



Top Secret



The "Truth" Story

C.-P. Yuan

Michigan State University

- Introduction
- Mass of Top Quark, prior to its discovery
- Top & Electroweak Symmetry Breaking
- Properties of Top
- Discriminate Models of Electroweak Symmetry Breaking
- Conclusion

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People have long asked,

“ What is the world made of? ”

and

“ What holds it together? ”

Elementary Particle Physics or High Energy Physics

Studying Fundamental Interactions (**Forces**)
in Nature

Leptons

- Don't feel the strong force
- Integer or Zero charge
- Flavours:

e^-	“electron” (0.511 MeV)	(1897)	In atoms
μ^-	“Muon” (206 m_e)	(1937)	First seen in Cosmic Ray
τ^-	“Tau” (17 m_μ)	(1975)	Seen at SLAC (Stanford Linear Accelerator Center)
ν_e	“electron neutrino” Pauli's explanation of Beta Decay (1930)	(1956)	Mass $\nu_e < 3 \text{ eV}$ $\nu_\mu < 0.19 \text{ MeV}$ $\nu_\tau < 18.2 \text{ MeV}$
ν_μ	“Muon neutrino”	(1962)	
ν_τ	“Tau neutrino”	(2000)	

Quarks

- Feel the strong force
- Fractionally charged

$$Q = \begin{cases} 2/3 \\ -1/3 \end{cases} \times \text{Proton charge}$$

- Constituents of neutron and proton
(udd) (uud)

$\begin{pmatrix} u \\ d \end{pmatrix}$ “up”
“down”

- First Evidence:

Stanford Linear Accelerator Center
(Giant Electron Microscope)

- Flavors:

u “up”
d “down”
s “strange”
c “charmed”
b “bottom”
t “top”

(1974)

(1977)

(1995)

@ Fermilab
(Tevatron)

“Beauty”
“Truth”



Interactions

Four forces in Nature

1 Gravity



Newton



2 Electromagnetism



Faraday



3 Weak Interaction

Beta (radioactive) decay

Sun is shining

Time scales: $10^{-12} \sim 10^3$ sec



4 Strong Interaction

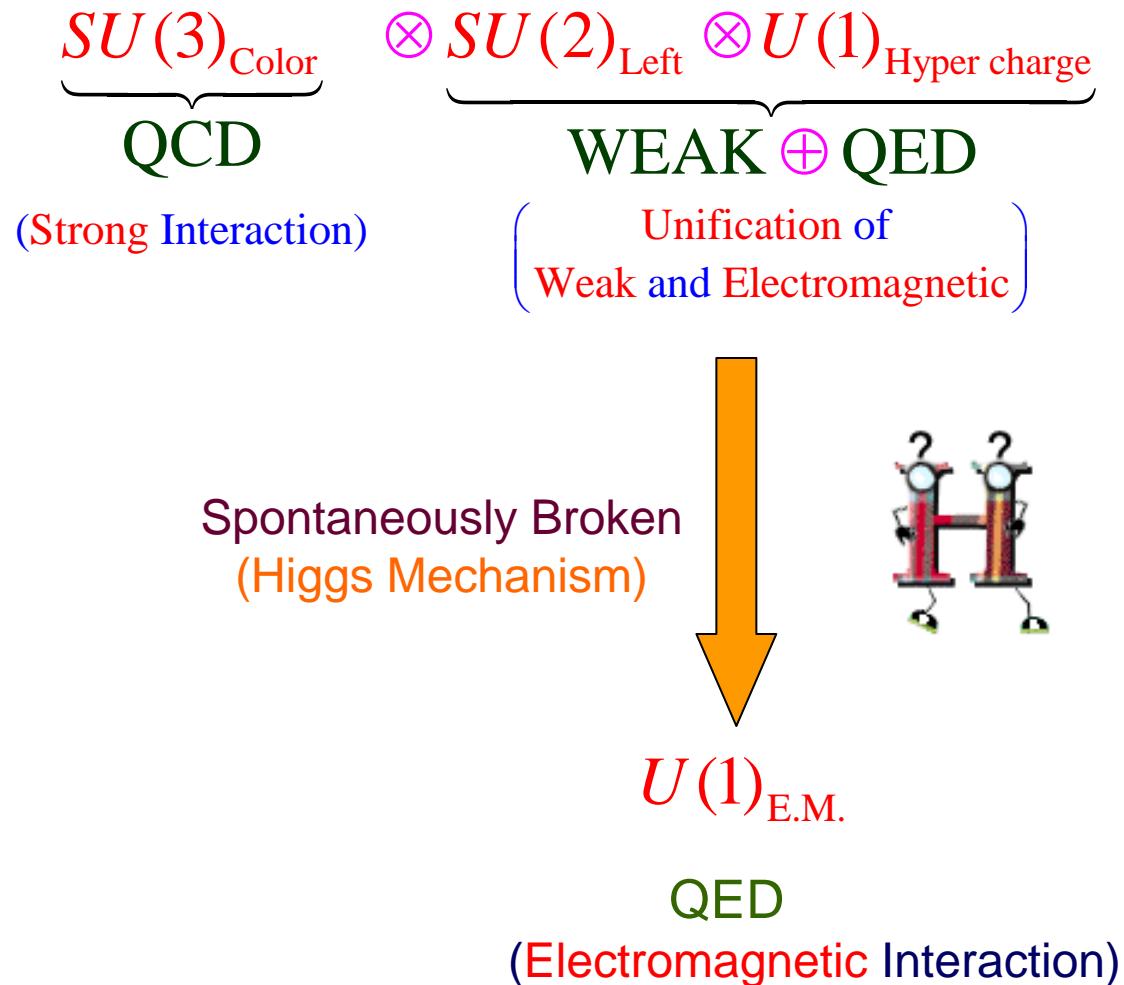
Hold nuclei together

Time scales: 10^{-23} sec



The Standard Model of Particle Physics

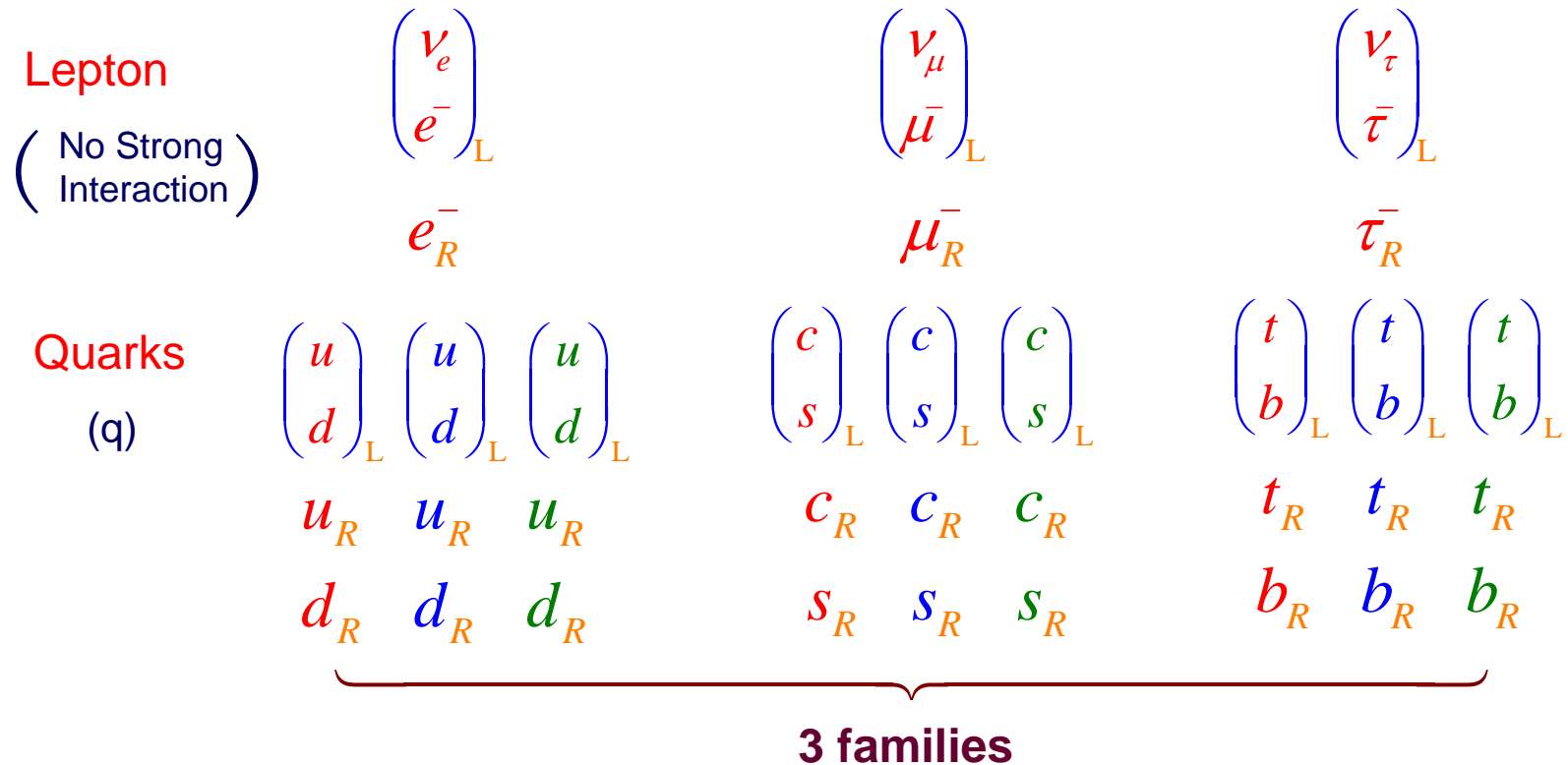
❖ Gauge Symmetry (Gravity is not included)



The Standard Model of Particle Physics

❖ Matter fields (make up all visible matter in the universe)

▪ Fermions (Spin 1/2)



▪ Scalar (Spin 0)

Higgs Boson (Not yet found!)

(From Higgs Mechanism — Spontaneous Symmetry Breaking)

The Standard Model of Particle Physics

❖ Interactions (mediated by interchanging Gauge Bosons, spin-1 force carrier)

1) Electromagnetic Interaction (QED)

Photon (massless)

2) Strong Interaction (QCD)

Gluon (massless) (1979)

3) Weak Interaction

W^+ , W^- and Z Gauge Bosons (1983)

(massive $M_w = 80.42 \text{ GeV}$ $M_z = 91.187 \text{ GeV}$ $1 \text{ GeV} = 10^9 \text{ eV}$)

In SM, the Mass of W-boson, either W^\pm or Z , arises from the Higgs Mechanism

(Without it, Gauge Bosons have to be massless from gauge principle.)

Higgs Mechanism in the SM

Two outstanding mysteries in the Electroweak theory :

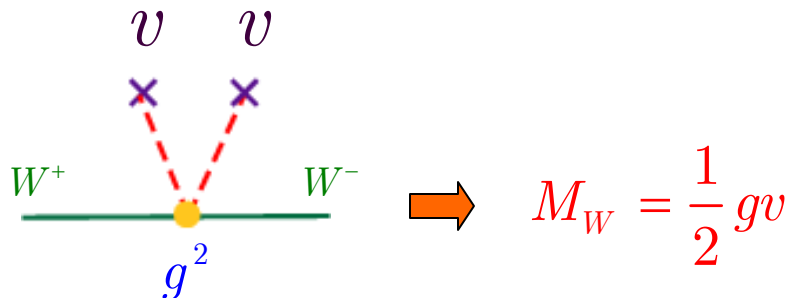
- The cause of **Electroweak Symmetry Breaking**
($M_W = 80 \text{ GeV}$, $M_Z = 91 \text{ GeV}$)
- The origin of **Flavor Symmetry Breaking**
(Quarks and Leptons have diverse masses.)

Both Symmetry Breaking are accommodated by including a fundamental **weak doublet of scalar (Higgs) boson**:

$$\Phi = \begin{pmatrix} \frac{v + H + i\phi^0}{\sqrt{2}} \\ i\phi^- \end{pmatrix}$$

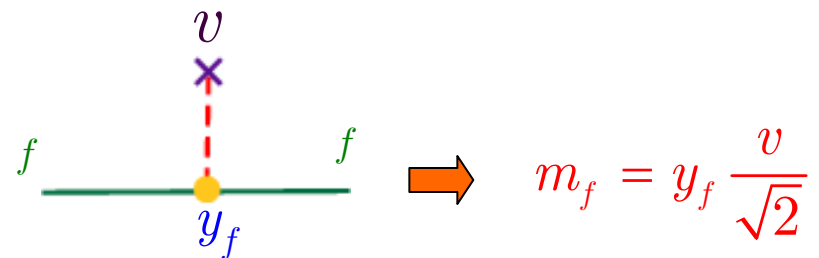
- To generate M_W and M_Z

$$L_\Phi = (D_\mu \Phi)^\dagger (D^\mu \Phi) - \lambda \left(\Phi^\dagger \Phi - \frac{v^2}{2} \right)^2$$



- To generate m_f

$$y_f \bar{F}_L \Phi f_R + \dots$$



How does SM predict ... ?

◆ In Quantum Mechanics

Schrodinger Equation:

$$i \frac{\partial \Psi}{\partial t} = H \Psi$$

1. Figure out what **H** is.
2. Insert **H** in S.E.
3. Calculate Predictions

◆ In Relativistic Quantum Field Theory

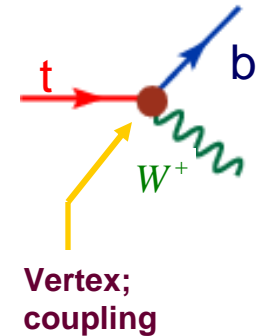
SM gives the Interaction Lagrangian \mathcal{L}

\mathcal{L}
↓

Feynman Rules
Feynman Diagrams }
↓

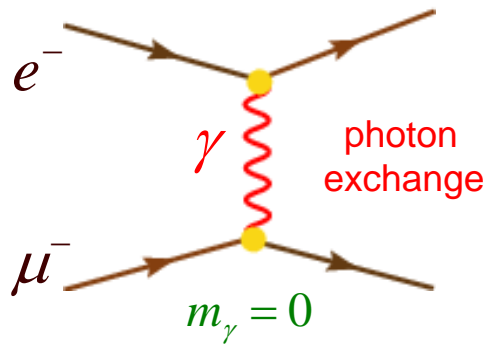
S-Matrix Elements
↓

Predictions

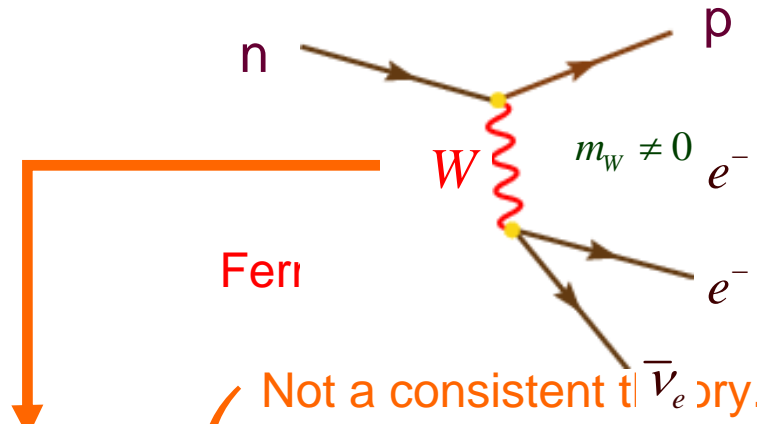


Electro-weak Unification

Electromagnetic Interaction:



Weak Interaction: (Beta Decay)



Not a consistent theory. Violates Unitarity condition.

Allows: Self-consistent calculations at high energy and to higher orders of perturbative theory

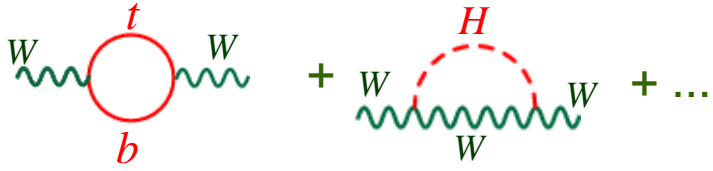
Prices to pay:

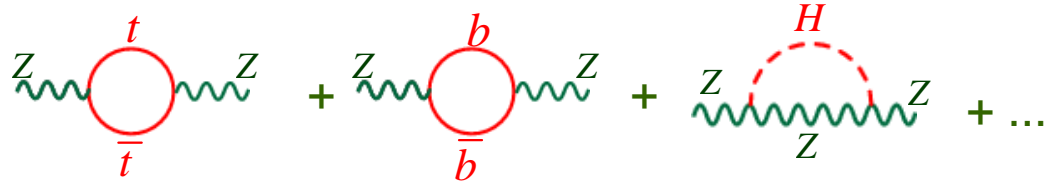
- 1) W^\pm must exist 1983
- 2) Simplest version requires also massive Z^0 1983

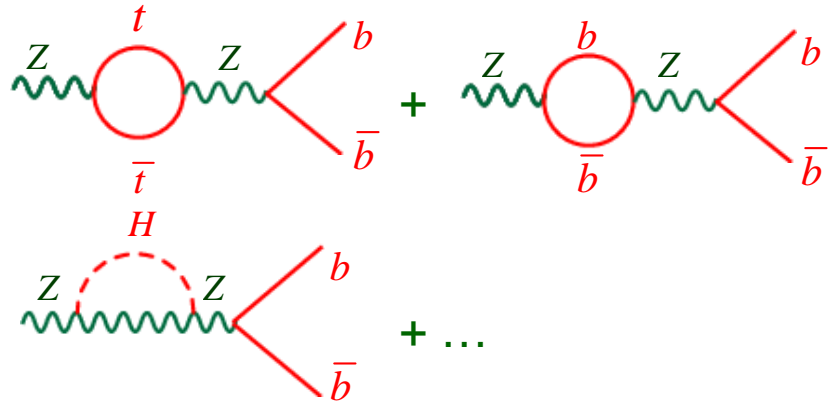
New weak charge preserving interactions 1973

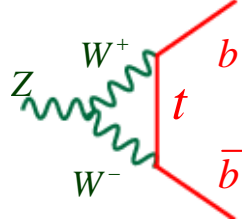
$\implies SU(2) \times U(1)$

Some Examples of Loop Corrections (Radiative corrections)

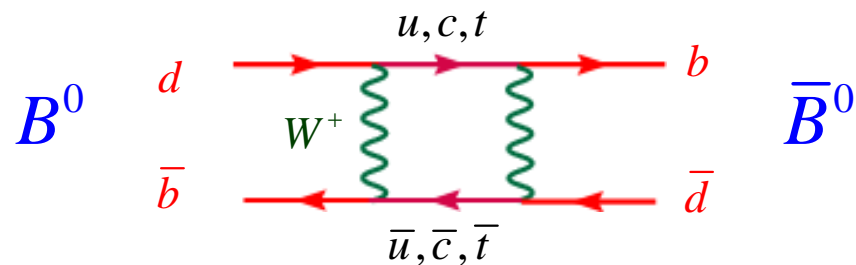
1) $m_W \sim$  + ... \longrightarrow Sum over Intermediate states

$m_Z \sim$  + ... \nearrow Sum over Intermediate states

2) $\Gamma_{Z \rightarrow b\bar{b}} \sim$  + ...



3) $B_d - \bar{B}_d$ mixing



Free Parameters in Standard Model

$$SU(3)_{\text{color}} \times SU(2)_{\text{Left}} \times U(1)_{\text{Hypercharge}}$$

$$\left. \begin{array}{l} g_3, g_2, g_1 \\ \lambda, \mu \end{array} \right\}$$

$$\left\{ \begin{array}{l} \alpha_S, \alpha_{\text{em}}, \theta_{\text{Weak mixing}} \\ V(\text{vacuum expectation value}) \\ m_H(\text{Higgs Boson mass}) \end{array} \right\}$$

This set can be traded by

$$\alpha_S, \alpha_{\text{em}}, G_F, m_Z, m_H$$

(3) Lepton masses

$$(e, \mu, \tau) \quad m_{\nu}'s=0$$

(6) Quark masses

$$(u, d, s, c, b, t)$$

Mixing of quark weak eigenstates
and mass eigenstates



3 angles and 1 phase
CP violation

(1) Strong CP phase



Total of **19** free parameters.
So far, all experimental data agree with the prediction of **SM**.

To include neutrino masses (suggested by Neutrino Oscillation data) in the SM

• For Dirac Neutrinos

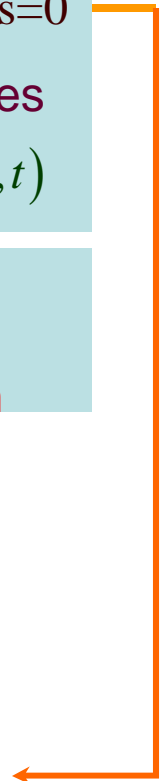


Add **3** masses and
3 mixing angles with
1 CP violation phase

• For Majorana Neutrinos

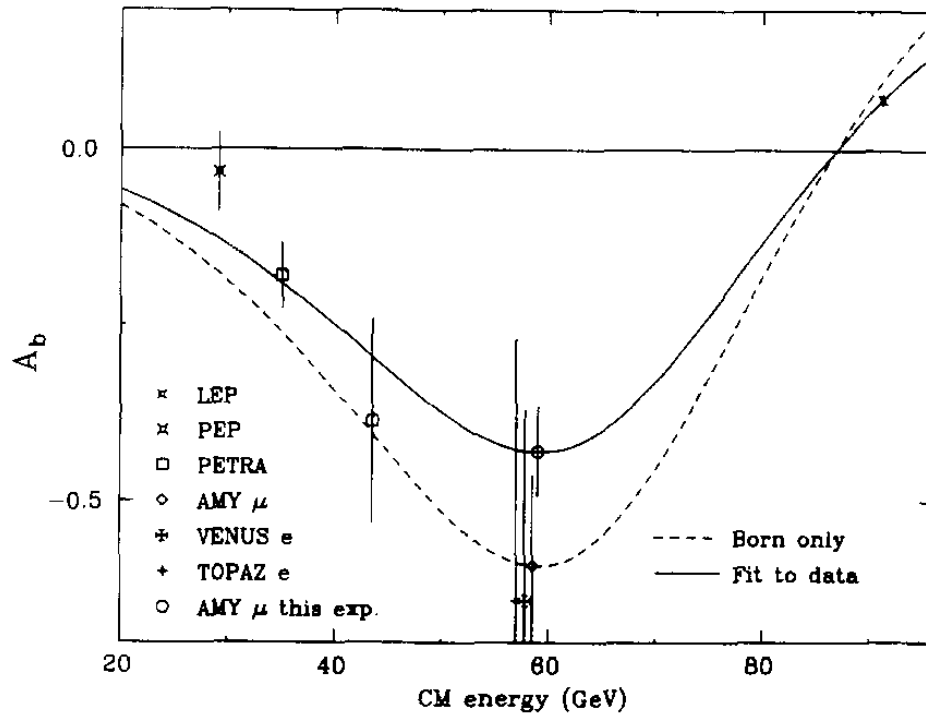


Add **3** masses and
3 mixing angles with
3 CP violation phase



Top Exists

(induced from data before 1990)

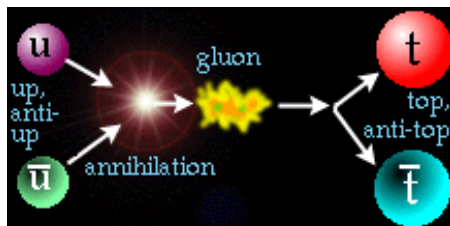


Forward-Backward Asymmetry of
bottom quark (A_b) in
 $e^+e^- \rightarrow b\bar{b}$
confirmed weak isospin of b

$$T_3 = -\frac{1}{2}$$

→ $T_3 = \frac{1}{2}$ state must exist,
which is called
TOP.

March 2, 1995



We had **champaign**
at the MSU High Energy physics
conference room to celebrate the
discovery of the **Top Quark** at **FNAL**
Tevatron by **CDF & D0** groups.

Recently,

$$m_t = 170.9 \pm 1.8 \text{ GeV}$$

Chronology of Top Hunting

Where is the Top Quark?

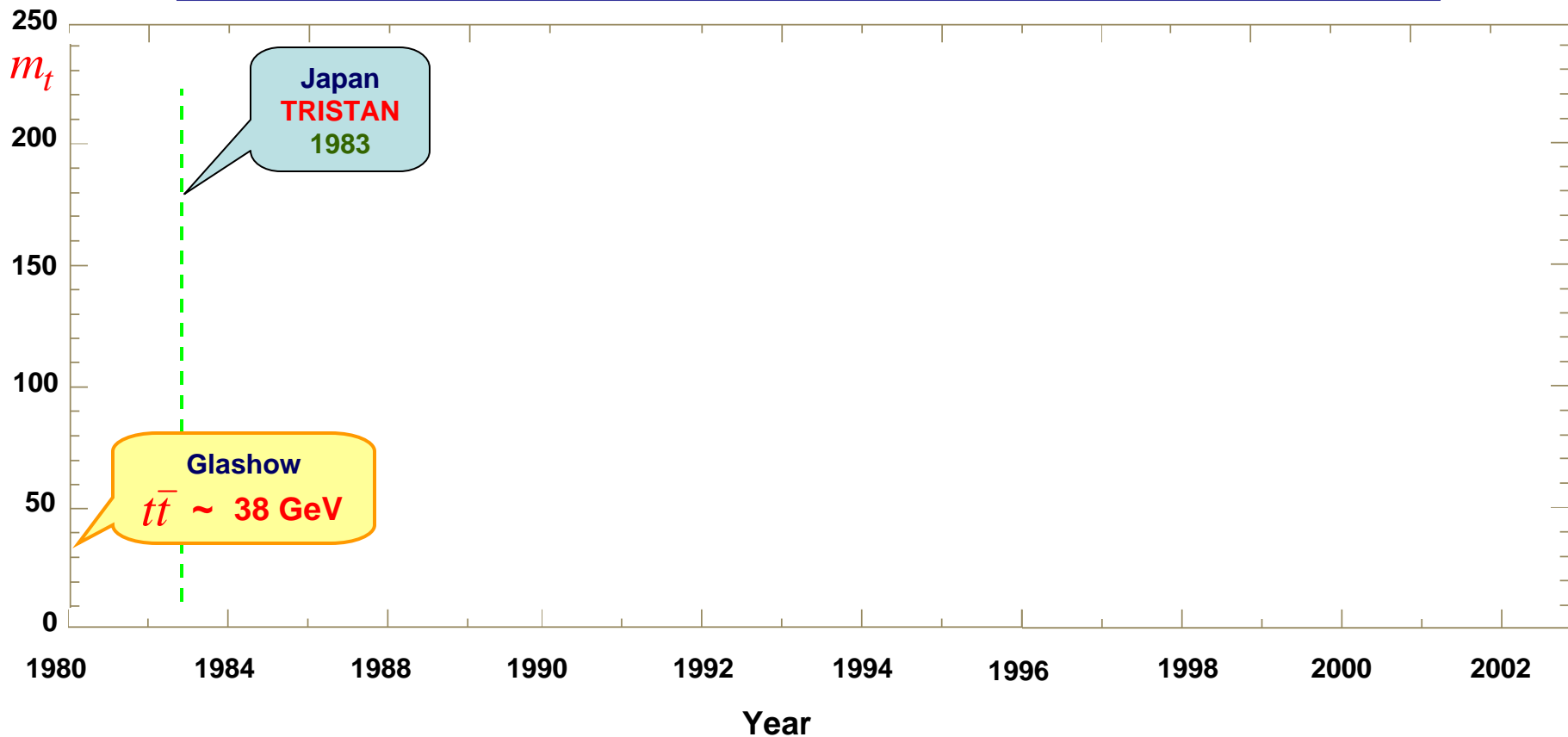
1980

Sheldon L. Glashow^(a)

*Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics,
Massachusetts Institute of Technology, Cambridge, Massachusetts 02139*

(Received 17 October 1980)

Arguments are presented suggesting that the top-quark analog of the J/ψ should lie at 38 ± 2 GeV. Should there exist a fourth $Q = \frac{2}{3}$ quark h , the first $\bar{h}h$ state must be heavier than 300 GeV.



Chronology of Top Hunting

MASS AND MIXING ANGLE PREDICTIONS FROM INFRA-RED FIXED POINTS

1980

B. PENDLETON and G.G. ROSS

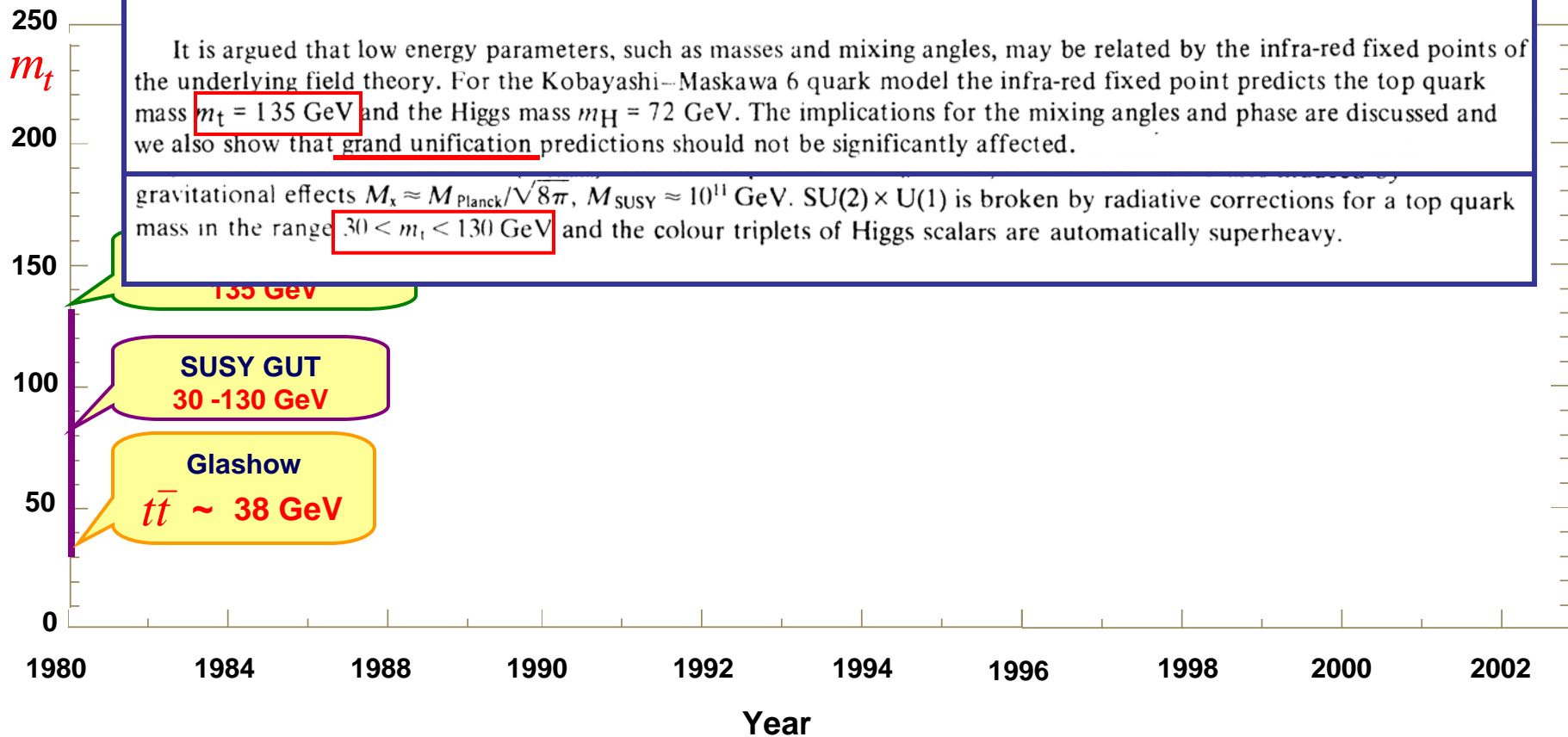
Theoretical Physics Department, Oxford OX1 3NP, UK

Received 15 July 1980

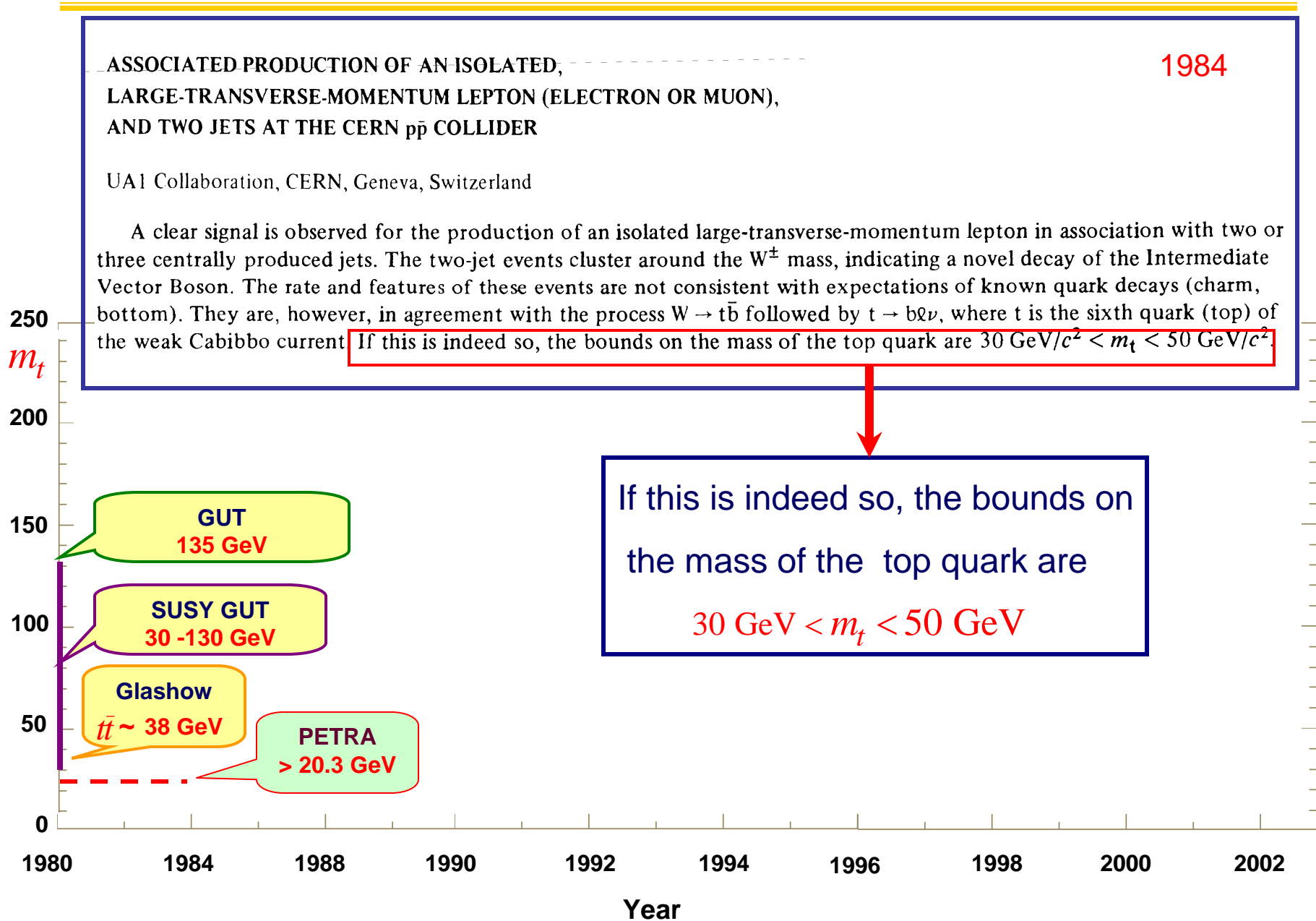
Revised manuscript received 3 November 1980

It is argued that low energy parameters, such as masses and mixing angles, may be related by the infra-red fixed points of the underlying field theory. For the Kobayashi–Maskawa 6 quark model the infra-red fixed point predicts the top quark mass $m_t = 135 \text{ GeV}$ and the Higgs mass $m_H = 72 \text{ GeV}$. The implications for the mixing angles and phase are discussed and we also show that grand unification predictions should not be significantly affected.

gravitational effects $M_x \approx M_{\text{Planck}}/\sqrt{8\pi}$, $M_{\text{SUSY}} \approx 10^{11} \text{ GeV}$. $SU(2) \times U(1)$ is broken by radiative corrections for a top quark mass in the range $30 < m_t < 130 \text{ GeV}$ and the colour triplets of Higgs scalars are automatically superheavy.



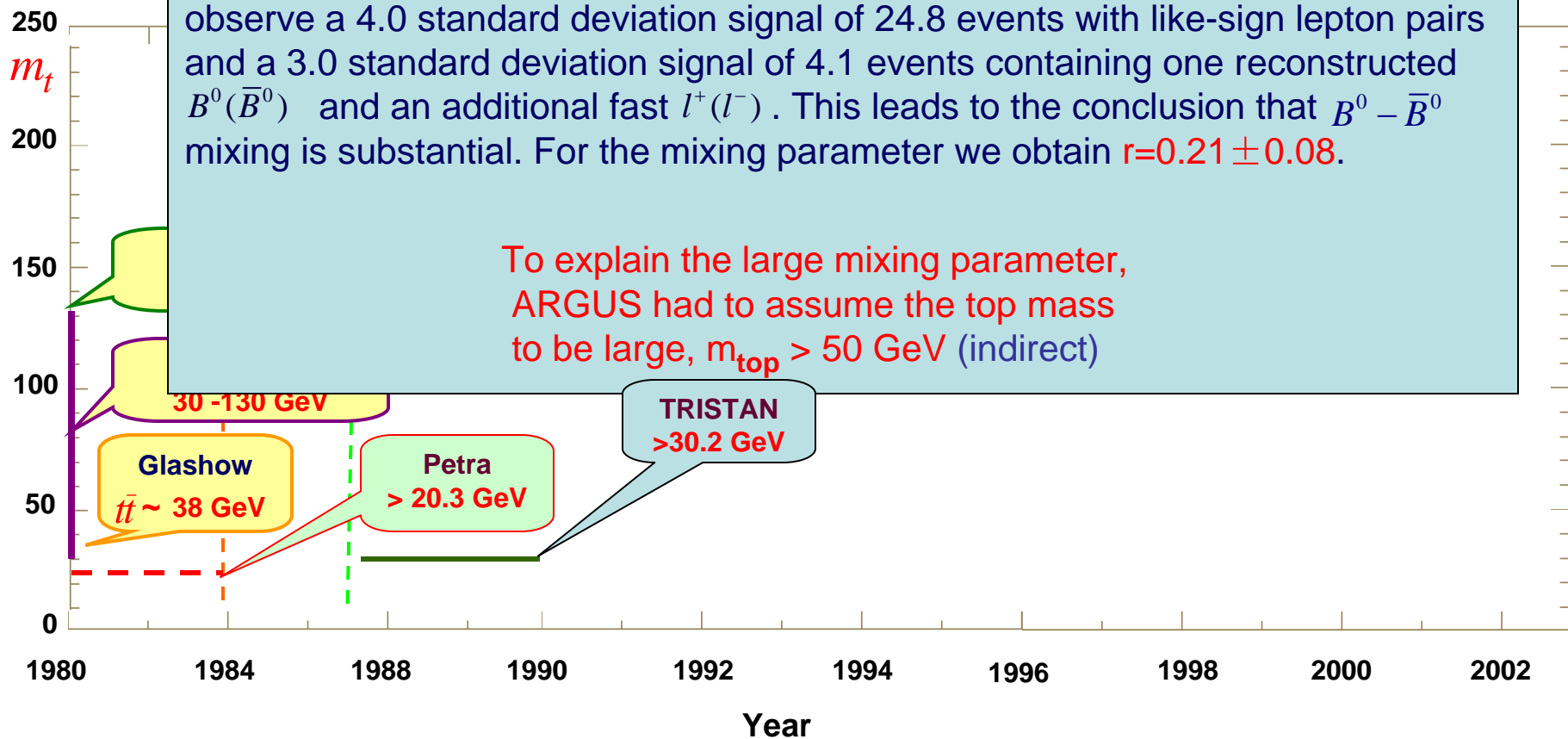
Chronology of Top Hunting



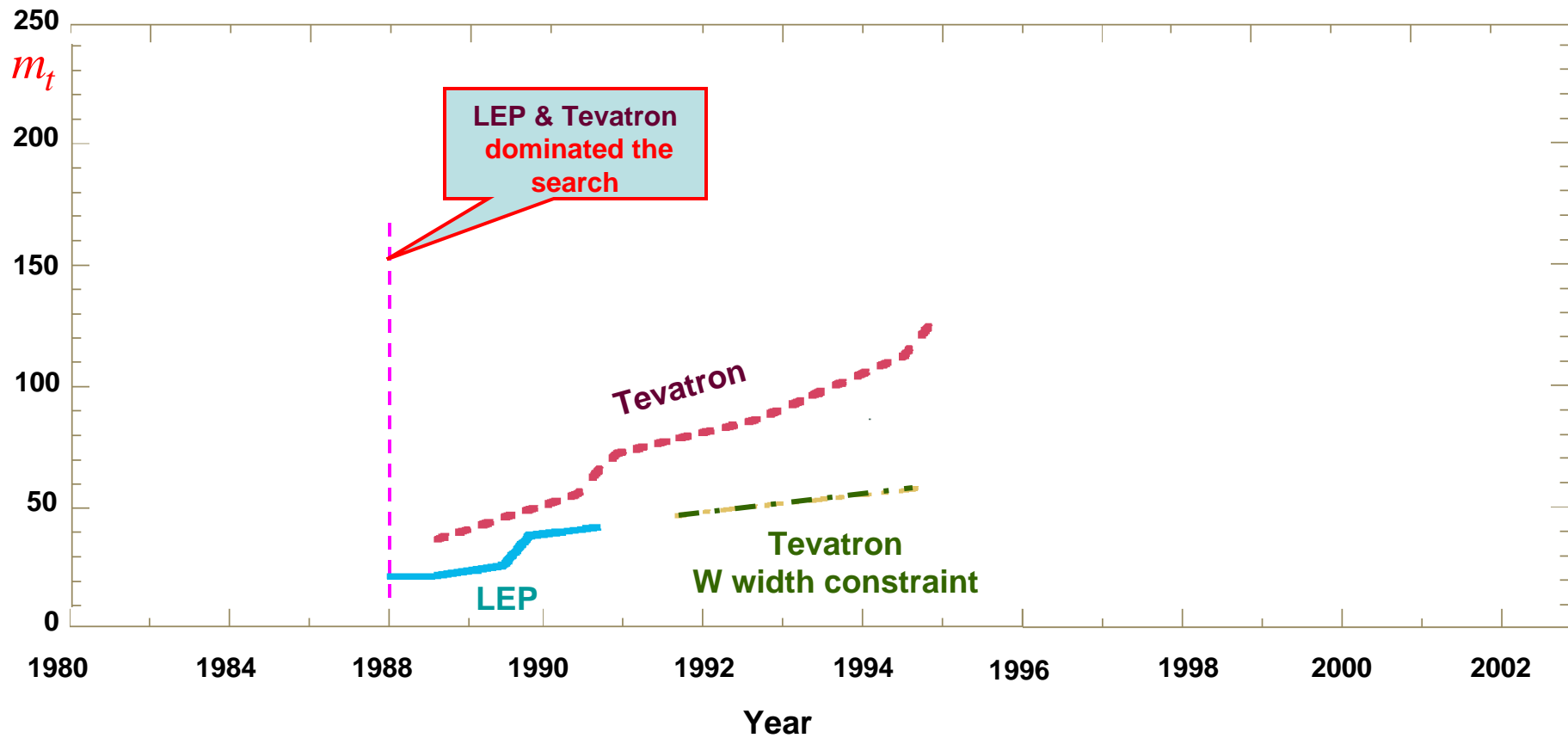
Chronology of Top Hunting

Observation of $B^0 - \bar{B}^0$ mixing
ARGUS Collaboration
Received 9 April 1987

Using the ARGUS detector at the DORIS II storage ring we have searched in three different ways for $B^0 - \bar{B}^0$ mixing in $\Upsilon(4S)$ decays. One explicitly mixed event, a decay $\Upsilon \rightarrow B^0 \bar{B}^0$, has been completely reconstructed. Furthermore, we observe a 4.0 standard deviation signal of 24.8 events with like-sign lepton pairs and a 3.0 standard deviation signal of 4.1 events containing one reconstructed $B^0(\bar{B}^0)$ and an additional fast $l^+(l^-)$. This leads to the conclusion that $B^0 - \bar{B}^0$ mixing is substantial. For the mixing parameter we obtain $r=0.21 \pm 0.08$.



Chronology of Top Hunting



Chronology of Top Hunting

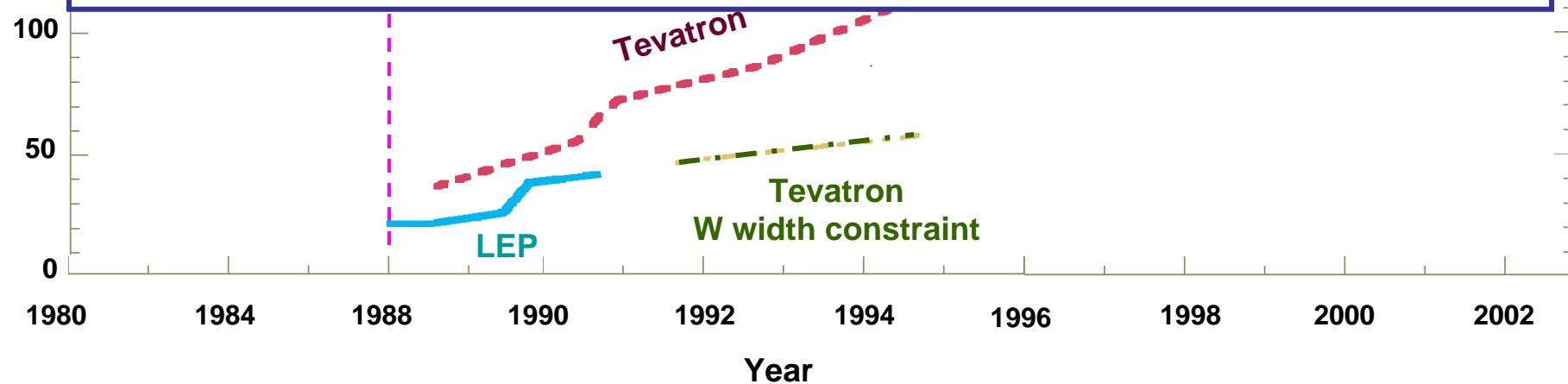
New method to detect a heavy top quark at the Fermilab Tevatron

C.-P. Yuan

High Energy Physics Division, Argonne National Laboratory, Argonne, Illinois 60439

(Received 15 May 1989)

We present a new method to detect a heavy top quark with mass ~ 180 GeV at the upgraded Fermilab Tevatron ($\sqrt{S} = 2$ TeV and integrated luminosity 100 pb^{-1}) and the Superconducting Super Collider (SSC) via the W -gluon fusion process. We show that an almost perfect efficiency for the “kinematic b tagging” can be achieved due to the characteristic features of the transverse momentum P_T and rapidity Y distributions of the spectator quark which emitted the virtual W . Hence, we can reconstruct the invariant mass $M^{e\nu b}$ and see a sharp peak within a 5-GeV-wide bin of the $M^{e\nu b}$ distribution. We conclude that more than one year of running is needed to detect a 180-GeV top quark at the upgraded Tevatron via the W -gluon fusion process. Its detection becomes easier at the SSC due to a larger event rate.



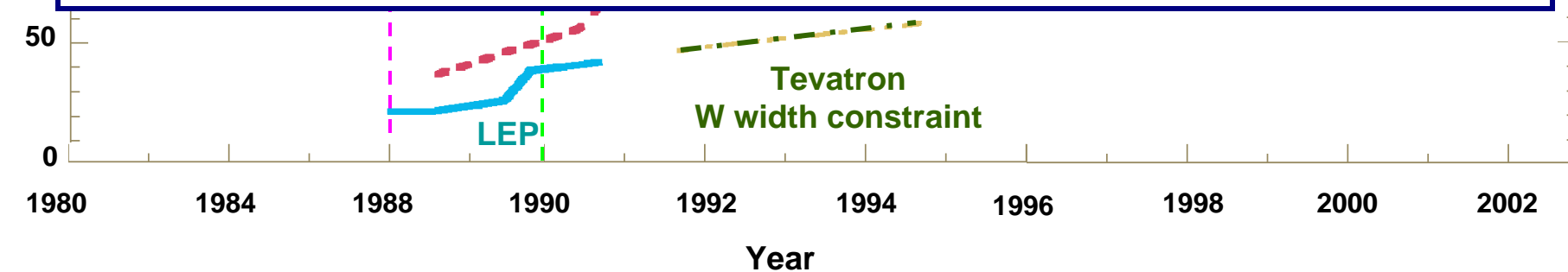
Chronology of Top Hunting

Minimal dynamical symmetry breaking of the standard model

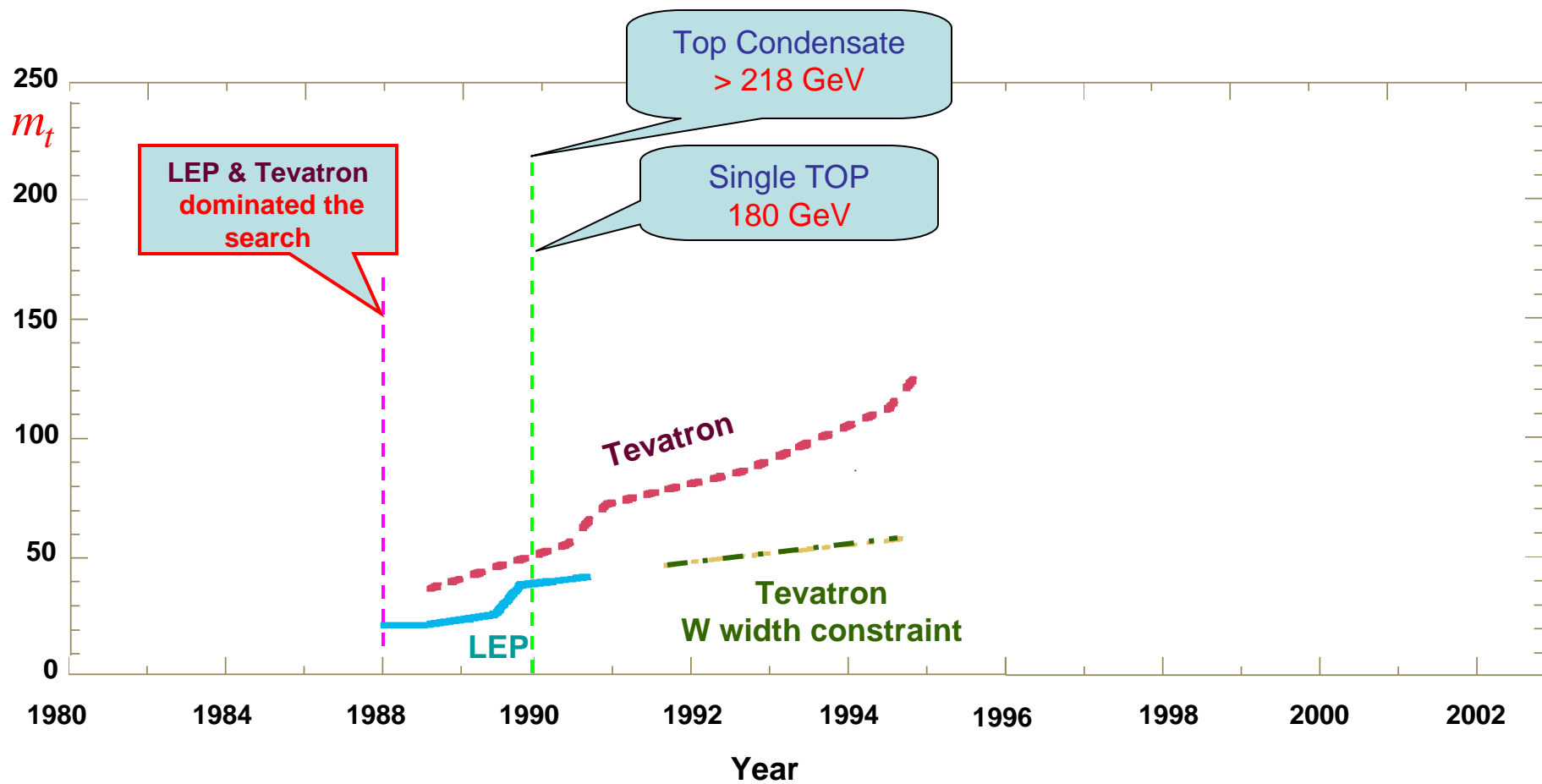
William A. Bardeen, Christopher T. Hill, and Manfred Lindner
Fermi National Accelerator Laboratory, P.O. Box 500, Batavia, Illinois 60510
 (Received 21 July 1989; revised manuscript received 2 November 1989)

We formulate the dynamical symmetry breaking of the standard model by a **top-quark condensate in analogy with BCS theory**. The low-energy effective Lagrangian is the usual standard model with supplemental relationships connecting masses of the top quark, W boson, and Higgs boson which now appears as a $\bar{t}t$ bound state. Precise predictions for m_t and m_H are obtained by abstracting the compositeness condition for the Higgs boson to boundary conditions on the renormalization-group equations for the full standard model at high energy.

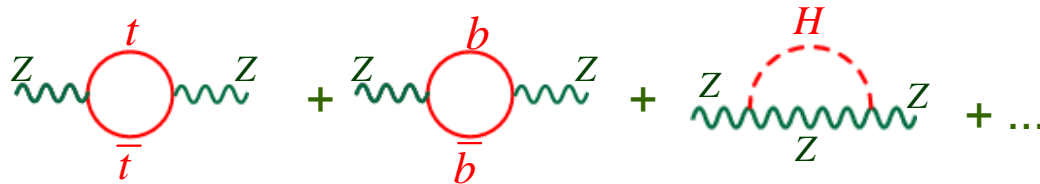
Λ (GeV)	10^{19}	10^{17}	10^{15}	10^{13}	10^{11}	10^{10}	10^9	10^8	10^7	10^6	10^5	10^4
m_t^{phys} (GeV)	218	223	229	237	248	255	264	277	293	318	360	455
Pert.	± 2	± 3	± 3	± 3	± 5	± 6	± 7	± 9	± 12	± 16	± 25	± 45
m_H^{phys} (GeV)	239	246	256	268	285	296	310	329	354	391	455	605
Pert.	± 3	± 3	± 4	± 5	± 8	± 9	± 11	± 15	± 21	± 32	± 56	± 142



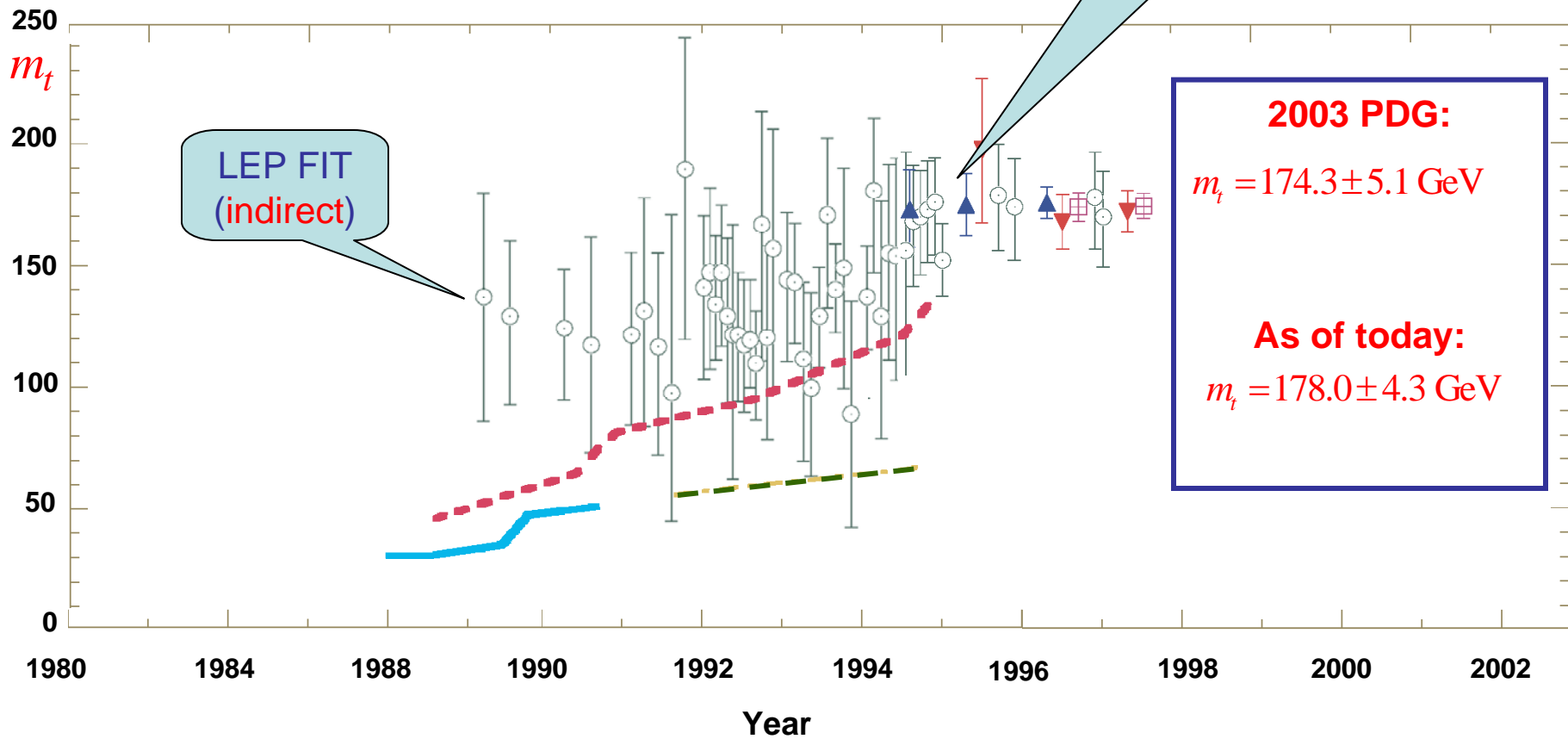
Chronology of Top Hunting



Chronology of Top Hunting



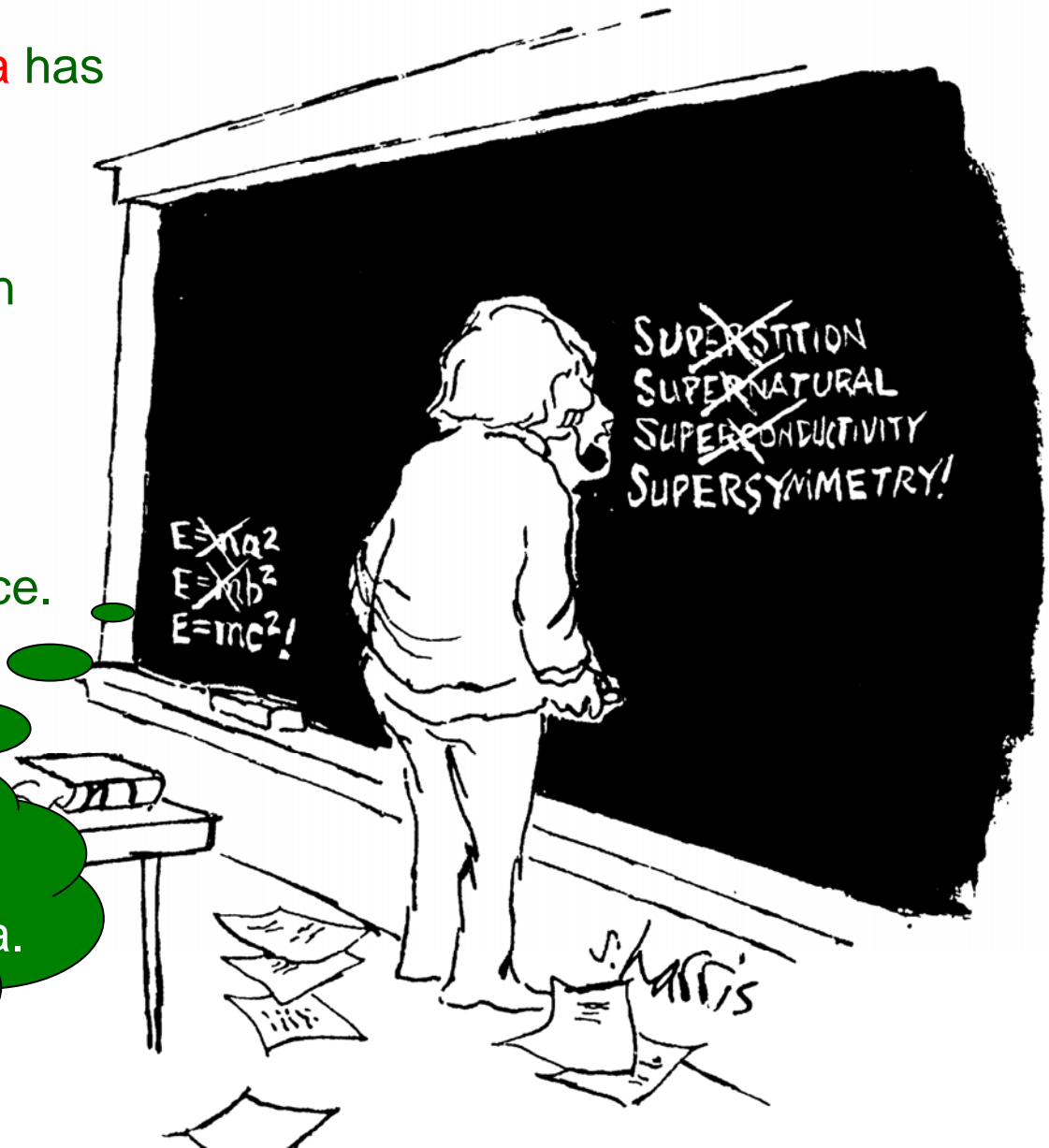
Discovery of TOP
@Tevatron



Lessons we learned from the History on the discovery of Top Quark

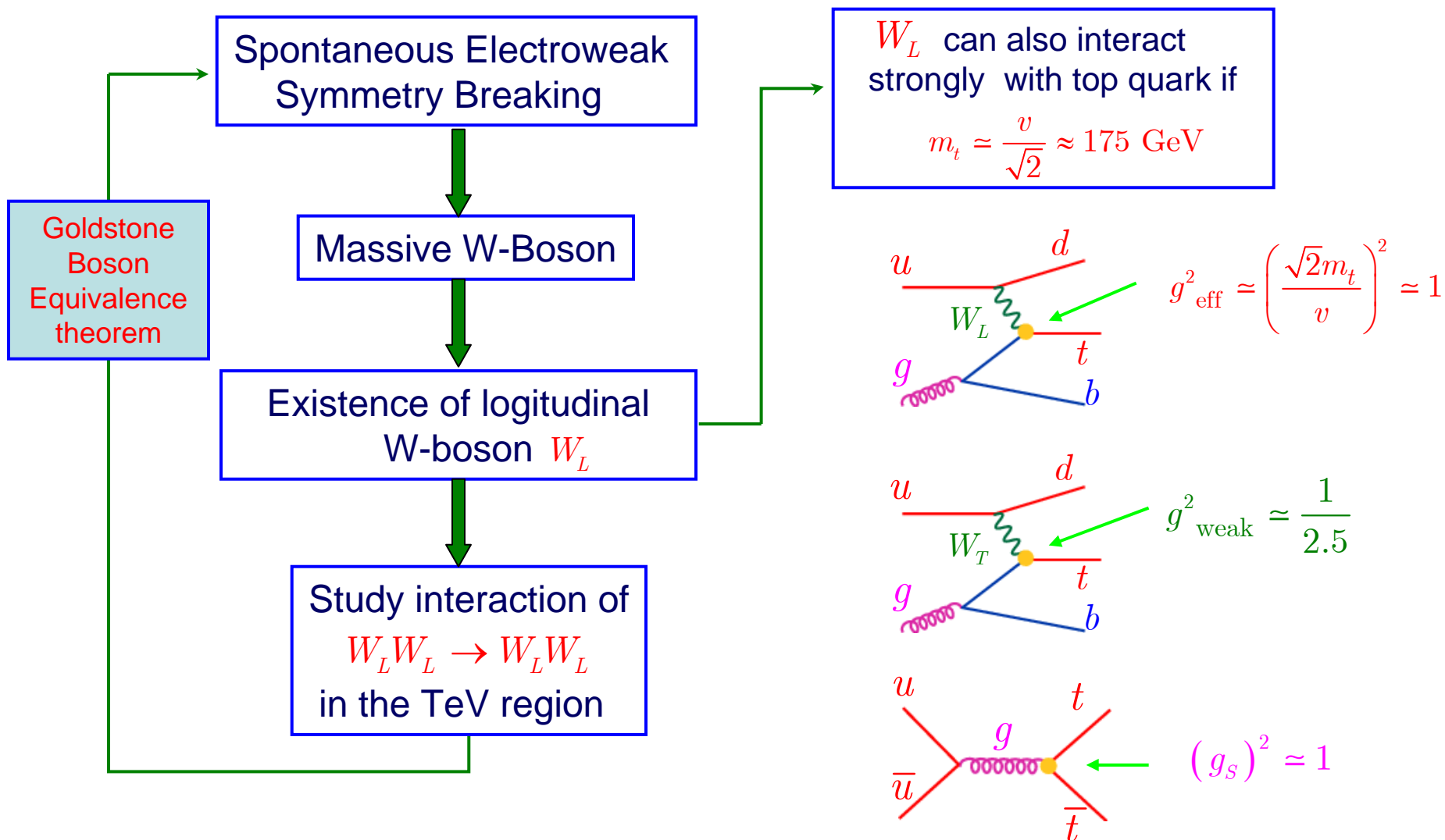
- Only **Experimental Data** has the final say about **Mother Nature**.
- The interaction between **Experimentalists** and **Theorists** is essential for the advance of science.

Theorists should not give up any probable idea.



What motivated my 1990 single-top paper

(with $m_t = 180 \text{ GeV}$)



What motivated my 1990 single-top paper

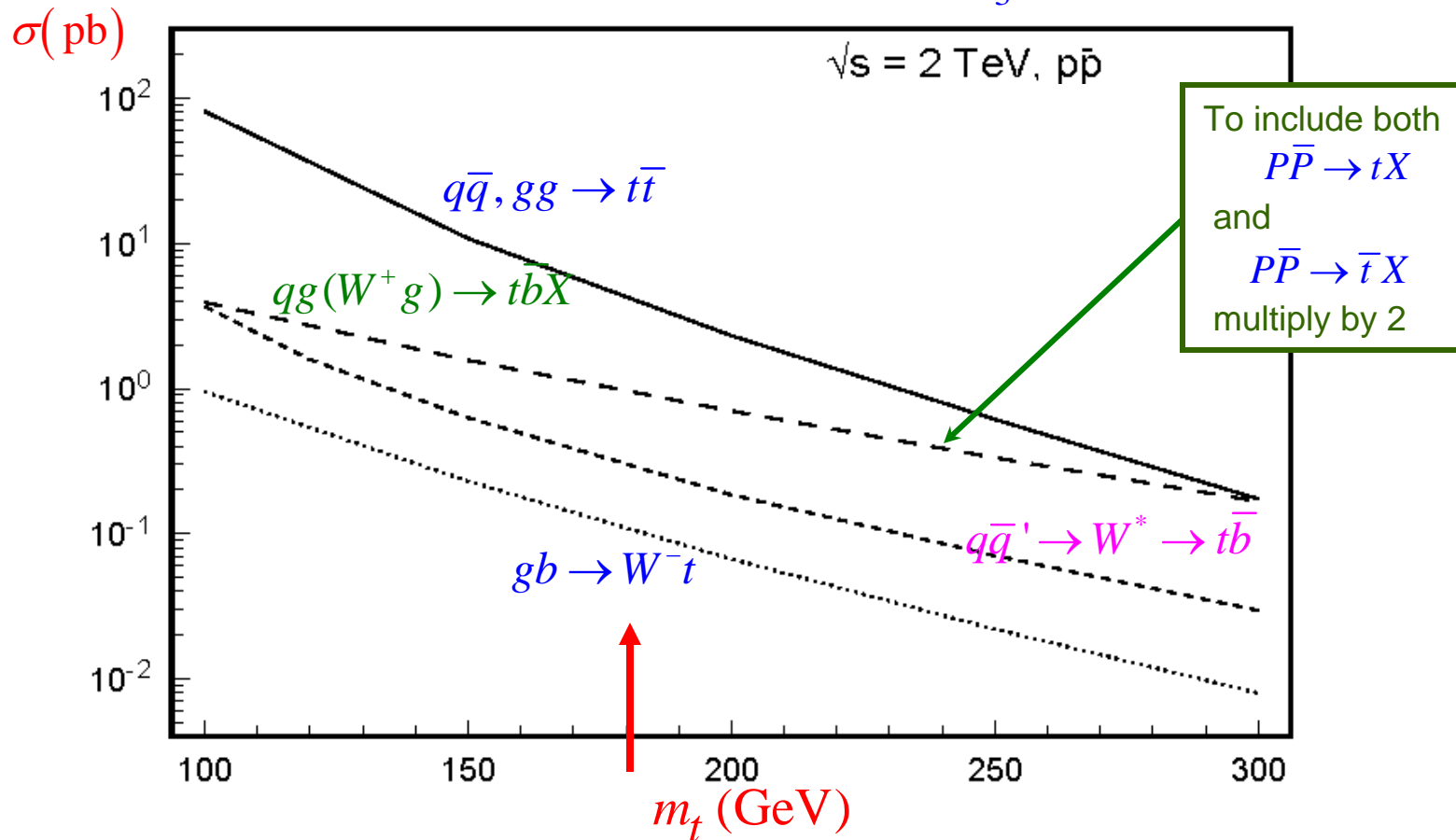
(with $m_t = 180$ GeV)

For $m_t = 180$ GeV,

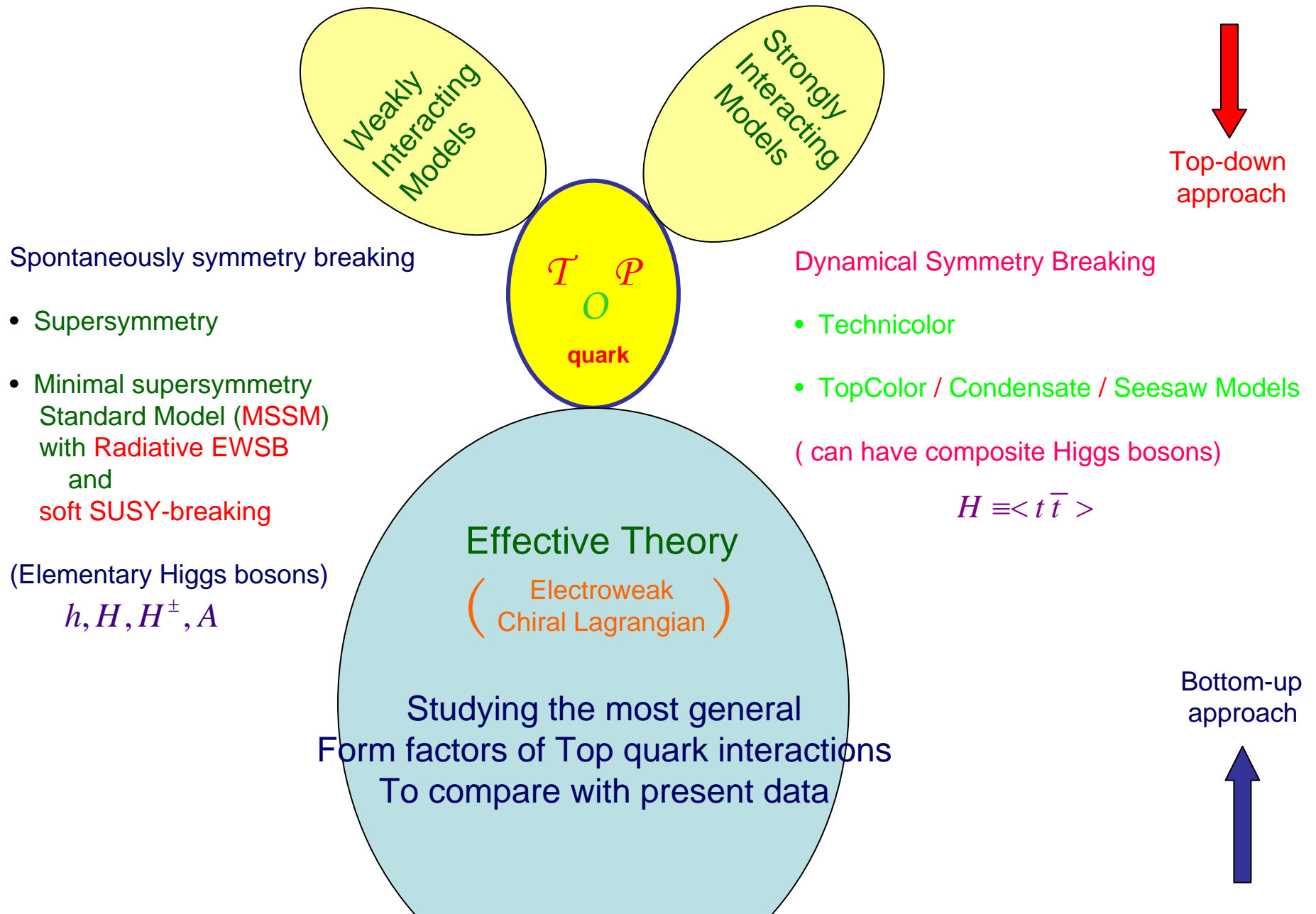
$$\sigma(Wg \rightarrow t\bar{b}, \bar{t}b) \sim \frac{1}{3}\sigma(t\bar{t})$$

$$\sigma(W^* \rightarrow t\bar{b}, \bar{t}b) \sim \frac{1}{3}\sigma(Wg \rightarrow t\bar{b}, \bar{t}b)$$

$$\sigma(Wt) \sim \frac{1}{3}\sigma(W^* \rightarrow t\bar{b})$$



Ideas of Symmetry Breaking (in 4-dim)



Top quark Decay ($m_t > m_W$)

- If the $SU(2)$ structure $\begin{pmatrix} t \\ b \end{pmatrix}_L$ of the Standard Model holds, then $t \rightarrow bW^+$ always occurs at tree level in any model.

➔ $\text{Br}(t \rightarrow bW) \sim 1$

- For a Standard Model t , the decay width $t \rightarrow bW^+$

$$\Gamma_t \sim 1.6 \text{ GeV} \left(\frac{m_t}{180} \right)^3$$

Lifetime

$$\tau_{\text{decay}} = \frac{1}{\Gamma_t} \sim 4.4 \times 10^{-25} \left(\frac{m_t}{180} \right)^3 \text{ sec}$$

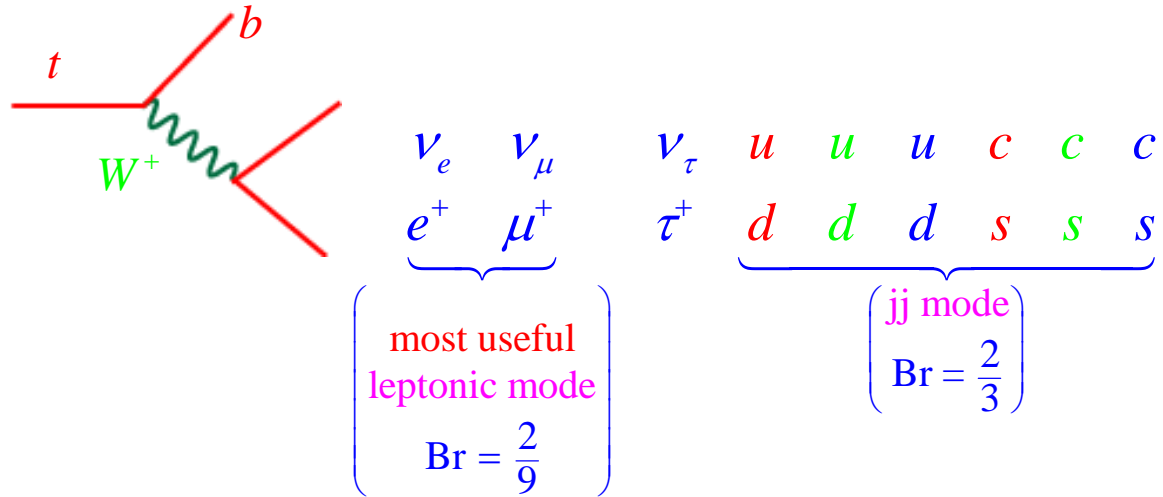
- ➔ t decays before it feels non-perturbative strong interaction.

$$\left(\frac{1}{\Lambda_{\text{QCD}}} \sim \frac{1}{0.2 \text{ GeV}} \sim 3.3 \times 10^{-24} \text{ sec} \right)$$

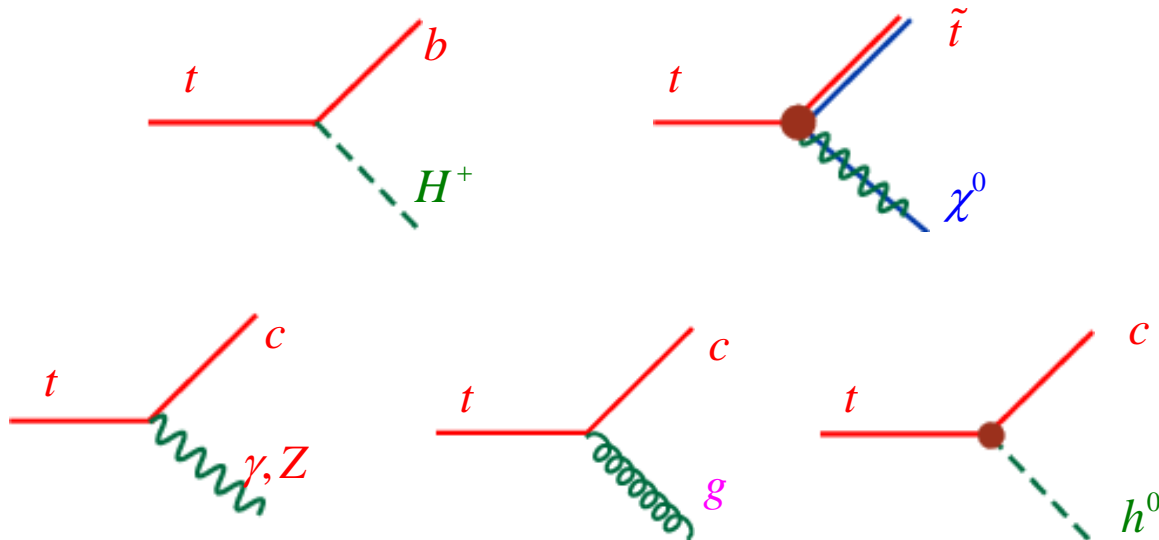
Studying
Property of
Bare quark.

Decay Branching Ratio of Top quark

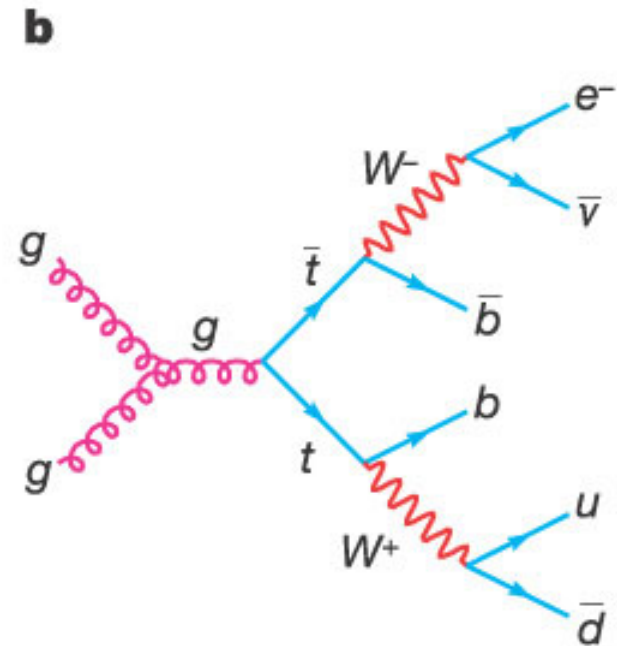
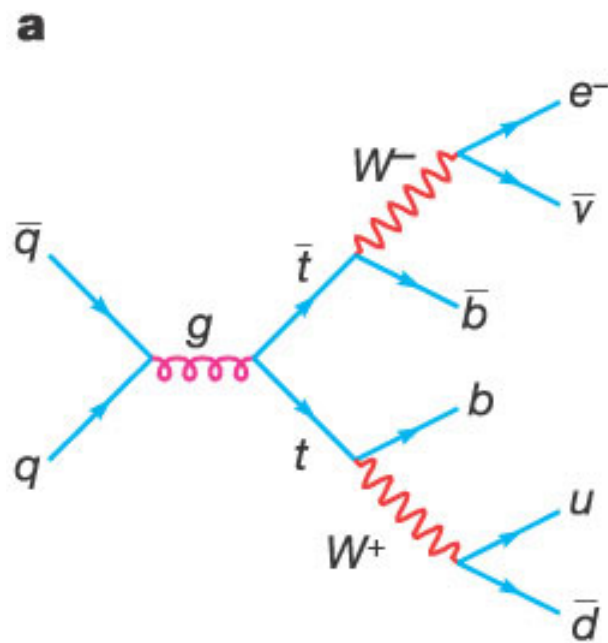
- In the SM:



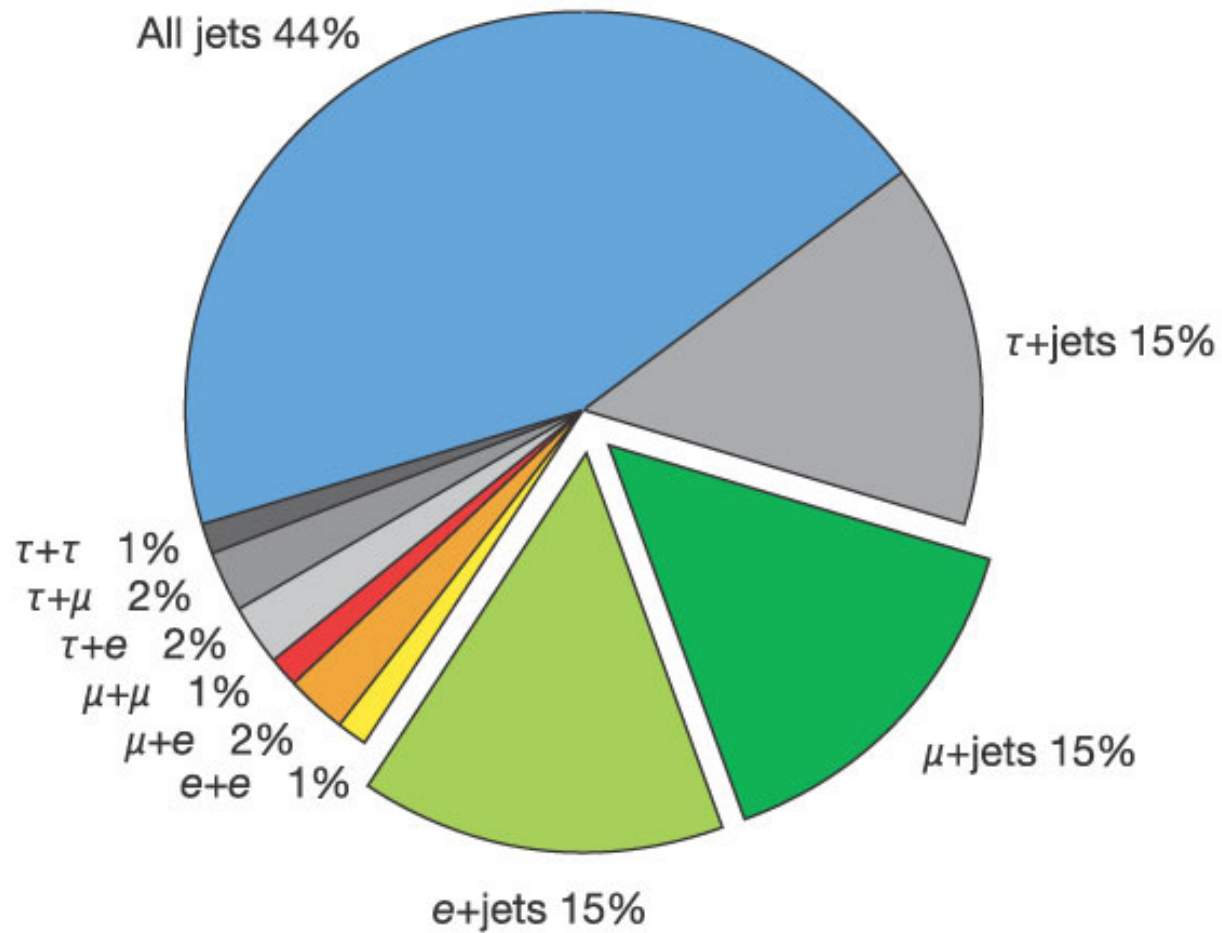
- New Physics:



$t\bar{t}$ Pair Production



Br in $t\bar{t}$ decay modes

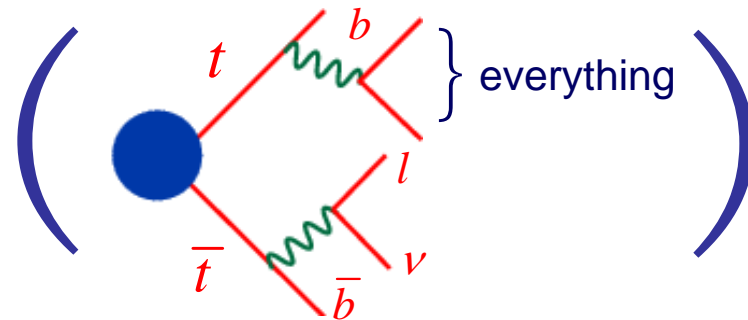
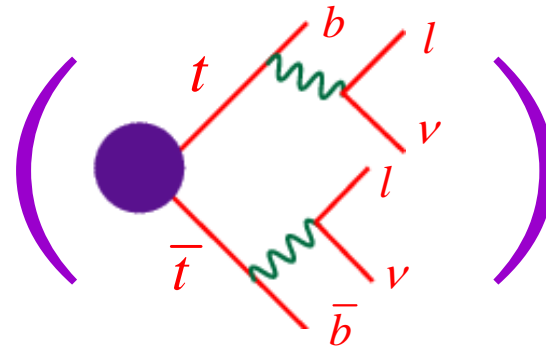


How to measure Branching Ratio (BR) ?

$$t \rightarrow b W^+ \rightarrow l^+ \nu$$

This can be done by measuring the ratio

$$R_l \equiv \frac{Br(t\bar{t} \rightarrow ll + X)}{Br(t\bar{t} \rightarrow l + X)}$$



If $t \rightarrow b H^+$, then

$$\rightarrow j j$$

R_l differs from R_l^{SM} .

What if ... ?

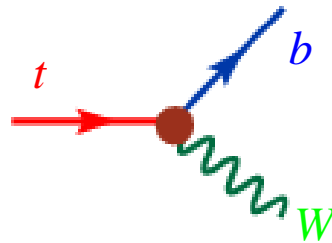
It is however possible that new physics

might not change the $\text{Br}(t \rightarrow bW)$,

(e.g. no additional new light fields
with mass less than m_t)

but will strongly modify the width of $\Gamma(t \rightarrow bW)$,

due to the interaction



is strongly modified.

Hence, the lifetime of top quark is different from **SM's** prediction.

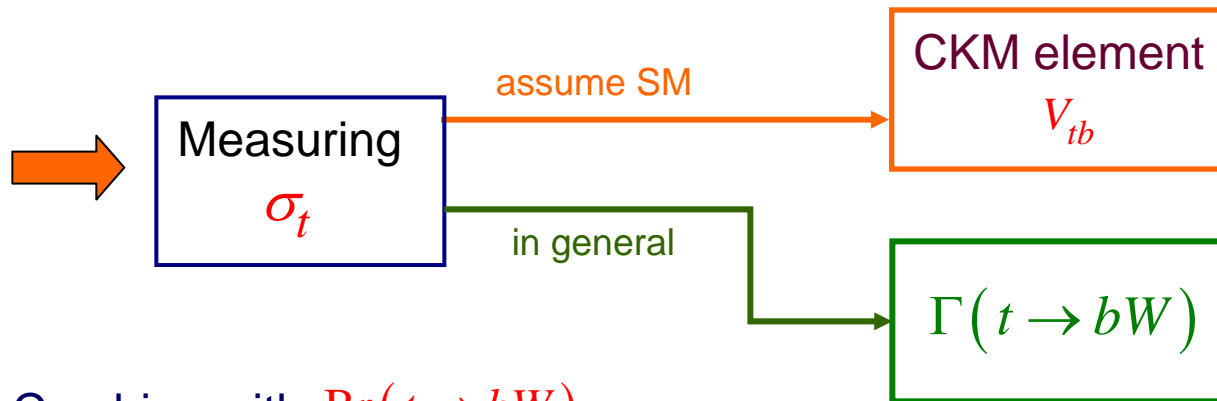
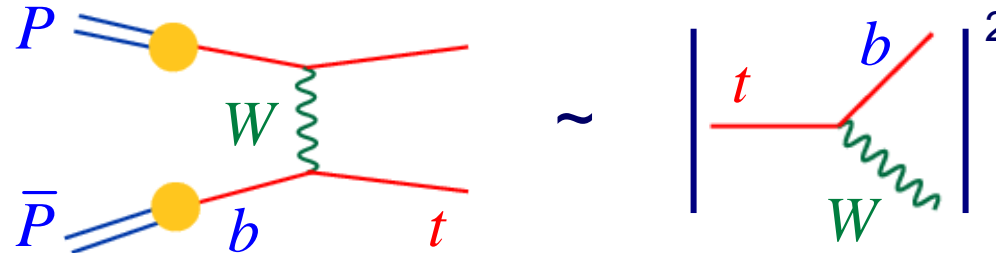


Need to study the interaction of $t-b-W$.

$$P\bar{P} \rightarrow t X \text{ and } P\bar{P} \rightarrow \bar{t} X$$

(single top production)

Since



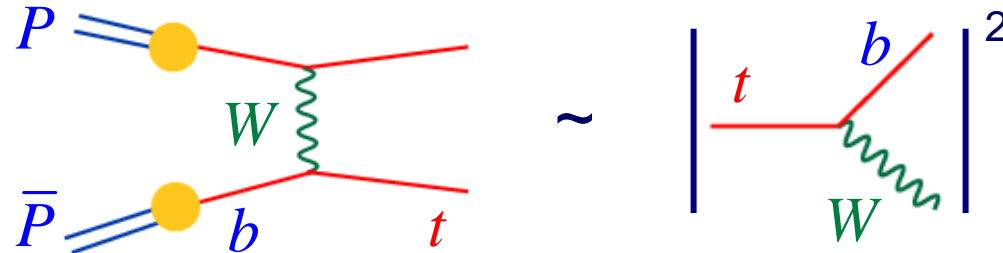
Combine with $\text{Br}(t \rightarrow bW)$

$$\Gamma_{\text{tot}} = \frac{\Gamma(t \rightarrow bW)}{\text{Br}(t \rightarrow bW)} \quad \Rightarrow \quad \text{Lifetime of Top} \quad \tau_{\text{top}} = \frac{1}{\Gamma_{\text{tot}}}$$

$$P\bar{P} \rightarrow t X \text{ and } P\bar{P} \rightarrow \bar{t} X$$

(single top production)

Since



The asymmetry in the production rate

$$A_t^{\text{CPX}} = \frac{\sigma(p\bar{p} \rightarrow t) - \sigma(p\bar{p} \rightarrow \bar{t})}{\sigma(p\bar{p} \rightarrow t) + \sigma(p\bar{p} \rightarrow \bar{t})}$$

can be used to measure CP-violation.

This observable is unique for $p\bar{p}$ collider.
(Tevatron)

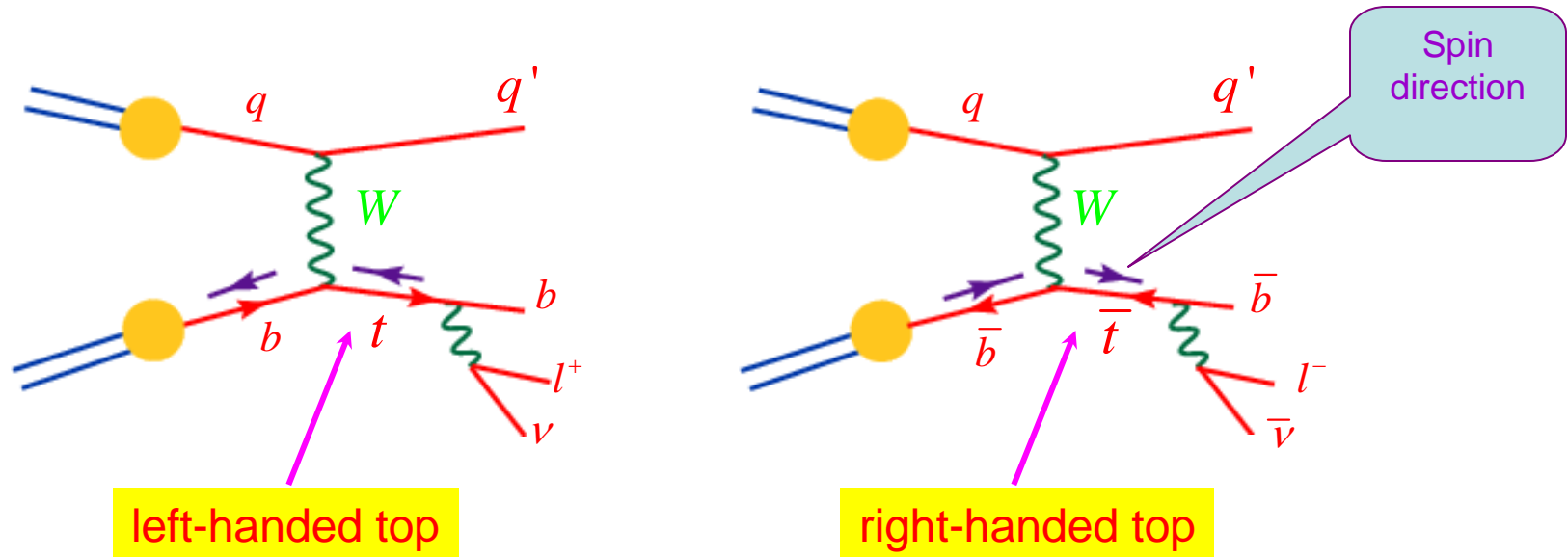
$$C: P \leftrightarrow \bar{P}$$

$$P: \vec{x} \leftrightarrow -\vec{x}$$

For 2 fb^{-1} ,

$$\delta A_t^{\text{CPX}} \sim 20\%$$

A SM t (\bar{t}) is purely
 left-handed (right-handed) polarized
 in the single-top process.



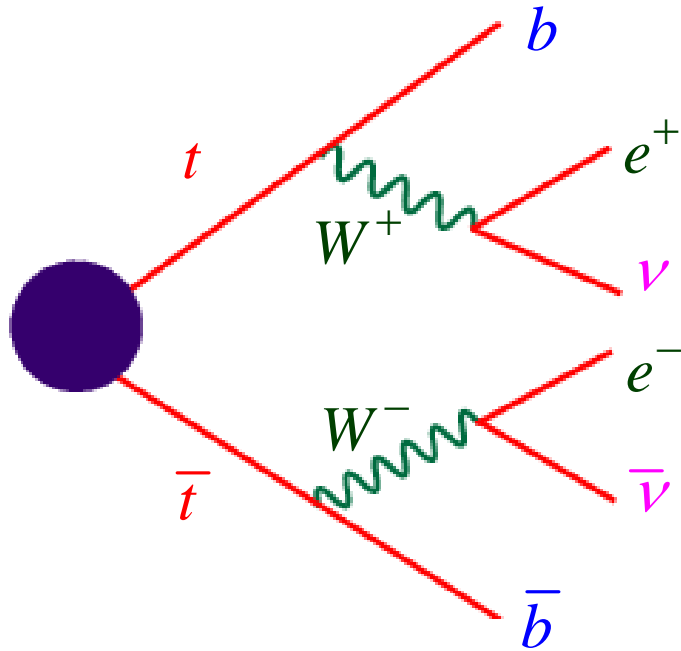
Measuring both

$$\left\langle \vec{\sigma}_t \cdot \vec{p}_b \times \vec{p}_{l^+} \right\rangle \text{ and } \left\langle \vec{\sigma}_{\bar{t}} \cdot \vec{p}_{\bar{b}} \times \vec{p}_{l^-} \right\rangle$$

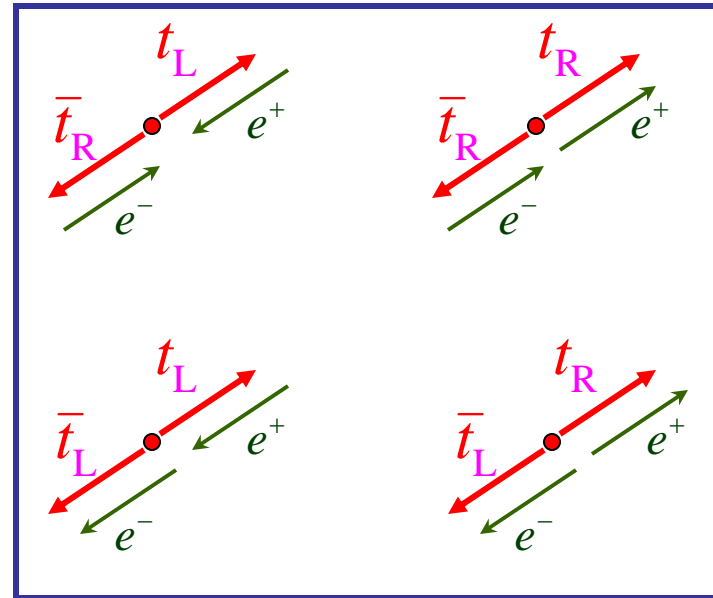


Probe CP-violation at the LHC

Spin correlation in $t\bar{t}$ events



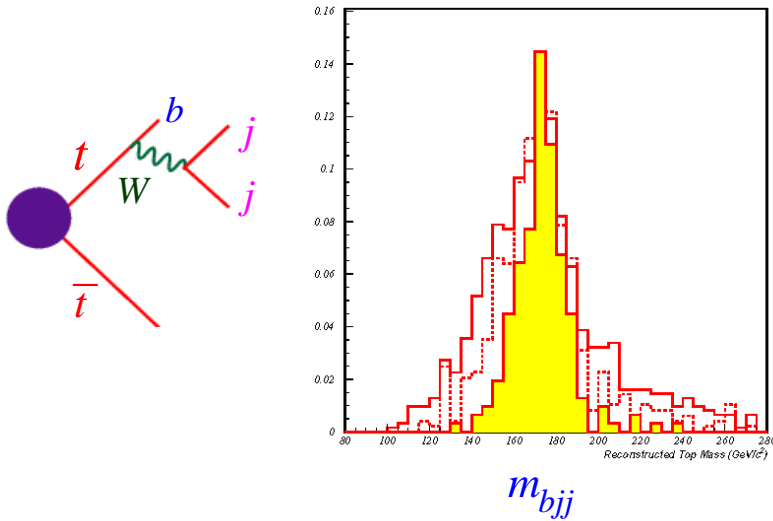
In the $t\bar{t}$ center-of-mass frame



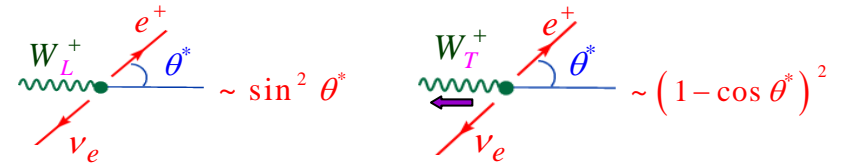
If $\sigma(t_L\bar{t}_L) \neq \sigma(t_R\bar{t}_R)$, then CP is violated.

Need better measurement of m_t

- From the invariant mass of (bjj)



- From the polarization of W

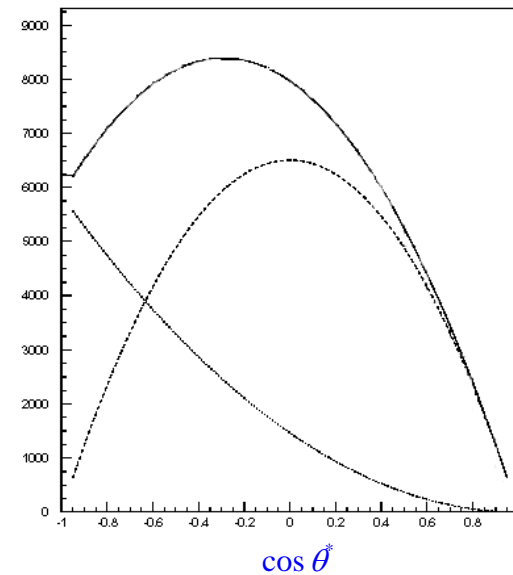
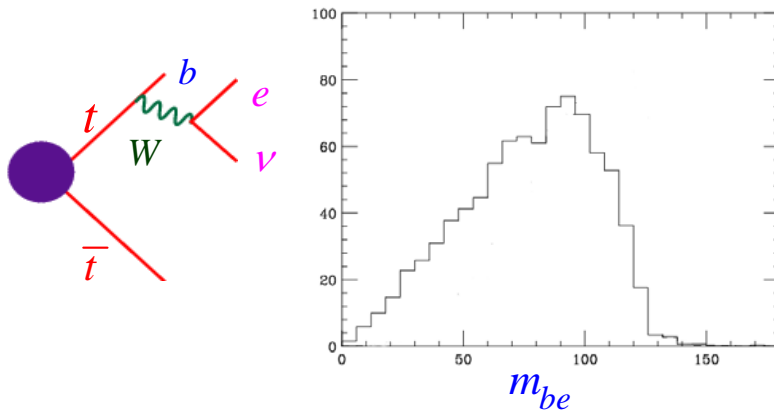


$$F(\cos \theta^*) \sim (1 - f_{\text{Long}}) \left(\frac{1 - \cos \theta^*}{2} \right)^2 + f_{\text{Long}} \left(\frac{\sin \theta^*}{\sqrt{2}} \right)^2$$

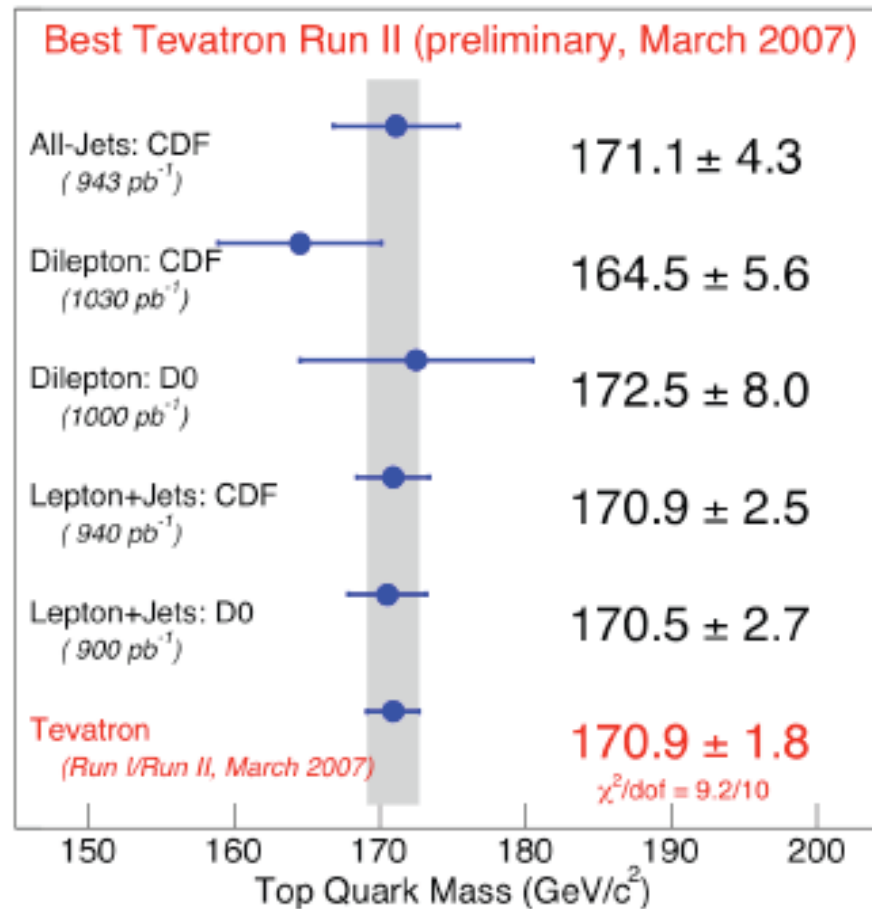
$$f_{\text{long}} = \frac{\Gamma(t \rightarrow bW_L)}{\Gamma(t \rightarrow bW_L) + \Gamma(t \rightarrow bW_T)} = \frac{m_t^2}{2m_W^2 + m_t^2}$$

$$\cos \theta^* = \frac{2m_{be}^2}{m_t^2 - m_W^2} - 1$$

- From the invariant mass of (be)



Top Quark Mass

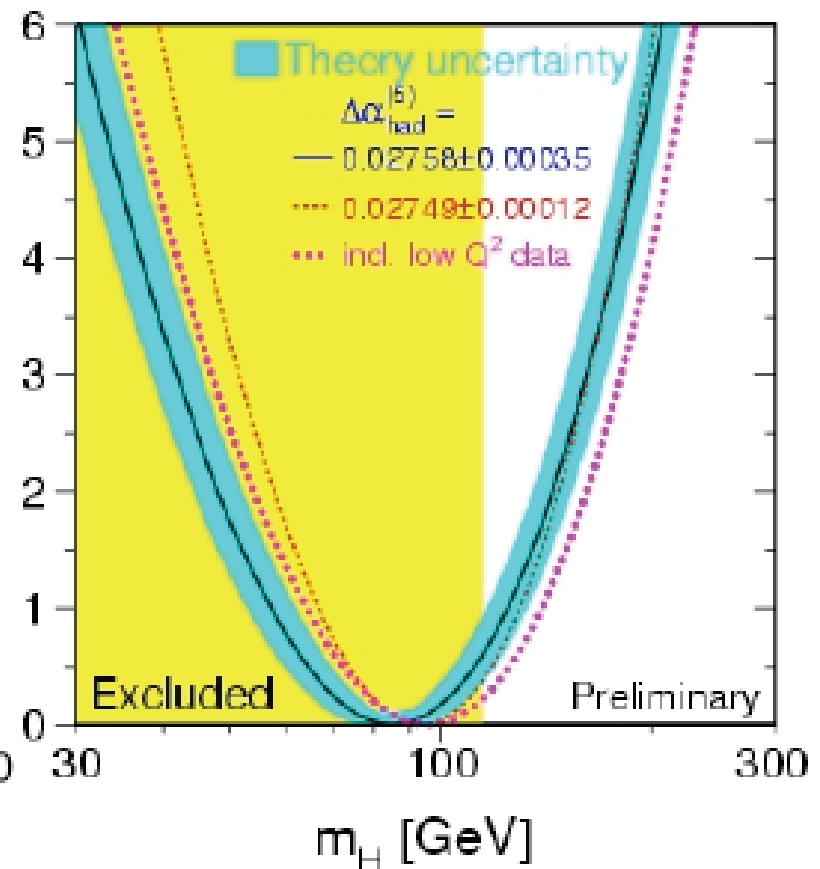
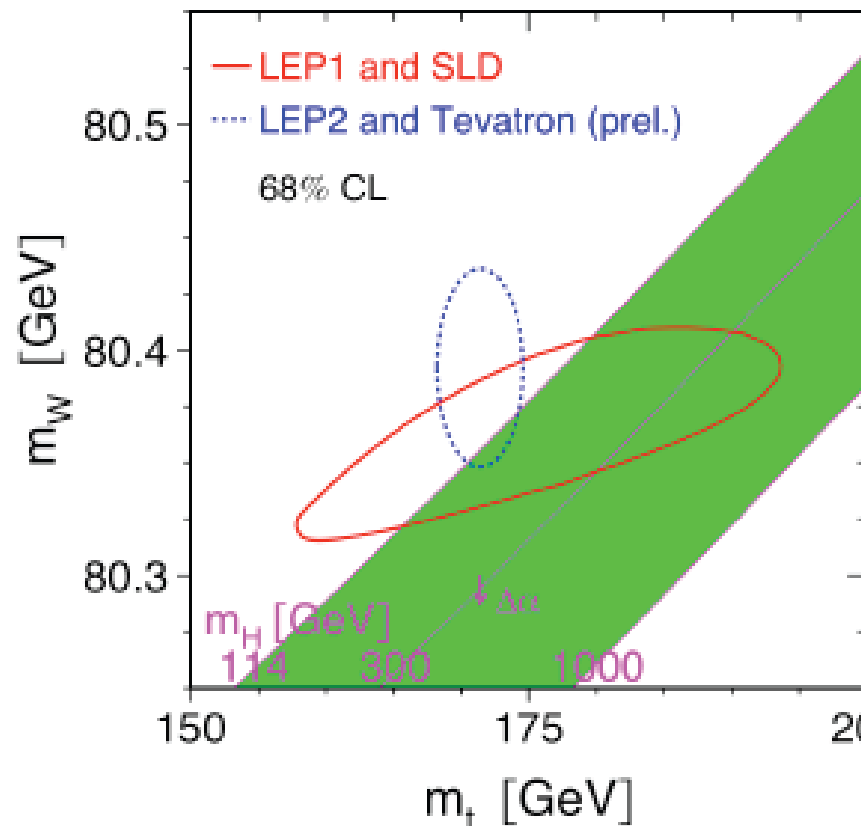


New Tevatron average (3 weeks ago): Top mass now measured to 1.8 GeV

<http://tevewwg.fnal.gov/top>

Impact on Higgs Mass

Before Winter 2007



Predicted Higgs mass from W loop corrections (LEP EWWG):

$m_H = 85^{+39}_{-28}$ GeV (<166 GeV at 95% CL)

direct search from LEP II: $m_H > 114.4$ GeV

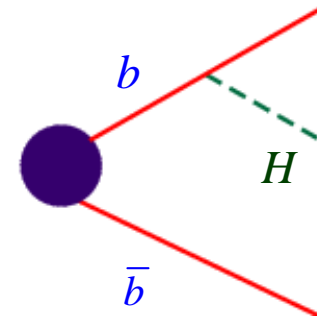
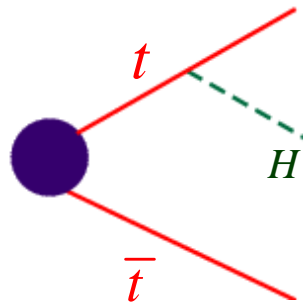
<http://lepewwg.web.cern.ch/LEPEWWG/>

Impact on Higgs Mass

- Summer 2006 SM Higgs fit: (LEP EWWG)
 - $M_H = 85^{+39}_{-28}$ GeV
 - $M_H < 166$ GeV (95% CL)
 - $M_H < 199$ GeV (95% CL) Including LEP II direct exclusion
- Updated preliminary SM Higgs fit: (With new CDF W Mass)
 - $M_H = 80^{+36}_{-26}$ GeV (M. Grünewald, private communication)
 - $M_H < 153$ GeV (95% CL)
 - $M_H < 189$ GeV (95% CL) Including LEP II direct exclusion
- Updated preliminary SM Higgs fit: (With new Tevatron top mass)
 - $M_H = 76^{+33}_{-24}$ GeV
 - $M_H < 144$ GeV (95% CL)
 - $M_H < 182$ GeV (95% CL) Including LEP II direct exclusion

Discriminating Models of Electroweak Symmetry Breaking

Testing the interaction of Top, Bottom and Higgs Boson



SM: $y_t^{\text{SM}} = \frac{m_t}{\sqrt{2}v} = 1$

$y_b^{\text{SM}} = \frac{m_b}{\sqrt{2}v} = \frac{1}{40}$

MSSM:
($\tan \beta = 40$) $y_t = y_t^{\text{SM}} \cdot \cot \beta = \frac{1}{40}$

$y_b = y_b^{\text{SM}} \cdot \tan \beta = 1$

TopColor:
 $H \equiv \langle t \bar{t} \rangle$ $y_t = 1$

$y_b = 1$

If Higgs boson exists

Discovering the Higgs boson and studying its interaction is essential to probe the **electroweak symmetry breaking** and the **flavor symmetry breaking**

Otherwise,

Studying interaction among **longitudinal W and Z bosons** in the **TeV** region and interaction of longitudinal W (Z) boson and **heavy fermions** (top and bottom)

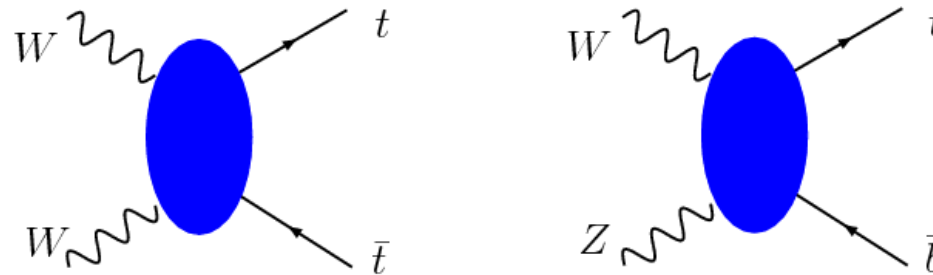
Higgsless Model

(Extra-dimension Models)

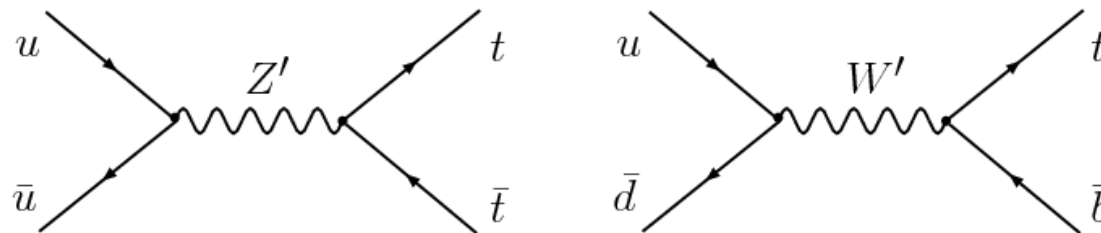
- No elementary or composite Higgs boson to regulate unitarity violation in the TeV region for

$$W W, Z Z \rightarrow W W, Z Z \quad \text{and} \quad W Z \rightarrow W Z$$

- Need to study $W W, Z Z \rightarrow t t$, $W Z \rightarrow t b$ scatterings in the TeV region



- Look for W' and Z' , to delay unitarity breakdown



Summary

We need experimental Data
to advance our knowledge.

Fermilab Tevatron



CERN LHC (Large Hadron Collider)



ILC (International Linear Collider)



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