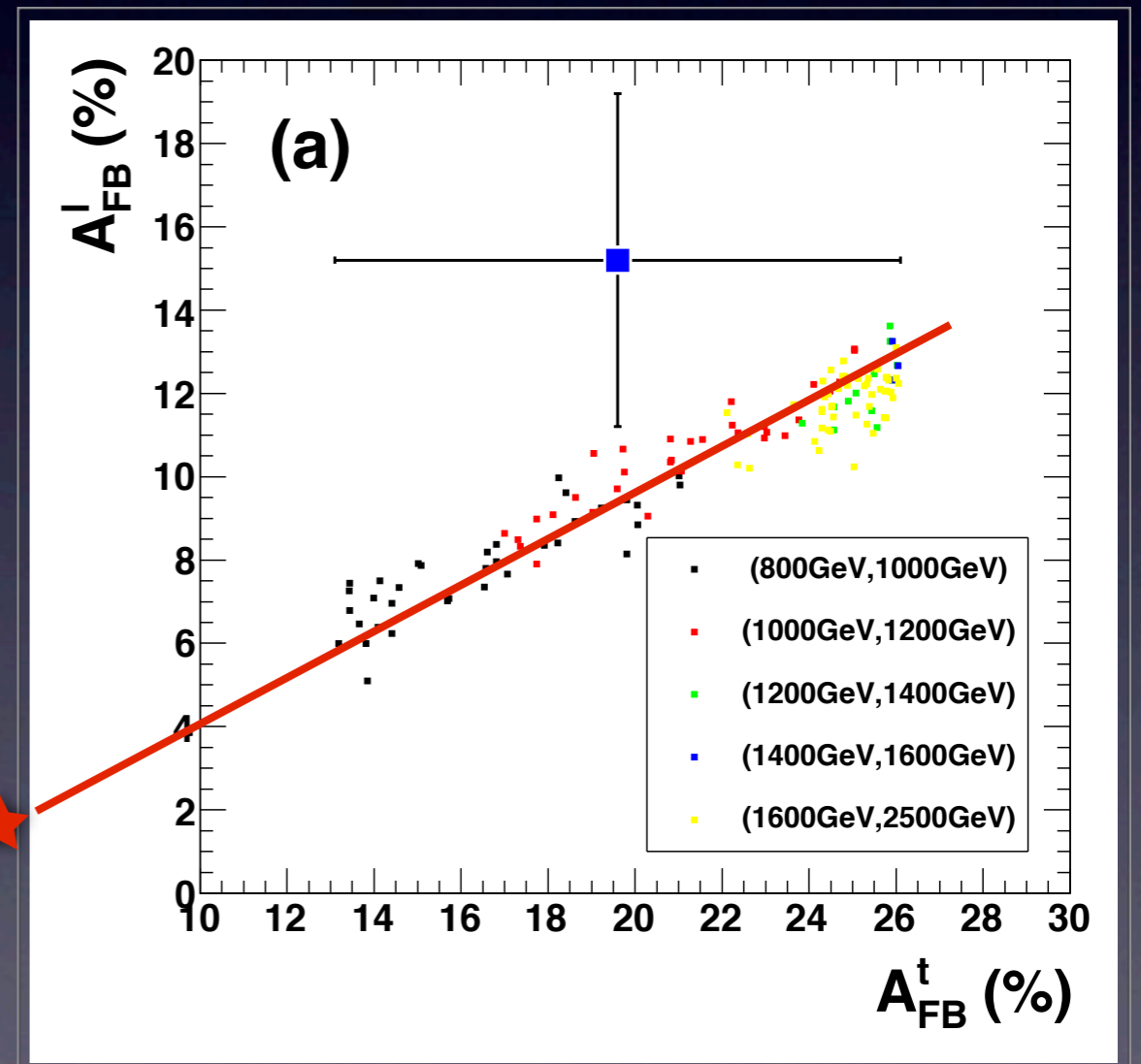
- Purely pseudo-vector coupling

$$\mathcal{L} = g_s (g_l \bar{q} \gamma^\mu \gamma_5 q + g_h \bar{Q} \gamma^\mu \gamma_5 Q) G'_\mu$$

- Best-fit

$$A_{FB}^l \simeq 0.47 \times A_{FB}^t + 0.25\%$$

SM ★



# FC $W$ -prime: $t$ -channel

- Purely right-handed flavor changing interaction

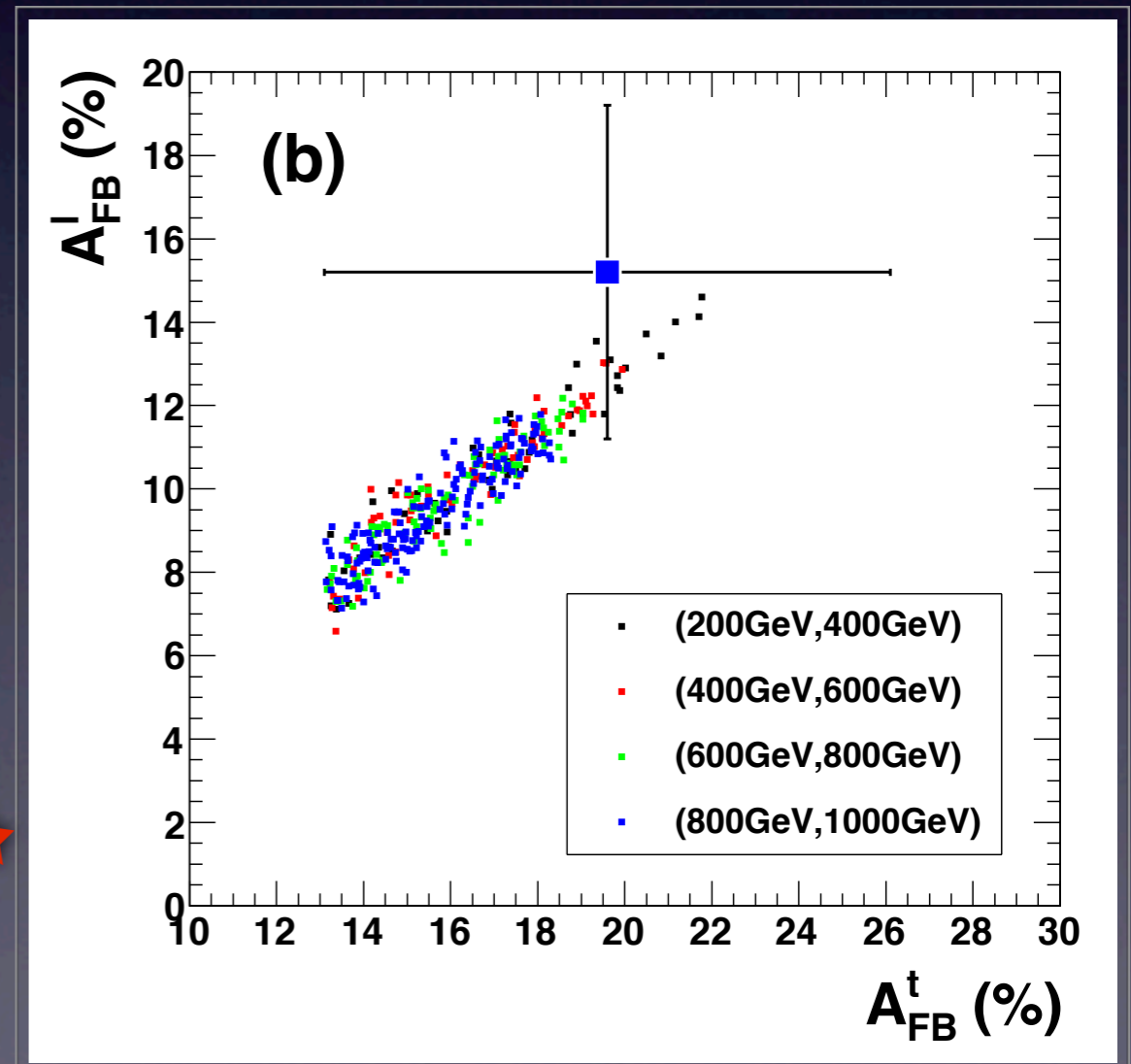
$$\mathcal{L} = g_2 g_R \bar{d} \gamma^\mu P_R t W'_\mu + h.c.$$

$$\rho_{t_R} > \rho_{t_L}$$

- Best-fit

$$A_{FB}^\ell \simeq 0.75 \times A_{FB}^t - 2.1\%$$

SM ★



# Conclusion

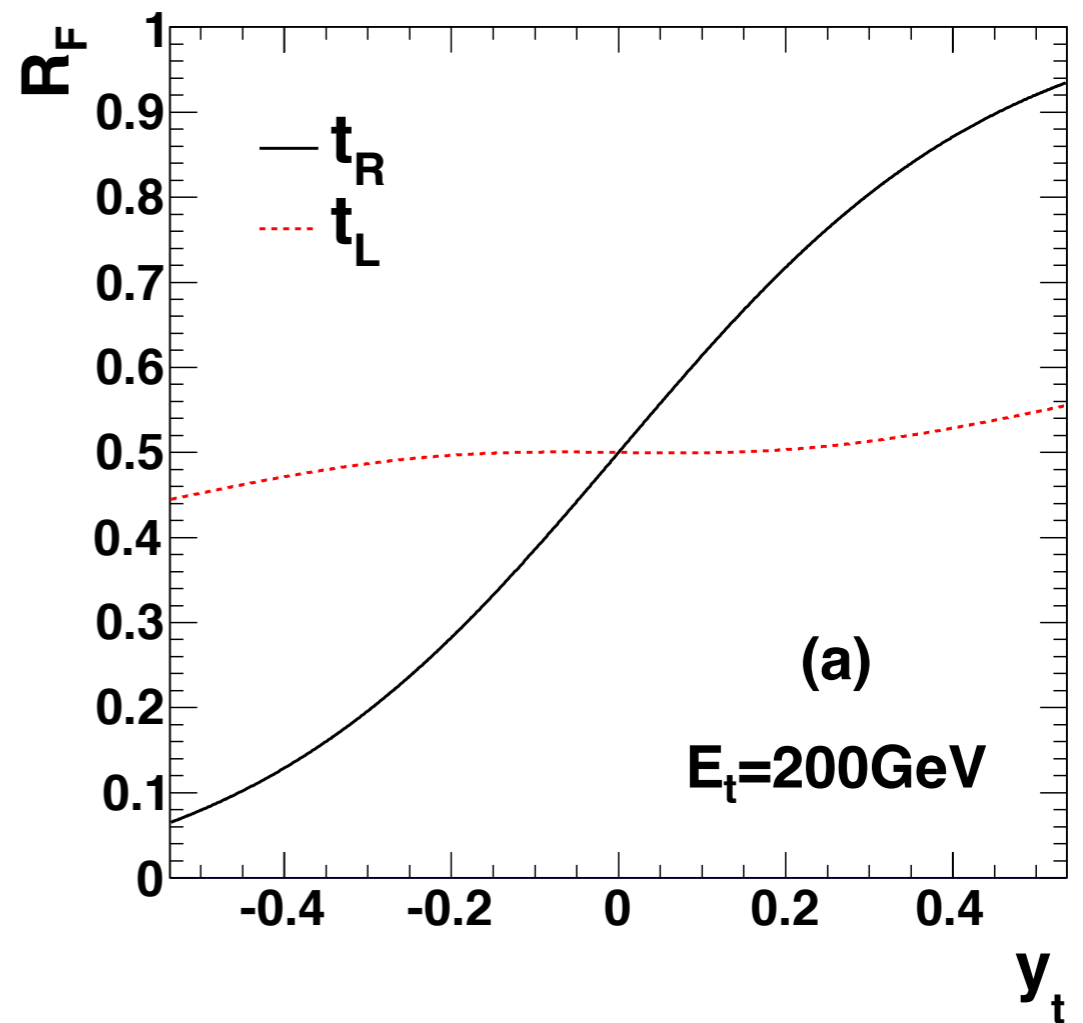
- $A_{FB}^t$  and  $A_{FB}^\ell$  is connected by the top-quark and charged lepton spin correlation.

$$A_{FB}^\ell \approx \rho_{t_L} A_{FB}^{t_L} \times (2\mathcal{R}_C^{t_L} - 1) + \rho_{t_R} A_{FB}^{t_R} \times (2\mathcal{R}_C^{t_R} - 1)$$

★  $\rho_{t_L} \ll \rho_{t_R}$   
 $A_{FB}^\ell \lesssim \frac{1}{2} A_{FB}^t$

★  $\rho_{t_L} = \rho_{t_R}$   
 $A_{FB}^\ell \lesssim \frac{1}{2} A_{FB}^t$

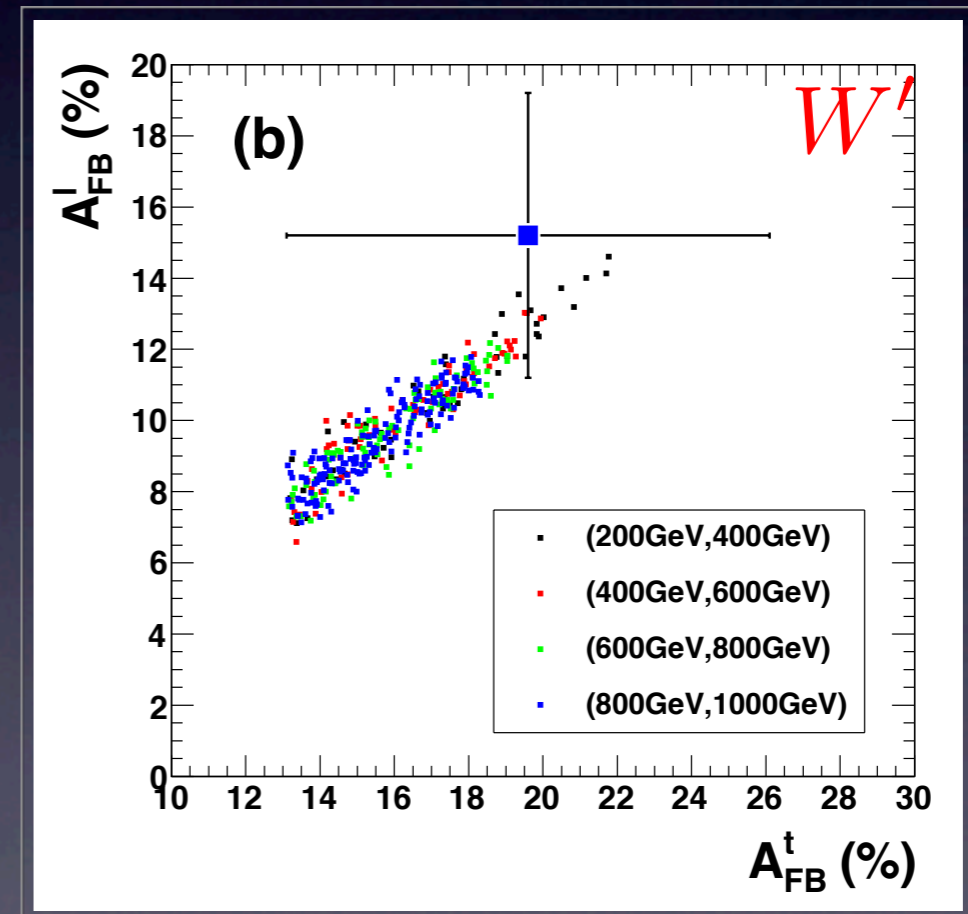
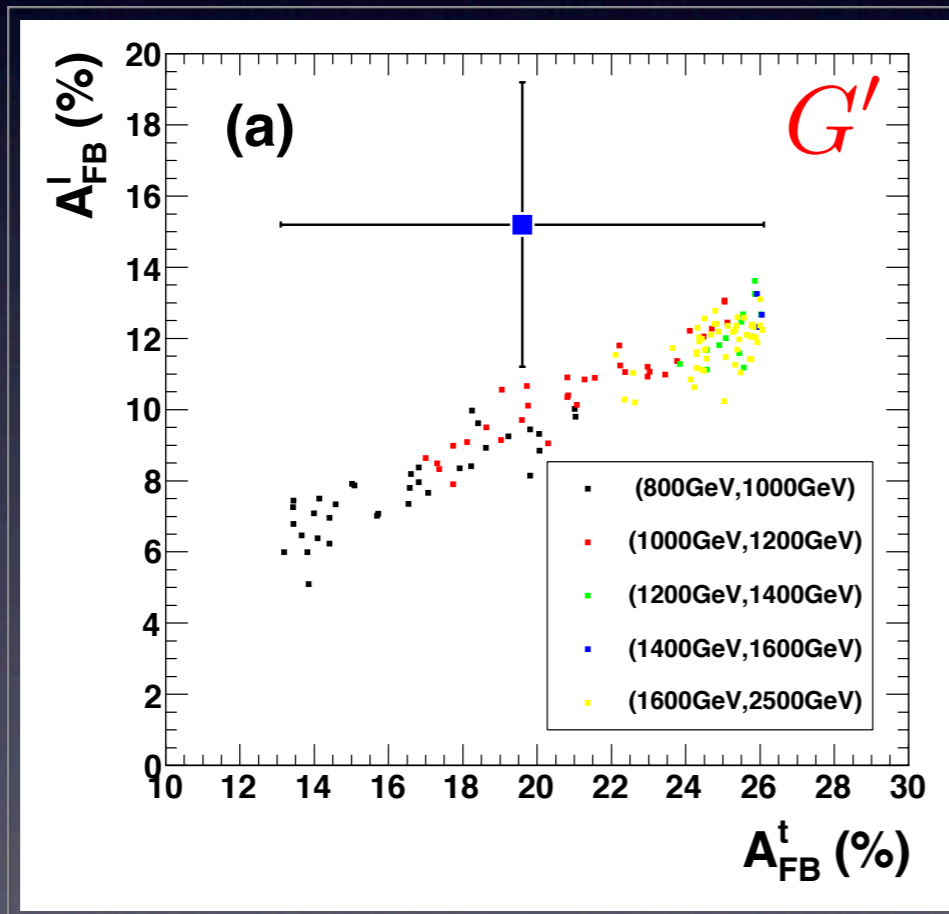
★  $\rho_{t_L} \gg \rho_{t_R}$   
 $A_{FB}^\ell \gtrsim \frac{1}{2} A_{FB}^t$



# Conclusion

- $A_{FB}^t$  and  $A_{FB}^\ell$  is connected by the top-quark and charged lepton spin correlation.

$$A_{FB}^\ell \approx \rho_{t_L} A_{FB}^{t_L} \times (2\mathcal{R}_C^{t_L} - 1) + \rho_{t_R} A_{FB}^{t_R} \times (2\mathcal{R}_C^{t_R} - 1)$$



$$A_{FB}^\ell \simeq 0.47 \times A_{FB}^t + 0.25\%$$

$$A_{FB}^\ell \simeq 0.75 \times A_{FB}^t - 2.1\%$$

Thank you !

# $A_{FB}^t$ versus $A_{FB}^\ell$

