A first test on spooky actions between free-traveling charged lepton pairs 首次测试自由带电轻子对间的量子纠缠

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子纠缠测量史中自由轻子的缺失

- As reviewed by C. N. Yang [4], the first experiment on quantum entanglement is the Wu-Shaknov Experiment published in 1950 [5] in which the angular correlation of two Compton-scattered **photons** arising from e^+e^- annihilation are measured
- The violation of Bell inequality was demonstrated in 1970s using entangled **photons** [6–8], confirming the non-locality of our universe
- Alain Aspect, John Clauser and Anton Zeilinger won the Nobel Prize in Physics in 2022 for demonstrating the potential to investigate and control particles (photons) that are in entangled states [9]



FIG. Angular correlation effects [10] demonstrated by the Wu-Shaknov Experiment



John Clauser used calcium atoms that could emit entangled photons after he had illuminated them with a special light. He set up a filter on either side to measure the photons' polarisation. After a series of measurements, he was able to show they violated a Bell incegulity.

FIG. Clauser's photon entanglement experiment [9]





The current absence of free-traveling leptons in QE measurements $\texttt{p}_{\texttt{L}}$ measurements $\texttt{p}_{\texttt{L}}$

- The ATLAS and CMS Collaborations recently observed quantum entanglement involving **top quarks** at a center-of-mass energy of 13 TeV, marking the highest energy measurements of quantum entanglement to date [12–15]
- Most studies on charged lepton QE have concentrated on the decaying tau leptons [16–22], while less attention has been given to electrons and muons
- Solid-state quantum computation was established in 2005 with electron pairs confined in semiconductor quantum dots [23]: entangled states were prepared, coherently manipulated, and measured
- No similar experiment has been done with free-traveling electrons as measuring the spin of a single traveling electron poses a significant challenge due to interference from its orbital motion [24]

Our proposal

Conduct a **first** measurement of the polarization correlation between charged lepton beams through joint measurements of their individual polarization-sensitive scatterings off two separate targets.

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可控纠缠轻子对源的建立

Theory: Concurrence, CHSH inequality, and the kinematic approach 理论: 纠缠度、CHSH 不等式与运动学方法

• Entanglement can be quantified by concurrence [25-27], defined as

$$\mathcal{C}(\rho_f) = \max\left\{0, \lambda_1 - \lambda_2 - \lambda_3 - \lambda_4\right\} \in [0, 1]$$
(1)

for a two-qubit system, where λ_i $(\lambda_i \geq \lambda_j, \ \forall i < j)$ are the square roots of the eigenvalues of the matrix $\rho_f(\sigma_2 \otimes \sigma_2)\rho_f^*(\sigma_2 \otimes \sigma_2)$. If $\mathcal{C} > 0$, the two-qubit system is entangled.

• The CHSH inequality, $I_2 \le 2$ [28], is the Bell inequality for a two-qubit system. The optimal (maximal) I_2 [29] evaluates to

$$I_2 = 2\sqrt{\lambda_1 + \lambda_2},\tag{2}$$

where λ_1 and λ_2 are the two largest eigenvalues of the matrix $C^{\rm T}C$, and C is the correlation matrix calculated by $C_{ij} = {\rm Tr}\left(\rho_f\left(\sigma_i\otimes\sigma_j\right)\right)$. $I_2=2\sqrt{2}$ is the upper limit of the quantum mechanics.

• In addition to the *decay approach* used for decaying particles, the *kinematic approach* [30, 31] can reconstruct quantum states from production kinematics, applicable to stable particles produced in simple QED scatterings.

可控纠缠轻子对源的建立

Electron-muon entanglement sources via muon on-target experiments 缪子打靶实现可控电子-缪子纠缠源!



Deam'		001017	o j/max	μ , max'	e, max'	μ ,	e,mm,	L, .	$\underline{\mathbf{n}}, \underline{\mathbf{n}} \geq 0.0 \mathrm{maa}$
	1	0.111	0.22	0.9	10.2	0.92	0.08	0.56	0.56
	10	0.146	0.044	2.8	3.3	5.2	4.5	0.39	0.39
	160	0.418	0.0014	4.6	0.5	10	145	0.027	0.022

可控纠缠轻子对源的建立

Electron-positron entanglement sources via positron on-target experiments 正电子打靶实现可控电子-正电子纠缠源!



- The angular ranges exhibiting $\mathcal{C}(\rho_f)>0$ in the center-of-mass frame are significantly broader
- The theoretical upper limits for both $\mathcal{C}(\rho_f)$ and I_2 in quantum mechanics are nearly reached as θ'_{e^+} approaches 3
- Assuming a 1 GeV positron beam with a flux of $10^{12}/s$ directed at a 10 cm thick Al target, the expected entangled event rate is $1.9 \times 10^9/s$
- A golden region for measurements:
 - $\bar{E}_{\rm beam}=\mathbf{1}~\mathbf{GeV},\,0.05~\mathrm{rad}\leq\theta_{e^+}\leq0.1~\mathrm{rad}$
 - 23.4% of all events with $\mathcal{C}(\rho_f) > 0$
 - $E \ge 0.094$ GeV, $\theta \ge 0.0103$ rad
 - $\mathcal{C}(\rho_{\,f})$ reaching up to $\mathbf{0.953}$ and I_2 up to $\mathbf{2.8281}$

$E_{ m beam}/{ m GeV}$	$E_{ m COM}/{ m GeV}$	$\mathcal{C}^{\max}(\boldsymbol{\rho}_f)$	I_2^{\max}	$E_{e^+}^{\min}/{ m GeV}$	$E_{e^-}^{\rm min}/{ m GeV}$	$ heta_{e^+}^{ m min}/{ m rad}$	$ heta_{e^-}^{ m min}/{ m rad}$	$\sigma_{ m E}/{ m \mu b}$
1	0.032	0.9996	2.8281	0.008	0.389	0.0255	0.0028	243.6
3	0.055	0.9997	2.8282	0.023	1.166	0.0147	0.0016	82.1
10	0.101	0.9997	2.8282	0.074	3.890	0.0081	0.0009	26.5



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时自由轻子纠缠对间相关性的首次测量

A first electron-positron beam correlation measurement proposal 电子-正电子束相关性测量的首个提案



FIG. Proposed cascade experiment for measuring polarization correlations of the primary products

Simulation setup:

- $0.05 \text{ rad} \le \theta_3 \le 0.1 \text{ rad}$ in a 1 GeV positron on-target experiment
- The spins of target electrons 5 and 6 are aligned with the beam direction
- Consider the main component of the primary state, $(LL+RR)/\sqrt{2}$



FIG. Joint angular distribution densities of the two secondary scattering processes

Assuming the two secondary targets are $10~{\rm cm}$ thick iron, the event rate in $\cos\theta_7' \leq 0.5~\wedge$ $-0.75 \leq \theta_9' \leq 0.75$ is ${\bf 1.4}\times {\bf 10^2/s}$ for the state $(LL+RR)/\sqrt{2}.$

Future prospects: Scattering-based simplified state tomography 展望: 基于散射的简化的量子态解析

Take $0.05 \text{ rad} \le \theta_3 \le 0.1 \text{ rad}$ in a 1 GeV positron on-target experiment as an example:

- The state of the primary products is approximately 1% $(RL+LR)/\sqrt{2}$, 1% $(RL-LR)/\sqrt{2}$, 7% $(RR-LL)/\sqrt{2}$, and 90% $(RR+LL)/\sqrt{2}$ in the lab frame
- The optimized ratio of the yields of $(LL+RR)/\sqrt{2}$ to UU is $1.29\pm0.03({\rm MC})$, corresponding to 4.4×10^3 post-optimization efficient signal event counts and an expected signal yield over a **27-second** run; the result for $(LR+RL)/\sqrt{2}$ is $0.78\pm0.02({\rm MC})$ in comparison
- Other uncertainties, such as those from process modeling and background suppression, may dominate the real experimental analysis
- For the 20% polarized targets, the ratios are 1.010 ± 0.009 and 0.986 ± 0.009 generated from 25 times the number of Monte Carlo events, corresponding to 2.5×10^4 efficient event counts accumulated in **680 seconds**
- The high event rate can help mitigate the decline in resolving power associated with low target polarization purities in real-world applications
- A simplified state tomography can be performed assuming prior knowledge from the primary scattering



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Summary

- GeV-scale muon and positron on-target experiments are examined as **controllable entangled lepton pair sources** through the kinematic approach
- Quantum entanglement and the CHSH inequality violation are present in the primary scattering products
- A first measurement of the correlation between entangled free-traveling lepton pairs is proposed to verify the entanglement
- The electron-positron beam polarization correlation measurement can be conducted with a high event rate at many domestic positron beam facilities

Process	Incident flux	Primary event rate	Secondary coincidence rate
$\mu^-e^- \to \mu^-e^-$	$10^5/s$	$2.6 imes 10^4 / d$	(not estimated)
$e^+e^- \to e^+e^-$	$10^{5}/{\rm s}$	$1.9 \times 10^{2} / s$	$4.4 \times 10^{2}/y$
$e^+e^- \to e^+e^-$	$10^{12}/{ m s}^{*}$	$1.9 imes10^9/{ m s}$	$1.4 imes 10^2/{ m s}$

*Possibly from the beam dump of the STCF.

Thanks for your attention!

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