# 粒子物理

## 20. 弱相互作用和V-A理论



#### **Parity**

**★** The parity operator performs spatial inversion through the origin:

$$\begin{split} \psi'(\vec{x},t) &= \hat{P}\psi(\vec{x},t) = \psi(-\vec{x},t) \\ \text{applying } \hat{P} \text{ twice: } \hat{P}\hat{P}\psi(\vec{x},t) = \hat{P}\psi(-\vec{x},t) = \psi(\vec{x},t) \\ \text{so} \qquad \hat{P}\hat{P} = I \quad \longrightarrow \quad \hat{P}^{-1} = \hat{P} \end{split}$$

To preserve the normalisation of the wave-function

$$\begin{split} \langle \psi | \psi \rangle &= \langle \psi' | \psi' \rangle = \langle \psi | \hat{P}^{\dagger} \hat{P} | \psi \rangle \\ \hat{P}^{\dagger} \hat{P} &= I & \rightarrow \hat{P} \text{ Unitary} \\ \bullet \text{ But since } \hat{P} \hat{P} &= I & \hat{P} &= \hat{P}^{\dagger} & \rightarrow \hat{P} \text{ Hermitian} \end{split}$$

which implies Parity is an observable quantity. If the interaction Hamiltonian commutes with  $\hat{P}$ , parity is an observable conserved quantity

• If 
$$\psi(\vec{x},t)$$
 is an eigenfunction of the parity operator with eigenvalue  $P$   
 $\hat{P}\psi(\vec{x},t) = P\psi(\vec{x},t) \implies \hat{P}\hat{P}\psi(\vec{x},t) = P\hat{P}\psi(\vec{x},t) = P^2\psi(\vec{x},t)$   
since  $\hat{P}\hat{P} = I$  and  $P^2 = 1 \implies$  Parity has eigenvalues  $P = \pm 1$ 

★ QED and QCD are invariant under parity
 ★ Experimentally observe that Weak Interactions do not conserve parity

#### **Intrinsic Parities of fundamental particles:**

#### Spin-1 Bosons

From Gauge Field Theory can show that the gauge bosons have P = -1

$$P_{\gamma} = P_g = P_{W^+} = P_{W^-} = P_Z = -1$$

Spin-<sup>1</sup>/<sub>2</sub> Fermions

From the Dirac equation showed:

Spin <sup>1</sup>/<sub>2</sub> particles have opposite parity to spin <sup>1</sup>/<sub>2</sub> anti-particles

Conventional choice: spin  $\frac{1}{2}$  particles have P = +1

$$P_{e^-} = P_{\mu^-} = P_{\tau^-} = P_{\nu} = P_q = +1$$

and anti-particles have opposite parity, i.e.

$$P_{e^+} = P_{\mu^+} = P_{\tau^+} = P_{\overline{\nu}} = P_{\overline{q}} = -1$$

**★** For Dirac spinors it was shown that the parity operator is:

$$\hat{P} = \gamma^0 = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & -1 \end{pmatrix}$$

#### Parity Conservation in QED and QCD

#### Consider the QED process $e^-q \rightarrow e^-q$

The Feynman rules for QED give:

$$-iM = [\overline{u}_e(p_3)ie\gamma^{\mu}u_e(p_1)]\frac{-ig_{\mu\nu}}{q^2}[\overline{u}_q(p_4)ie\gamma^{\nu}u_q(p_2)]$$

which can be expressed in terms of the electron and quark 4-vector currents:

$$\begin{split} M &= -\frac{e^2}{q^2} g_{\mu\nu} j_e^{\mu} j_q^{\nu} = -\frac{e^2}{q^2} j_e . j_q \\ \text{with} \quad j_e &= \overline{u}_e(p_3) \gamma^{\mu} u_e(p_1) \text{ and } \quad j_q = \overline{u}_q(p_4) \gamma^{\mu} u_q(p_2) \end{split}$$

**★**Consider the what happen to the matrix element under the parity transformation

Spinors transform as

$$u \stackrel{\hat{P}}{\to} \hat{P}u = \gamma^0 u$$

Adjoint spinors transform as

$$\overline{u} = u^{\dagger} \gamma^{0} \xrightarrow{P} (\hat{P}u)^{\dagger} \gamma^{0} = u^{\dagger} \gamma^{0} \gamma^{0} = u^{\dagger} \gamma^{0} \gamma^{0} = \overline{u} \gamma^{0}$$
$$\overline{u} \xrightarrow{\hat{P}} \overline{u} \gamma^{0}$$

• Hence  $j_e = \overline{u}_e(p_3)\gamma^{\mu}u_e(p_1) \xrightarrow{\hat{P}} \overline{u}_e(p_3)\gamma^0\gamma^{\mu}\gamma^0u_e(p_1)$ 

**★** Consider the components of the four-vector current

The time-like component remains unchanged and the space-like components change sign

Similarly 
$$j_q^0 \xrightarrow{\hat{P}} j_q^0 \longrightarrow j_q^k \longrightarrow -j_q^k \quad k = 1, 2, 3$$



**★** Consequently the four-vector scalar product

$$j_e \cdot j_q = j_e^0 j_q^0 - j_e^k j_q^k \xrightarrow{P} j_e^0 j_q^0 - (-j_e^k)(-j_q^k) = j_e \cdot j_q \quad k = 1,3$$

**QED Matrix Elements are Parity Invariant** 

Parity Conserved in QED

 $\star$  The QCD vertex has the same form and, thus,

Parity Conserved in QCD

#### **Parity Violation in \beta-Decay**

**★** The parity operator  $\hat{P}$  corresponds to a discrete transformation  $x \rightarrow -x$ , etc.

**+** Under the parity transformation:

Vectors<br/>change sign $\vec{r} \xrightarrow{\hat{P}} - \vec{r}$ <br/> $\vec{p} \xrightarrow{\hat{P}} - \vec{p}$  $(p_x = \frac{\partial}{\partial x}, etc.)$ Note B is an<br/>axial vector<br/> $d\vec{B} \propto \vec{J} \wedge \vec{r} d^3 \vec{r}$ Axial-Vectors<br/>unchanged $\vec{L} \xrightarrow{\hat{P}} \vec{L}$ <br/> $\vec{\mu} \xrightarrow{\hat{P}} \vec{\mu}$  $(\vec{L} = \vec{r} \wedge \vec{p})$  $d\vec{B} \propto \vec{J} \wedge \vec{r} d^3 \vec{r}$ 

★ 1957: C.S.Wu et al. studied beta decay of polarized cobalt-60 nuclei:

 $^{60}$ Co $\rightarrow^{60}$ Ni<sup>\*</sup> + e<sup>-</sup> +  $\overline{\nu}_{e}$ 

Observed electrons emitted preferentially in direction opposite to applied field



If parity were conserved: expect equal rate for producing e<sup>-</sup> in directions along and opposite to the nuclear spin.

★Conclude parity is violated in WEAK INTERACTION that the WEAK interaction vertex is **NOT** of the form  $\overline{u}_e \gamma^{\mu} u_{\nu}$ 

### **Bilinear Covariants**

★ The requirement of Lorentz invariance of the matrix element severely restricts the form of the interaction vertex. QED and QCD are "VECTOR" interactions:

$$j^{\mu} = \overline{\psi} \gamma^{\mu} \phi$$

This combination transforms as a 4-vector

★ In general, there are only 5 possible combinations of two spinors and the gamma matrices that form Lorentz invariant currents, called "bilinear covariants":

Туре	Form	Components	"Boson Spin"
SCALAR	$\overline{\psi}\phi$	1	0
PSEUDOSCALAR	$\overline{\psi}\gamma^5\phi$	1	0
<b>VECTOR</b>	$\overline{\psi}\gamma^{\mu}\phi$	4	1
<b>AXIAL VECTOR</b>	$\overline{\psi}\gamma^{\mu}\gamma^{5}\phi$	4	1
<b>TENSOR</b>	$\overline{\psi}(\gamma^{\mu}\gamma^{\nu}-\gamma^{\nu}\gamma^{\mu}$	) <b>ø 6</b>	2

★ Note that in total the sixteen components correspond to the 16 elements of a general 4x4 matrix: "decomposition into Lorentz invariant combinations"

★ In QED the factor  $g_{\mu\nu}$  arose from the sum over polarization states of the virtual photon (2 transverse + 1 longitudinal, 1 scalar) = (2J+1) + 1

★ Associate SCALAR and PSEUDOSCALAR interactions with the exchange of a SPIN-0 boson, etc. – no spin degrees of freedom

### **V-A Structure of the Weak Interaction**

- ★ The most general form for the interaction between a fermion and a boson is a linear combination of bilinear covariants
- ★ For an interaction corresponding to the exchange of a spin-1 particle the most general form is a linear combination of VECTOR and AXIAL-VECTOR
- ★ The form for WEAK interaction is <u>determined from experiment</u> to be VECTOR – AXIAL-VECTOR (V – A)



★ Can this account for parity violation?

★ First consider parity transformation of a pure AXIAL-VECTOR current  $j_A = \overline{\psi} \gamma^{\mu} \gamma^5 \phi$  with  $\gamma^5 = i \gamma^0 \gamma^1 \gamma^2 \gamma^3$ ;  $\gamma^5 \gamma^0 = -\gamma^0 \gamma^5$   $j_A = \overline{\psi} \gamma^{\mu} \gamma^5 \phi \xrightarrow{\hat{P}} \overline{\psi} \gamma^0 \gamma^{\mu} \gamma^5 \gamma^0 \phi = -\overline{\psi} \gamma^0 \gamma^{\mu} \gamma^0 \gamma^5 \phi$   $j_A^0 = \xrightarrow{\hat{P}} -\overline{\psi} \gamma^0 \gamma^0 \gamma^0 \gamma^5 \phi = -\overline{\psi} \gamma^0 \gamma^5 \phi = -j_A^0$  $j_A^k = \xrightarrow{\hat{P}} -\overline{\psi} \gamma^0 \gamma^k \gamma^0 \gamma^5 \phi = +\overline{\psi} \gamma^k \gamma^5 \phi = +j_A^k$  k = 1, 2, 3 or  $j_A^{\mu} \xrightarrow{\hat{P}} -j_{A\mu}$  • The space-like components remain unchanged and the time-like components change sign (the opposite to the parity properties of a vector-current)

$$j_A^0 \xrightarrow{\hat{P}} -j_A^0; \quad j_A^k \xrightarrow{\hat{P}} +j_A^k; \qquad j_V^0 \xrightarrow{\hat{P}} +j_V^0; \quad j_V^k \xrightarrow{\hat{P}} -j_V^k$$

• Now consider the matrix elements

$$M \propto g_{\mu\nu} j_1^{\mu} j_2^{\nu} = j_1^0 j_2^0 - \sum_{k=1,3} j_1^k j_2^k$$

- For the combination of a two axial-vector currents  $j_{A1}.j_{A2} \xrightarrow{\hat{P}} (-j_1^0)(-j_2^0) - \sum_{k=1,3} (j_1^k)(j_2^k) = j_{A1}.j_{A2}$
- Consequently parity is conserved for both a pure vector and pure axial-vector interactions
- However the combination of a vector current and an axial vector current

$$j_{V1}.j_{A2} \xrightarrow{P} (j_1^0)(-j_2^0) - \sum_{k=1,3} (-j_1^k)(j_2^k) = -j_{V1}.j_{A2}$$

changes sign under parity – can give parity violation !

★ Now consider a general linear combination of VECTOR and AXIAL-VECTOR (note this is relevant for the Z-boson vertex)

$$\psi_{1} \qquad \mu \qquad \phi_{1} \qquad j_{1} = \overline{\phi}_{1} (g_{V} \gamma^{\mu} + g_{A} \gamma^{\mu} \gamma^{5}) \psi_{1} = g_{V} j_{1}^{V} + g_{A} j_{1}^{A} \qquad \frac{g_{\mu v}}{q^{2} - m^{2}} \qquad \psi_{2} \qquad \phi_{2} \qquad j_{2} = \overline{\phi}_{2} (g_{V} \gamma^{\mu} + g_{A} \gamma^{\mu} \gamma^{5}) \psi_{2} = g_{V} j_{2}^{V} + g_{A} j_{2}^{A} \qquad M_{fi} \propto j_{1} \cdot j_{2} = g_{V}^{2} j_{1}^{V} \cdot j_{2}^{V} + g_{A}^{2} j_{1}^{A} \cdot j_{2}^{A} + g_{V} g_{A} (j_{1}^{V} \cdot j_{2}^{A} + j_{1}^{A} \cdot j_{2}^{V})$$

Consider the parity transformation of this scalar product

$$j_1.j_2 \xrightarrow{P} g_V^2 j_1^V.j_2^V + g_A^2 j_1^A.j_2^A - g_V g_A(j_1^V.j_2^A + j_1^A.j_2^V)$$

• If either  $g_A$  or  $g_V$  is zero, Parity is conserved, i.e. parity conserved in a pure VECTOR or pure AXIAL-VECTOR interaction

• Relative strength of parity violating part  $\propto$ 

$$\frac{g_V g_A}{g_V^2 + g_A^2}$$

Maximal Parity Violation for V-A (or V+A)

### **Chiral Structure of QED (Reminder)**

**★** The CHIRAL projections operators

$$P_R = \frac{1}{2}(1+\gamma^5); \quad P_L = \frac{1}{2}(1-\gamma^5)$$

project out chiral right- and left- handed states

★ In the ultra-relativistic limit, chiral states correspond to helicity states

★ Any spinor can be expressed as:

$$\boldsymbol{\psi} = \frac{1}{2}(1+\gamma^5)\boldsymbol{\psi} + \frac{1}{2}(1-\gamma^5)\boldsymbol{\psi} = P_R\boldsymbol{\psi} + P_L\boldsymbol{\psi} = \boldsymbol{\psi}_R + \boldsymbol{\psi}_L$$

**The QED vertex**  $\overline{\psi}\gamma^{\mu}\phi$  in terms of chiral states:

$$\overline{\psi}\gamma^{\mu}\phi = \overline{\psi}_{R}\gamma^{\mu}\phi_{R} + \overline{\psi}_{R}\gamma^{\mu}\phi_{L} + \overline{\psi}_{L}\gamma^{\mu}\phi_{R} + \overline{\psi}_{L}\gamma^{\mu}\phi_{L}$$

conserves chirality, e.g.

$$\overline{\Psi}_R \gamma^\mu \phi_L = \frac{1}{2} \psi^\dagger (1+\gamma^5) \gamma^0 \gamma^\mu \frac{1}{2} (1-\gamma^5) \phi$$
  
$$= \frac{1}{4} \psi^\dagger \gamma^0 (1-\gamma^5) \gamma^\mu (1-\gamma^5) \phi$$
  
$$= \frac{1}{4} \overline{\psi} \gamma^\mu (1+\gamma^5) (1-\gamma^5) \phi = 0$$

★ In the ultra-relativistic limit only two helicity combinations are non-zero



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## **Helicity Structure of the WEAK Interaction**

**\star** The charged current (**W**<sup> $\pm$ </sup>) weak vertex is:

$$\frac{-ig_w}{\sqrt{2}}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)$$



★Since  $\frac{1}{2}(1-\gamma^5)$  projects out left-handed chiral particle states:  $\overline{\psi}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)\phi = \overline{\psi}\gamma^{\mu}\phi_L$ 

**★**Writing  $\overline{\psi} = \overline{\psi}_R + \overline{\psi}_L$  and from discussion of QED,  $\overline{\psi}_R \gamma^\mu \phi_L = 0$  gives  $\overline{\psi}_{\frac{1}{2}} \gamma^\mu (1 - \gamma^5) \phi = \overline{\psi}_L \gamma^\mu \phi_L$ 



Only the left-handed chiral components of particle spinors and right-handed chiral components of anti-particle spinors participate in charged current weak interactions

★At very high energy  $(E \gg m)$ , the left-handed chiral components are helicity eigenstates :



LEFT-HANDED PARTICLES Helicity = -1

RIGHT-HANDED ANTI-PARTICLES Helicity = +1



e.g. In the relativistic limit, the only possible electron – neutrino interactions are:





## **Helicity in Pion Decay**

★ The decays of charged pions provide a good demonstration of the role of helicity in the weak interaction



Might expect the decay to electrons to dominate – due to increased phase space.... The opposite happens, the electron decay is helicity suppressed

#### ★ Consider decay in pion rest frame.

- Pion is spin zero: so the spins of the  $\sqrt{a}$  and  $\mu$  are opposite
- Weak interaction only couples to RH chiral anti-particle states. Since neutrinos are (almost) massless, must be in RH Helicity state
- Therefore, to conserve angular mom. muon is emitted in a RH HELICITY state



But only left-handed CHIRAL particle states participate in weak interaction

**★** The general right-handed helicity solution to the Dirac equation is

$$u_{\uparrow} = N \begin{pmatrix} c \\ e^{i\phi}s \\ \frac{|\vec{p}|}{E+m}c \\ \frac{|\vec{p}|}{E+m}e^{i\phi}s \end{pmatrix} \quad \text{with} \quad c = \cos\frac{\theta}{2} \text{ and } \quad s = \sin\frac{\theta}{2}$$

project out the left-handed <u>chiral</u> part of the wave-function using

$$P_L = \frac{1}{2}(1 - \gamma^5) = \frac{1}{2} \begin{pmatrix} 1 & 0 & -1 & 0 \\ 0 & 1 & 0 & -1 \\ -1 & 0 & 1 & 0 \\ 0 & -1 & 0 & 1 \end{pmatrix}$$

giving 
$$P_L u_{\uparrow} = \frac{1}{2} N \left( 1 - \frac{|\vec{p}|}{E+m} \right) \begin{pmatrix} c \\ e^{i\phi}s \\ -c \\ -e^{i\phi}s \end{pmatrix} = \frac{1}{2} N \left( 1 - \frac{|\vec{p}|}{E+m} \right) u_L$$

In the limit  $m \ll E$  this tends to zero

• similarly

$$P_R u_{\uparrow} = \frac{1}{2} N \left( 1 + \frac{|\vec{p}|}{E+m} \right) \begin{pmatrix} c \\ e^{i\phi} s \\ c \\ e^{i\phi} s \end{pmatrix} = \frac{1}{2} N \left( 1 + \frac{|\vec{p}|}{E+m} \right) u_R$$

In the limit 
$$m \ll E$$
 ,  $P_R u_\uparrow 
ightarrow u_R$ 



In the limit  $E \gg m$ , as expected, the RH chiral and helicity states are identical

Although only LH chiral particles participate in the weak interaction the contribution from RH Helicity states is not necessarily zero !

$$\overline{v}_{\mu}$$
 ←  $\overline{v}_{\mu}$  ↓  $\mu^{-}$   
m<sub>ν</sub> ≈ 0: RH Helicity ≡ RH Chiral  $m_{\mu} \neq 0$ : RH Helicity has LH Chiral Component

★ Expect matrix element to be proportional to LH chiral component of RH Helicity electron/muon spinor

$$M_{fi} \propto \frac{1}{2} \left( 1 - \frac{|\vec{p}|}{E+m} \right) = \frac{m_{\mu}}{m_{\pi} + m_{\mu}}$$
 from the kinematics of pion decay at rest

+ Hence because the electron mass is much smaller than the pion mass the decay  $\pi^- \rightarrow e^- \overline{\nu}_e$  is heavily suppressed.

#### **Evidence for V-A**

**★** The V-A nature of the charged current weak interaction vertex fits with experiment

**EXAMPLE** charged pion decay

•Experimentally measure:

$$\frac{\Gamma(\pi^- \to e^- \overline{\nu}_e)}{\Gamma(\pi^- \to \mu^- \overline{\nu}_\mu)} = (1.230 \pm 0.004) \times 10^{-4}$$

•Theoretical predictions (depend on Lorentz Structure of the interaction)

V-A 
$$(\overline{\psi}\gamma^{\mu}(1-\gamma^{5})\phi)$$
 or V+A  $(\overline{\psi}\gamma^{\mu}(1+\gamma^{5})\phi) \implies \frac{\Gamma(\pi^{-} \to e^{-}\overline{\nu}_{e})}{\Gamma(\pi^{-} \to \mu^{-}\overline{\nu}_{\mu})} \approx 1.3 \times 10^{-4}$   
Scalar  $(\overline{\psi}\phi)$  or Pseudo-Scalar  $(\overline{\psi}\gamma^{5}\phi) \implies \frac{\Gamma(\pi^{-} \to e^{-}\overline{\nu}_{e})}{\Gamma(\pi^{-} \to \mu^{-}\overline{\nu}_{\mu})} = 5.5$ 

**EXAMPLE** muon decay



Measure electron energy and angular distributions relative to muon spin direction. Results expressed in terms of general S+P+V+A+T form in "Michel Parameters"

e.g. TWIST expt:  $6x10^9 \mu$  decays Phys. Rev. Lett. 95 (2005) 101805

 $\rho = 0.75080 \pm 0.00105$ 

V-A Prediction:  $\rho = 0.75$ 

 $\theta_{e}$ 

### **Weak Charged Current Propagator**

The charged-current Weak interaction is different from QED and QCD in that it is mediated by massive W-bosons (80.3 GeV)

This results in a more complicated form for the propagator:



In addition the sum over W boson polarization states modifies the numerator

 $\alpha$ 



spin 1 W<sup>±</sup> 
$$\frac{-i\left[g_{\mu\nu} - q_{\mu}q_{\nu}/m_W^2\right]}{q^2 - m_W^2} \qquad \overset{\mu}{\sim} \overset{q}{\sim} \overset{q}{\sim} \overset{\nu}{\sim} \overset{\nu}{\sim}$$

However in the limit where  $q^2$  is small compared with  $m_W = 80.3 \,\text{GeV}$  the interaction takes a simpler form.

W-boson propagator ( 
$$q^2 \ll m_W^2$$
 )  $\frac{i g_{\mu \nu}}{m_W^2}$   $\mu_{\bullet} v$ 

The interaction appears point-like (i.e no q<sup>2</sup> dependence)

### **Connection to Fermi Theory**

**\star** In 1934, before the discovery of parity violation, Fermi proposed, in analogy with QED, that the invariant matrix element for  $\beta$ -decay was of the form:

$$M_{fi} = G_{\rm F} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} \psi] [\overline{\psi} \gamma^{\nu} \psi]$$

where  $G_{\rm F} = 1.166 \times 10^{-5} \, {\rm GeV^{-2}}$ 

Note the absence of a propagator : i.e. this represents an interaction at a point

★ After the discovery of parity violation in 1957 this was modified to

$$M_{fi} = \frac{G_{\rm F}}{\sqrt{2}} g_{\mu\nu} [\overline{\psi} \gamma^{\mu} (1 - \gamma^5) \psi] [\overline{\psi} \gamma^{\nu} (1 - \gamma^5) \psi]$$

(the factor of  $\sqrt{2}$  was included so the numerical value of  $G_{\rm F}$  did not need to be changed)

**★** Compare to the prediction for W-boson exchange

## Strength of Weak Interaction

**★** Strength of weak interaction most precisely measured in muon decay



• To a very good approximation the W-boson propagator can be written  $\frac{-i\left[g_{\mu\nu} - q_{\mu}q_{\nu}/m_{W}^{2}\right]}{q^{2} - m_{W}^{2}} \approx \frac{ig_{\mu\nu}}{m_{W}^{2}}$ 

measure  $g_W^2/m_W^2$   $\rightarrow G_F = 1.16639(1) \times 10^{-5} \,\text{GeV}^{-2}$ Muon decay



**To obtain the intrinsic strength of weak interaction need to know mass of** W-boson:  $m_W = 80.403 \pm 0.029 \,\text{GeV}$ 

$$\Rightarrow \ \alpha_W = \frac{g_W^2}{4\pi} = \frac{8m_W^2 G_F}{4\sqrt{2}\pi} = \frac{1}{30}$$

The intrinsic strength of the weak interaction is similar to, but greater than, the EM interaction ! It is the massive W-boson in the propagator which makes it appear weak. For  $q^2 \gg m_W^2$  weak interactions are more likely than EM.

#### **Summary**

★ Weak interaction is of form Vector – Axial-vector (V-A)

$$\frac{-ig_w}{\sqrt{2}}\frac{1}{2}\gamma^{\mu}(1-\gamma^5)$$

★ Consequently only left-handed chiral particle states and right-handed chiral anti-particle states participate in the weak interaction

MAXIMAL PARITY VIOLATION

**★** Weak interaction also violates Charge Conjugation symmetry

**\star** At low  $q^2$  weak interaction is only weak because of the large W-boson mass

$$\frac{G_{\rm F}}{\sqrt{2}} = \frac{g_W^2}{8m_W^2}$$

**★** Intrinsic strength of weak interaction is similar to that of QED