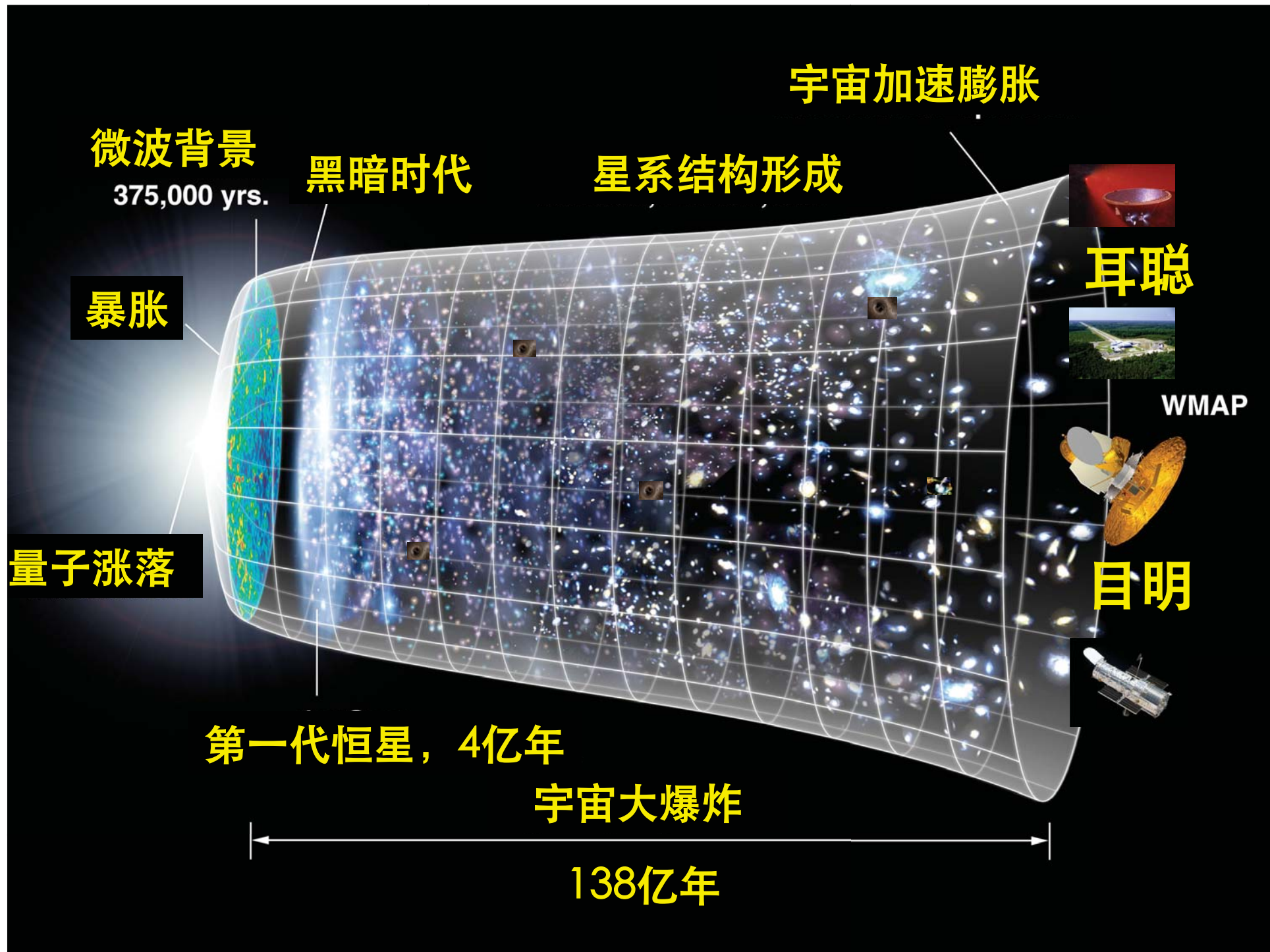


Hearing, seeing, and understanding the universe

Qingjuan Yu (于清娟)

Kavli Institute for Astronomy and Astrophysics,  
Peking University  
December 19, 2019

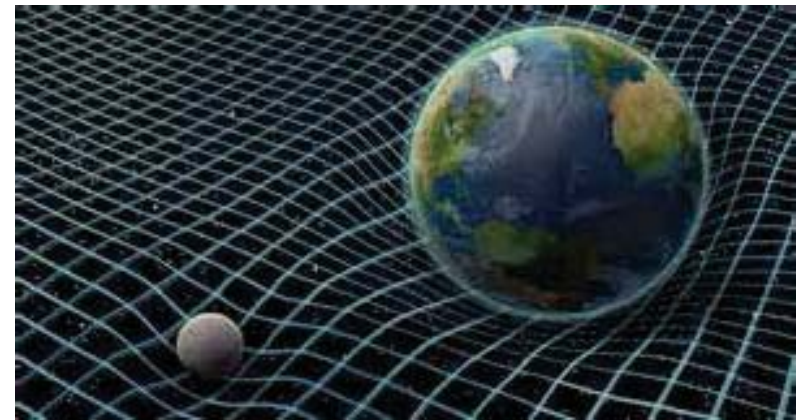


# Outline

- Gravitational waves (GWs)
  - Basics
  - detection
  - significance
- Supermassive binary black holes (BBHs)
  - BHs
    - Stellar-mass BHs
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- Opportunities, Challenge & Summary

# Gravitational Waves

- Waves: sonic waves, electromagnetic waves, seismic waves, gravity waves (fluid mechanics) ... ..
- Gravitational Waves
  - Gravity: Spacetime
    - Static space+time: Newton's gravity
    - Curved spacetime: General relativity
      - Matter/energy distribution  $\rightarrow$  geometry of spacetime
      - Geometry of spacetime  $\rightarrow$  motion
      - Change of matter/energy distribution  $\rightarrow$  change of geometry of spacetime
  - Wave properties
- Quantization? Gravitons?
- **New probes:** Astrophysics



# Spacetime solutions from Einstein's General Relativity

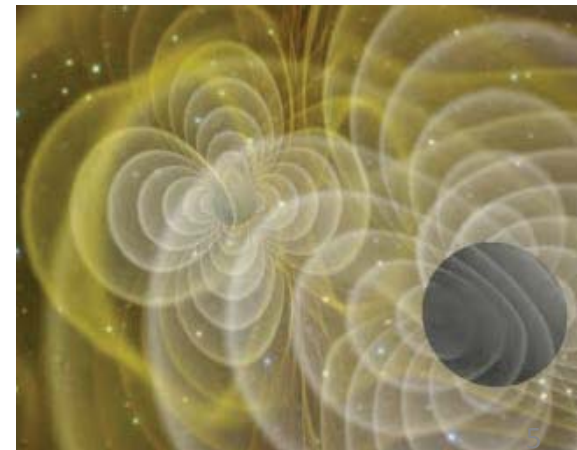
- Einstein field equation
  - Equivalence principle
  - Principle of general covariance

$$G_{\alpha\beta} = \frac{8\pi G}{c^4} T_{\alpha\beta}$$

- Weak field: linearization
  - Metric perturbation: Wave equation

$$-\square \bar{h}_{\alpha\beta} = \frac{16\pi G}{c^4} T_{\alpha\beta} \quad (\text{Lorenz gauge}) \quad \partial \bar{h}^{\mu\alpha} / \partial x^\mu = 0$$

- Strong field: numerical relativity
  - Breakthrough
  - Challenge
- Observations: no contradictions so far.



# Strength

- Mass, size, velocity,  
(non-spherical symmetric) quadrupole
- Strong source:  $v \rightarrow c$ ,  $r \rightarrow GM/c^2$
- Strong sources of astronomical objects:
  - Formation/collapse of compact objects (BHs, neutron stars)
  - Inspiral/merger of compact object binaries
- Extremely weak attenuation (why?)



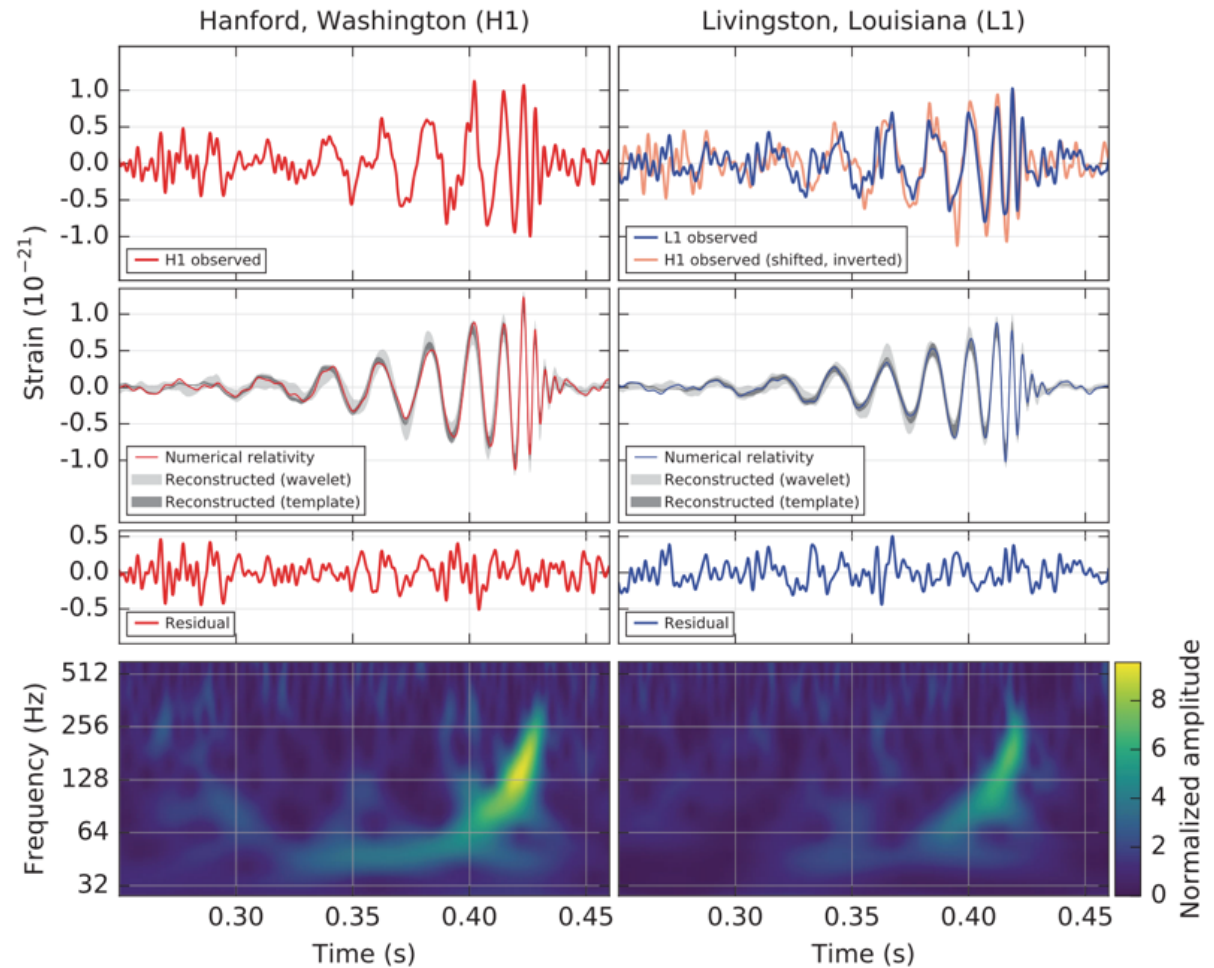
# Gravitational wave direct detection

GW150914

BBH mergers

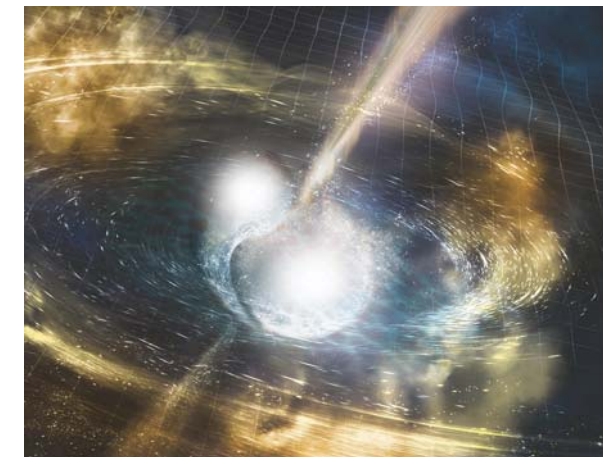
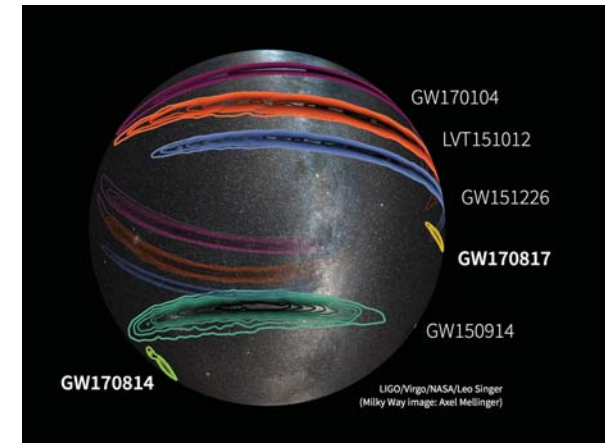
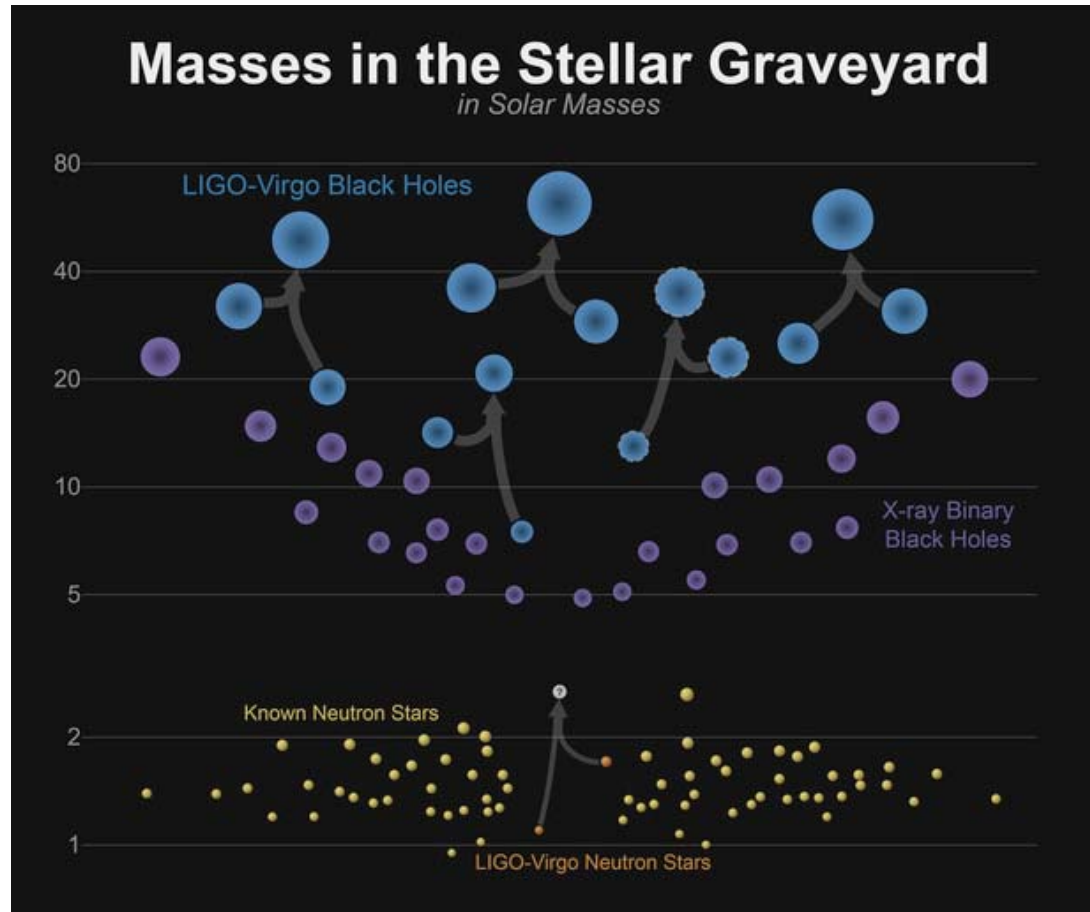


Laser and vacuum equip.



LIGO

(Abbott et al. 2016)



Neutron star mergers

Kilonova/macronova/Li-Paczynski nova

Electromagnetic counterpart





Barry C. Barish (Caltech)



Kip S. Thorne (Caltech)



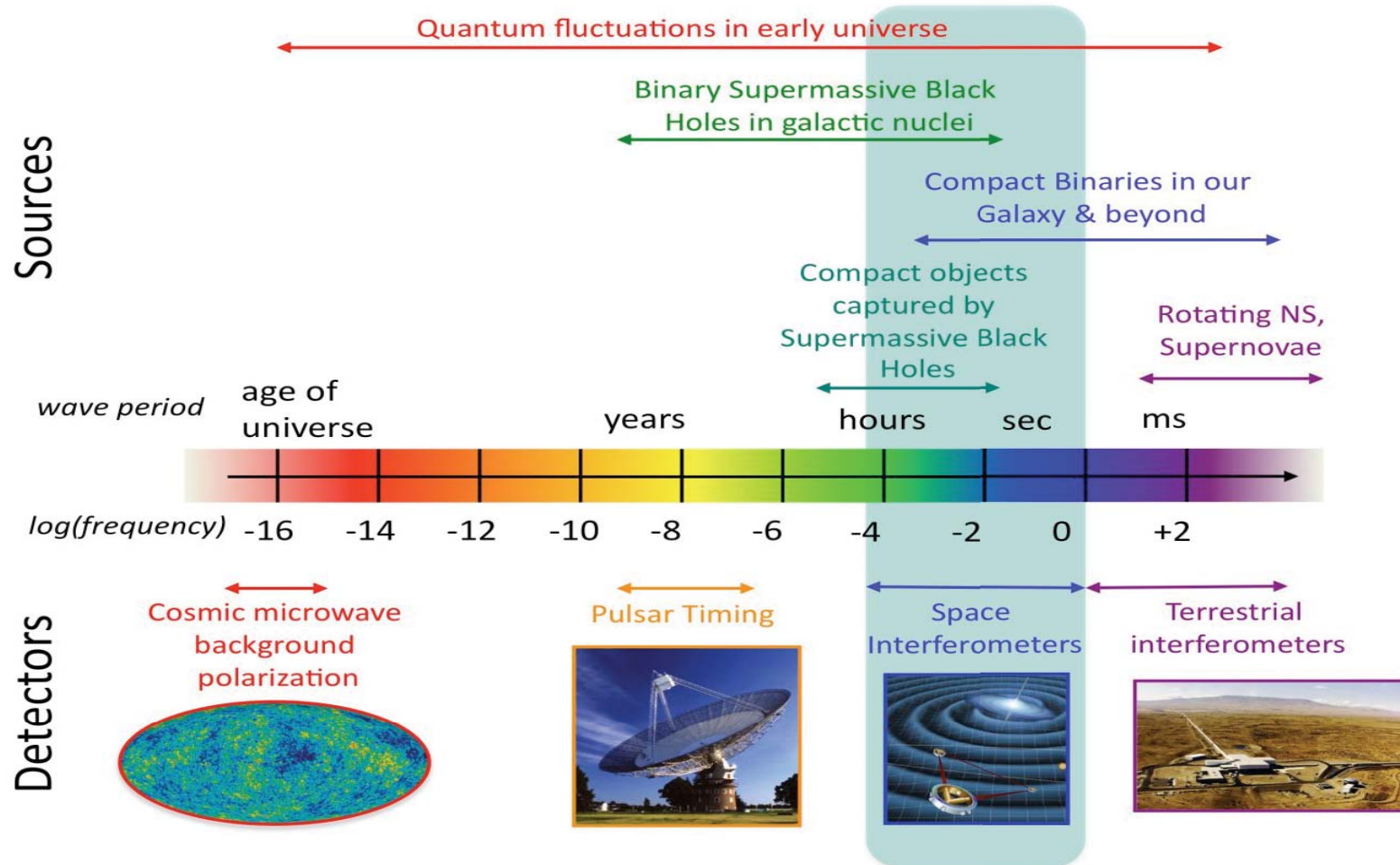
Rainer Weiss (MIT)



## 2017 Nobel Prize in Physics

for decisive contributions to the LIGO detector  
and the observation of gravitational waves

# The Gravitational Wave Spectrum



高频：1-1000Hz；中子双星、双黑洞并合、超新星、脉冲星X射线双星背景；  
 低频：0.001-1Hz，超大质量双黑洞并合，极端质量比旋近，白矮星并合及背景；  
 甚低频： $10^{-9}$ - $10^{-3}$ Hz，超大质量双黑洞旋近，宇宙弦，QCD尺度相变；  
 极低频： $10^{-18}$ - $10^{-15}$ Hz，原初引力波背景及其在微波背景光子上的印迹。

# New/Great Era

Scientific significance of GW studies in astrophysics/  
fundamental physics/cosmology

- Gravity?
- GR? (speed of light, equivalence principle...)
- Formation and evolution of compact objects (BHs, neutron stars)? Mass and spin distributions?
- Equation of states (superdense)
- Hubble constant (cosmological parameter)
- Generation of the universe
- ... ..

# Gravitational wave radiation, supermassive binary black holes, formation and evolution of galaxies and supermassive black holes

Supermassive BBHs, formation and evolution of BHs

- GW radiation at the PTA bands?
- GW radiation at the LISA bands, EMRIs?
- Origin of seed black holes, clues from the LIGO bands?

Galaxy formation and evolution

- Hosts: GW astrophysical sources
- Correlation between supermassive BHs and galaxies
- First galaxies/BHs in the early universe

Both

- Probing the cosmological structure formation and evolution

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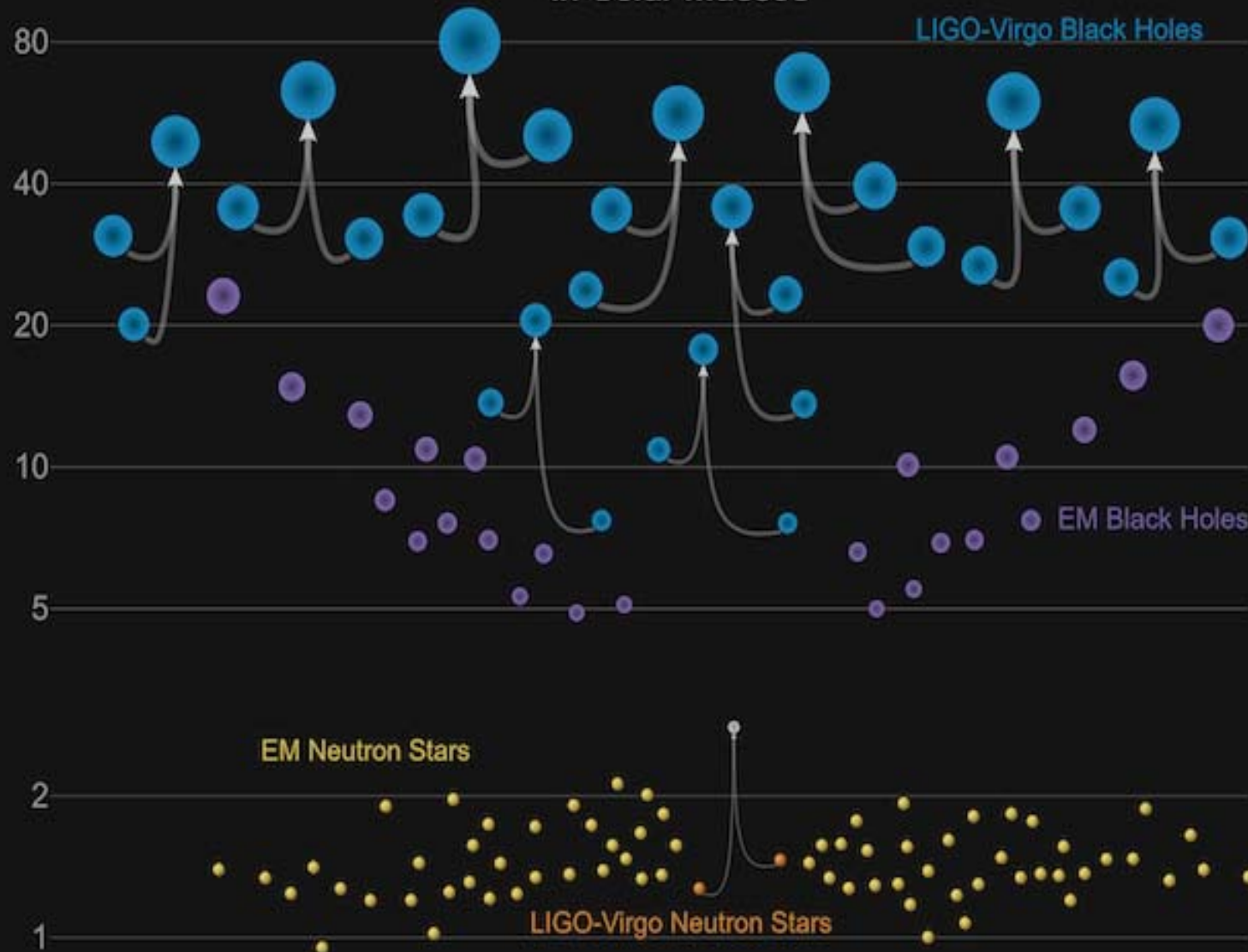
# Black Holes as astronomical objects

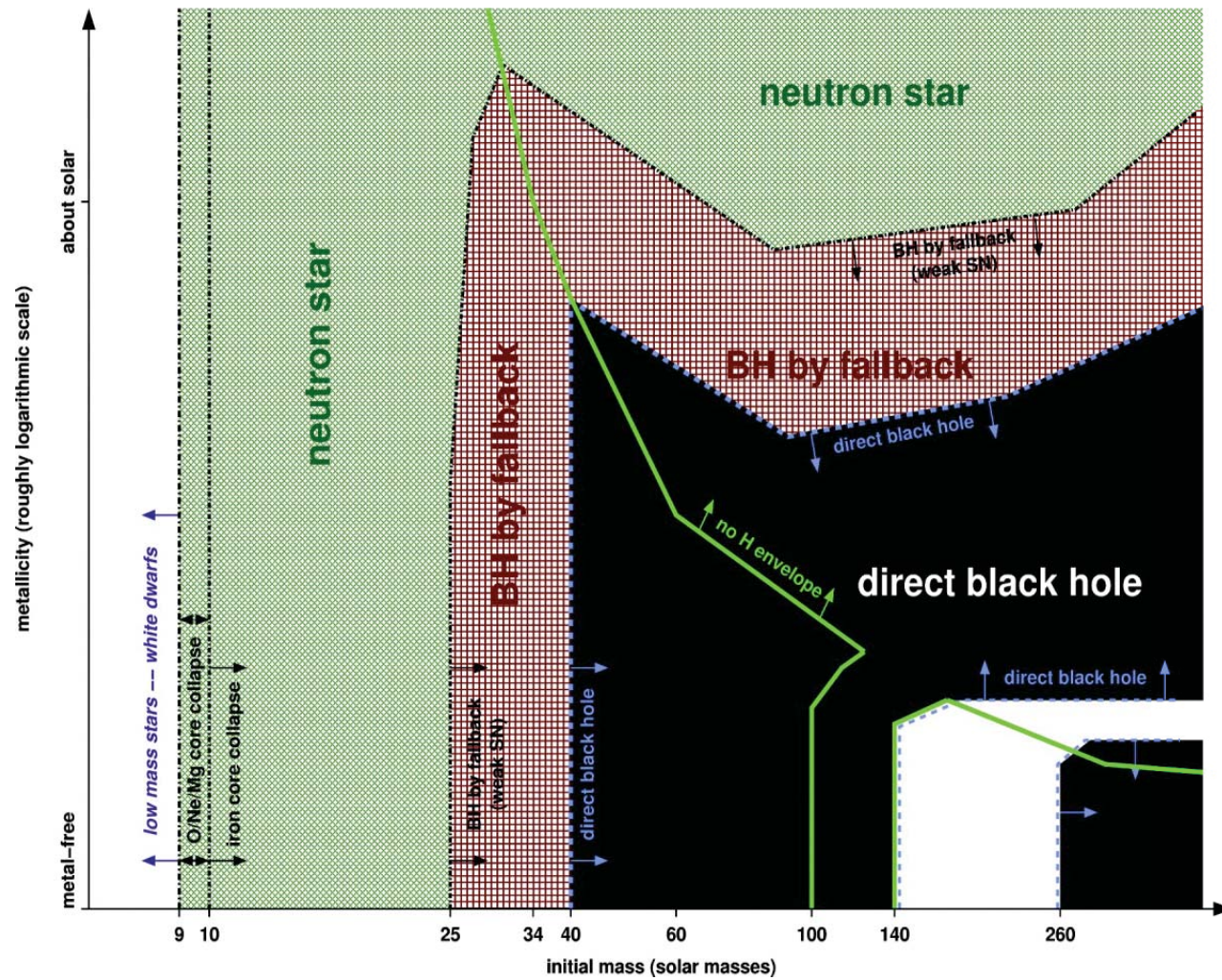
## Classification by mass

- **Stellar-mass BHs:**
  - Observations: several ten solar masses
  - Remnants of stellar evolution, mass limits? (Liu et al. 2019), Mergers?
- Intermediate-mass BHs ( $\sim 10^3$  solar mass)?
- **Supermassive BHs in galactic centers** ( $\sim 10^5$ – $10^{10}$  solar mass)
- Micro-BHs, primordial BHs

# Masses in the Stellar Graveyard

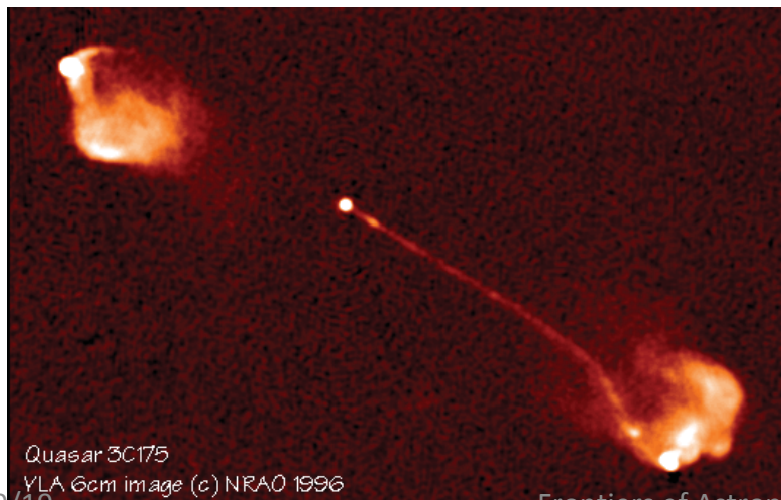
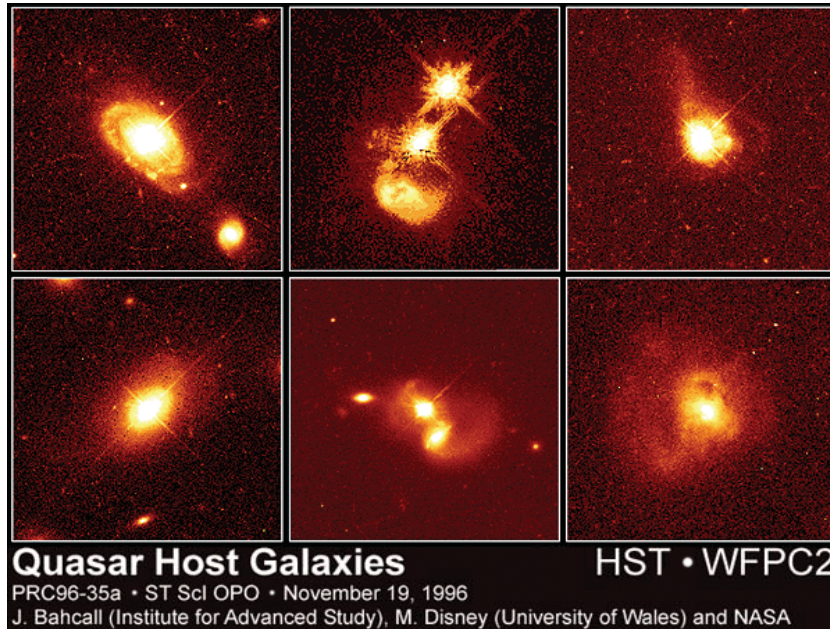
*in Solar Masses*







# QSOs and Active Galactic Nuclei



# Energy generation mechanism

Fundamental question:

How is the energy generated?

- $\sim 10^{42}-10^{48} \text{ erg/s}$  ( $10^9-10^{15} L_{\text{sun}}$ )  
characteristic luminosity of field galaxies:  $\sim 10^{44} \text{ erg/s}$
- Small size (short-term variability):  $\sim c\delta t$  (solar system)

## Accretion onto massive BHs

- **Mass:**

$$F_{\text{grav}} \geq F_{\text{rad}}$$
$$\frac{GMm_p}{r^2} \geq \frac{\sigma_e L}{4\pi cr^2}$$
$$M \geq \frac{\sigma_e L}{4\pi Gcm_p} = 8 \times 10^7 M_{\text{sun}} \left( \frac{L}{10^{46} \text{ erg/s}} \right)$$





# Supermassive BHs in AGNs

- Efficiency:

$$L = \epsilon \dot{M} c^2, \quad \dot{M} \approx \frac{0.2}{\epsilon} \cdot \frac{L}{10^{46} \text{ erg/s}} M_{\text{sun}}/\text{yr}$$

$$\epsilon = 0.007, \text{ nuclear reaction}$$

$$U = \frac{GMm}{r}$$

$$L \approx \frac{dU}{dt} = \frac{GM}{r} \frac{dm}{dt} = \frac{GM\dot{M}}{r},$$

$$\epsilon = \frac{GM}{c^2 r} \sim 0.1 \quad (r \sim 5R_s = 10 \frac{GM}{c^2})$$

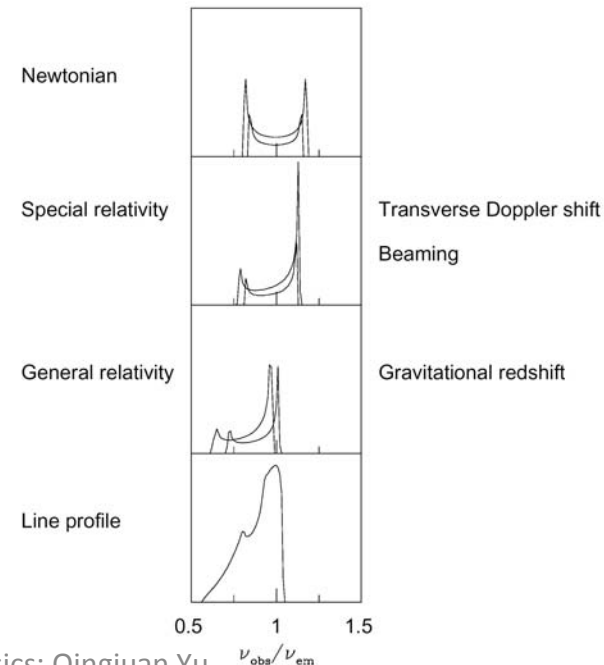
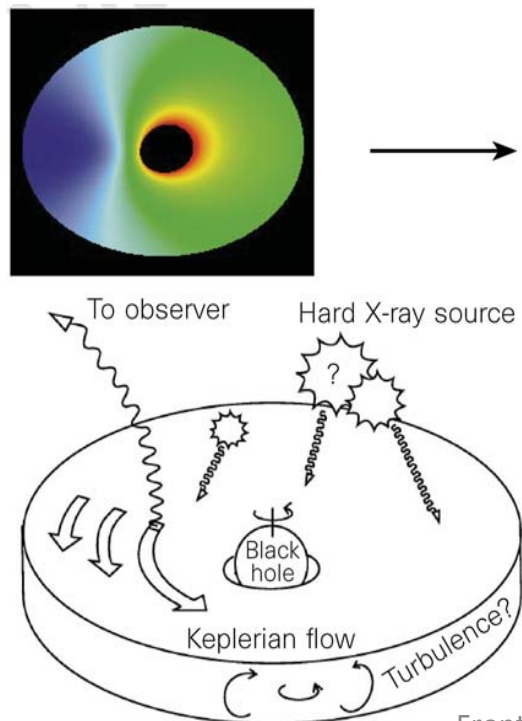
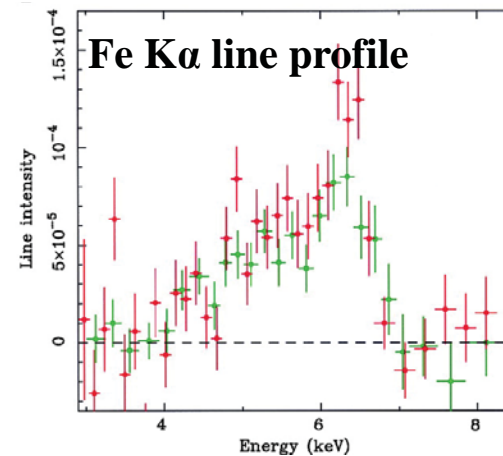
– Schwarzschild BH and Kerr BH: 0.057, 0.31  
( $a=0.998$ )

(Angular momentum: how to lose?)

- Jets:  $\sim c$ , sign of deep potential

## Fe K $\alpha$ emission lines: Strongest lines of evidence for the existence of massive BHs

- Broad and asymmetric (Doppler and gravitational broadening)
- Short-term variability ( $\sim 10^4$ s)
- Emitted from inner disc region





The Prize Winners

The Norwegian Academy of Science and Letters awards  
**THE KAVLI PRIZE IN ASTROPHYSICS 2008**  
to:

**Maarten Schmidt**

Emeritus Professor of Astronomy, California Institute of Technology, USA

and

**Donald Lynden-Bell**

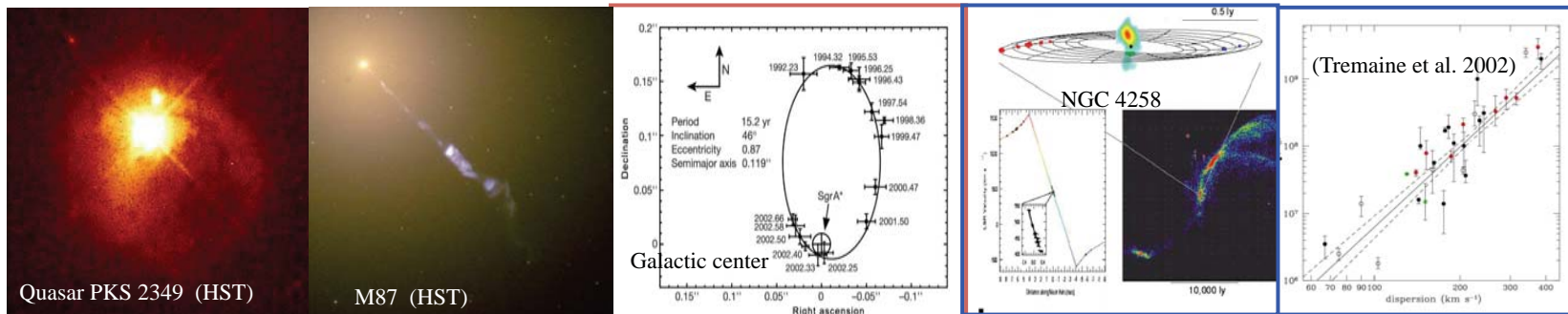
Emeritus Professor, Institute of Astronomy, Cambridge University, UK

"for their seminal contributions to understanding the nature of quasars"



# Existence of massive black holes in galactic centers

- QSOs: powered by accretion onto massive BHs in faraway galaxies (Schmidt 1963; Salpeter 1964; Zel'dovich & Novikov 1964; Lynden-Bell 1969; Rees 1984).
- Faraway galaxies represent history of nearby galaxies (cosmological principle).  
--> QSO remnants in local galaxies?  
(Lynden-Bell 1969; Soltan 1982; Small & Blandford 1992; Yu & Tremaine 2002)
- Nearby galactic centers indeed contain massive dark objects (Kormendy & Richstone 1995; Magorrian et al. 1998; Gebhardt et al. 2002; Pinkney et al. 2003; Ferrarese & Ford 2005).

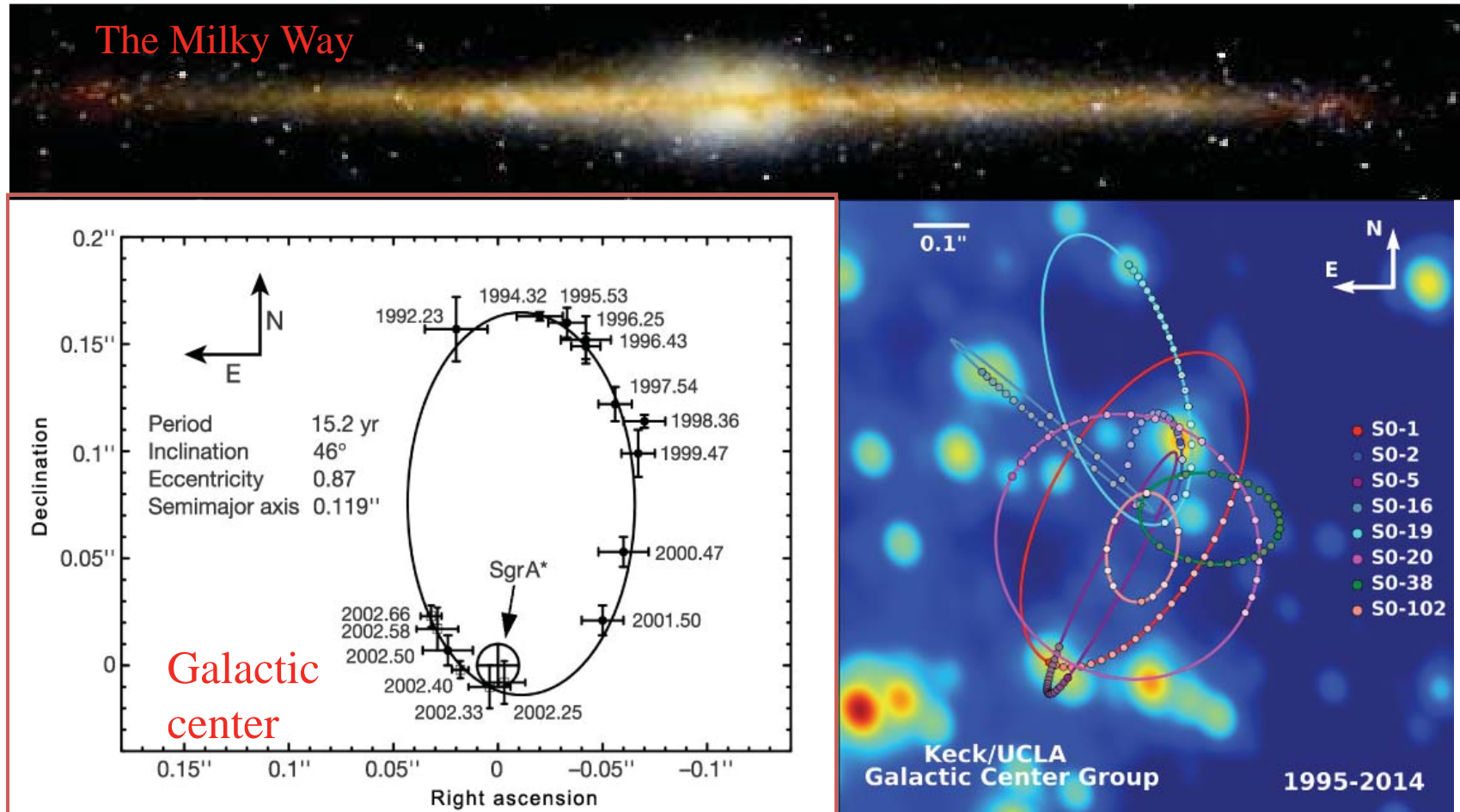


# Toward the *Galactic* center





# Evidence of Massive BHs in Nearby Galaxies



(Reinhard Genzel  
Andrea Ghez)

$$M = rv^2/G$$

$$M_{\text{BH}} = 4 \times 10^6 M_{\text{sun}}$$

## Supermassive BH in the GC: Shaw prize

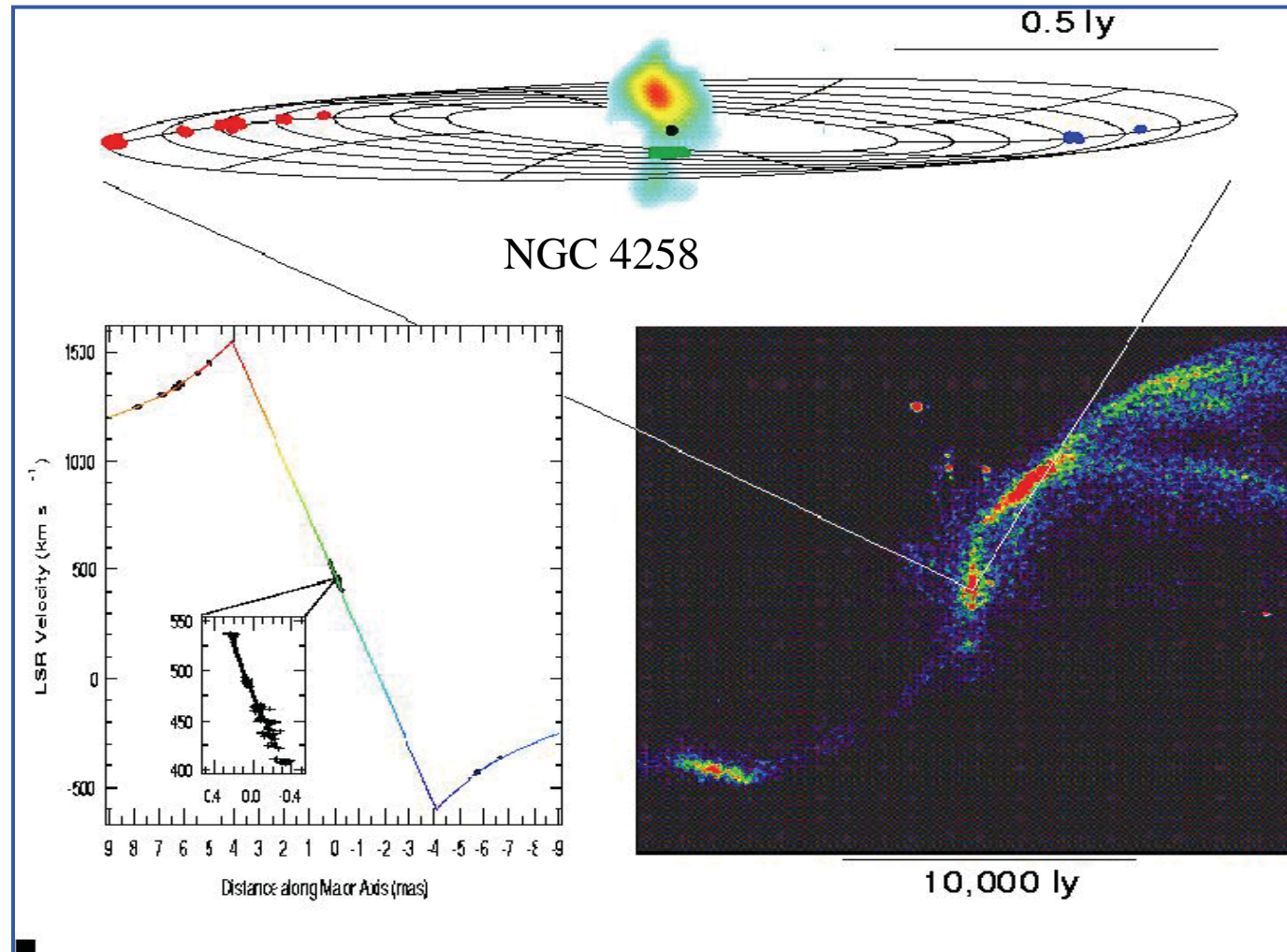


Reinhard Genzel



In recognition of his outstanding contributions in demonstrating that the Milky Way contains a supermassive black hole at its centre.

# Evidence of Massive BHs in Nearby Galaxies



$$M_{\text{BH}} = (3.9 \pm 0.1) \times 10^7 M_{\text{sun}}$$

Frontiers of Astrophysics: Qingjuan Yu

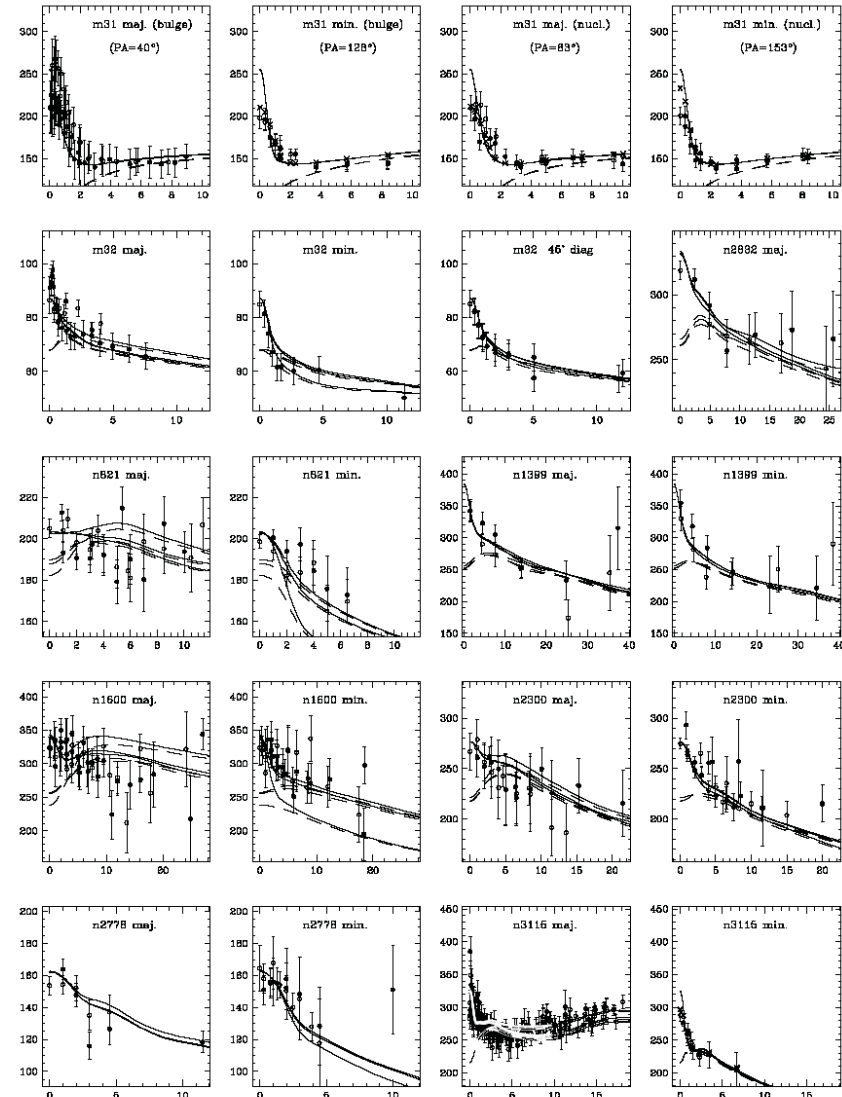
# Evidence of Massive BHs in Nearby Galaxies

- Stellar dynamics

(Magorrian et al. 1998)

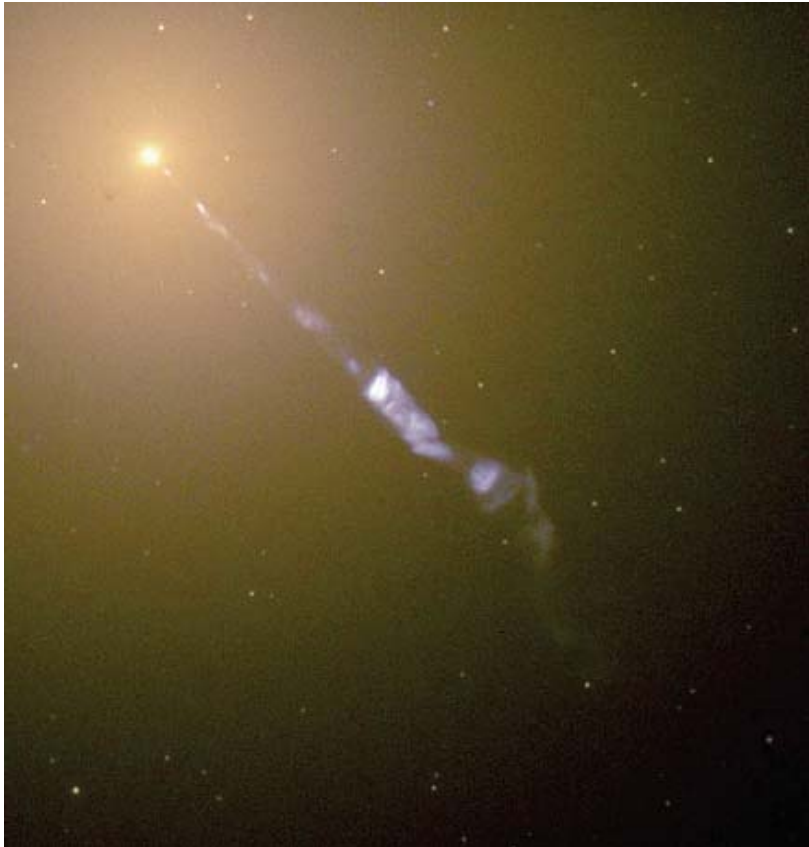
$$M(r) = \frac{V^2 r}{G} + \frac{\sigma_r^2 r}{G} \left[ -\frac{d \ln v}{d \ln r} - \frac{d \ln \sigma_r^2}{d \ln r} - \left( 1 - \frac{\sigma_\theta^2}{\sigma_r^2} \right) - \left( 1 - \frac{\sigma_\phi^2}{\sigma_r^2} \right) \right]$$

$(v^2 + \sigma^2)^{1/2} / (\text{km s}^{-1}) \rightarrow$

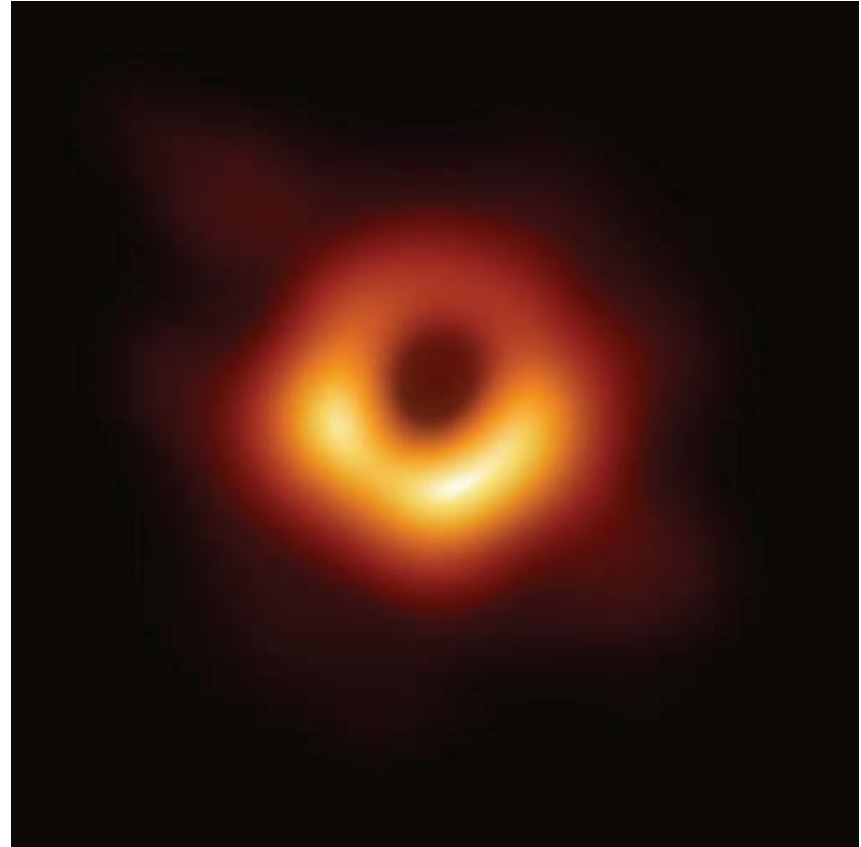




# Seeing the BH in M87



Hubble Space Telescope



Event Horizon Telescope

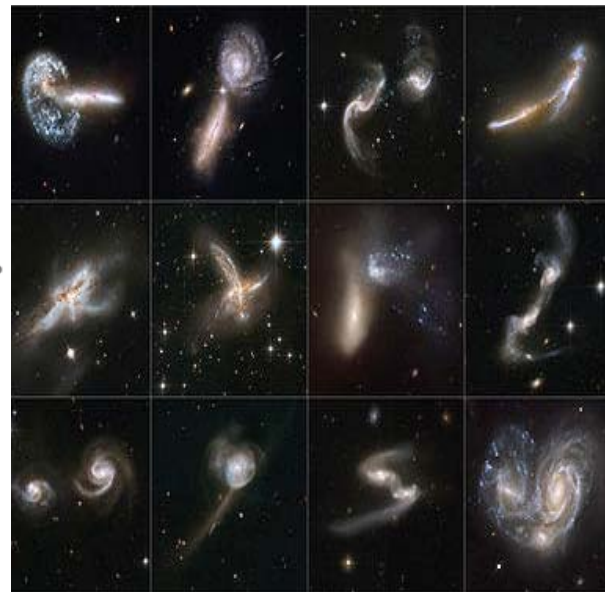
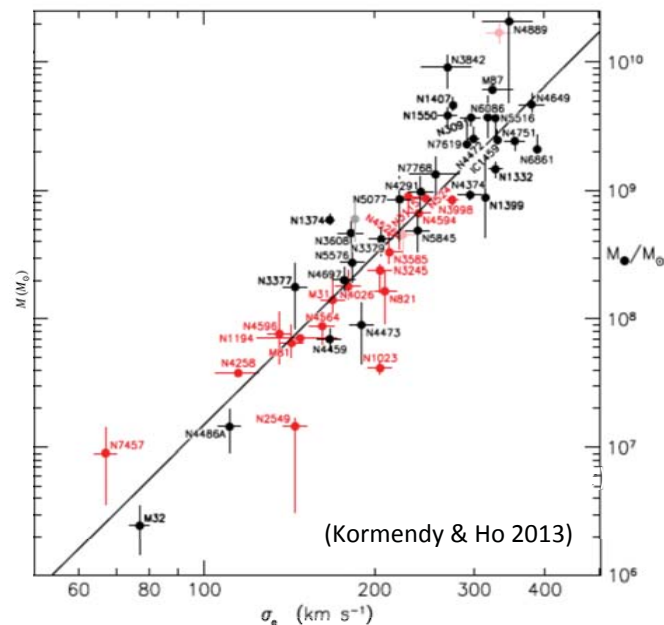


# Outline

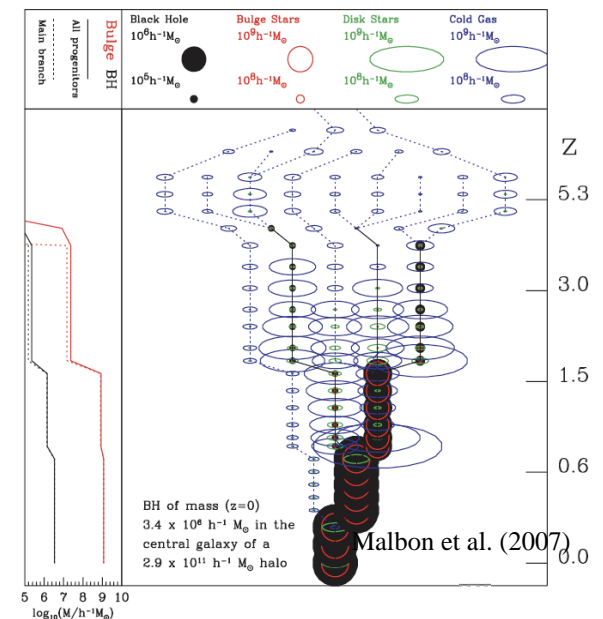
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# Massive BBHs/dual AGNs

- Massive black holes (MBHs) exist in the centers of most, if not all, galaxies.
- Mergers of galaxies play the central role in the hierarchical galaxy formation model, and we do see many galaxies that experienced major mergers.
- Binary/paired MBHs are natural products of mergers of galaxies.
- Mergers of galaxies can drive gaseous material to the very center of the merged galaxies and are believed to be responsible for the AGN/QSO phenomenon.
- Binary/dual/paired AGNs are expected products of the mergers of galaxies.



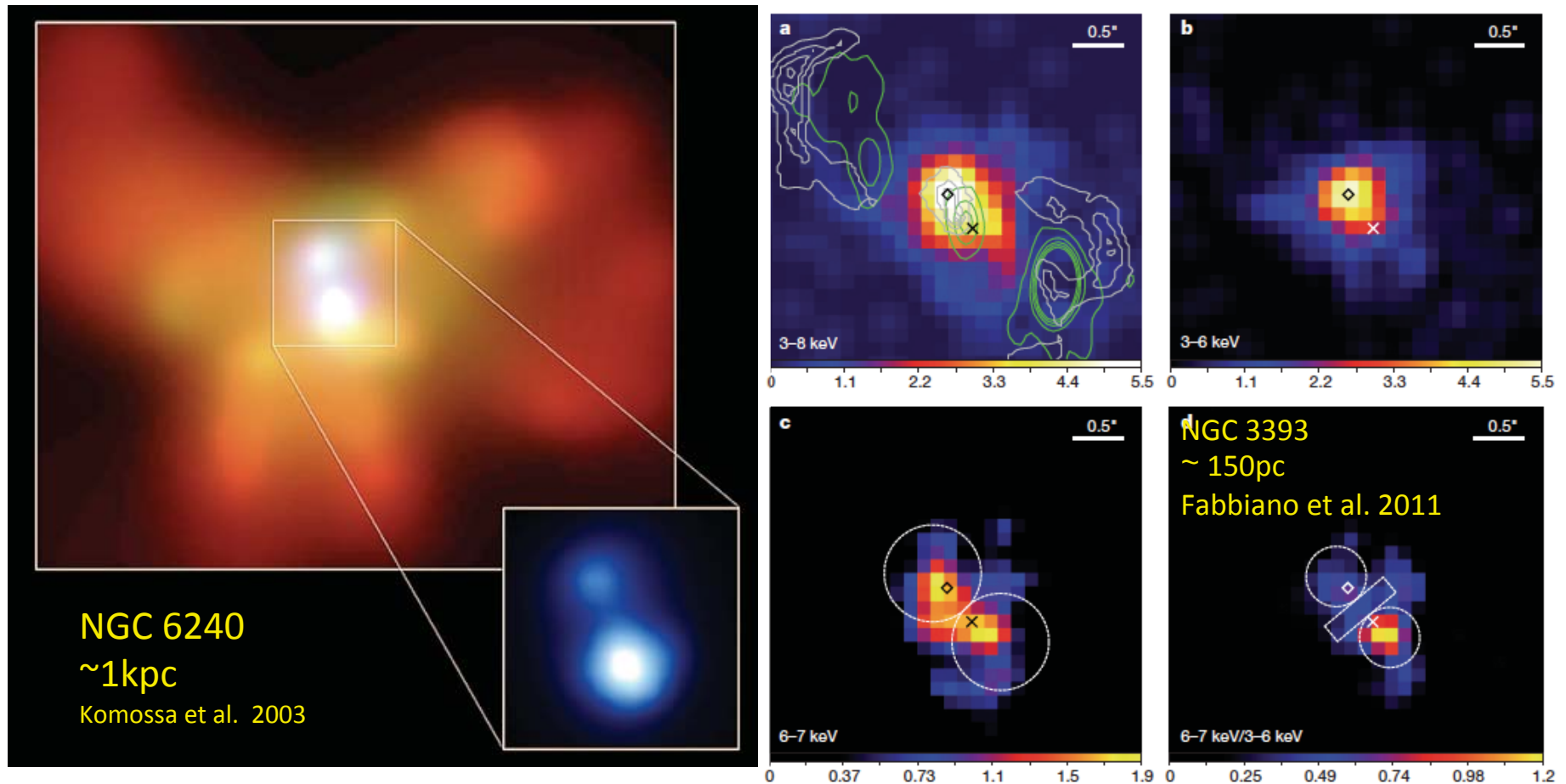
Frontiers of Astrophysics: Qingjuan Yu



Constraining the big pictures / approaching the long-standing questions in astrophysics, cosmology, and fundamental physics:

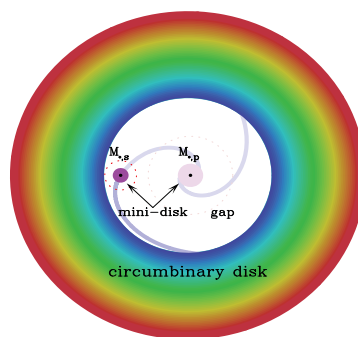
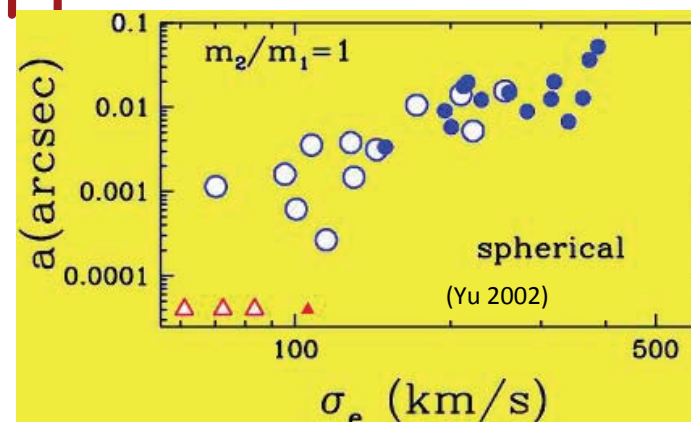
- Hierarchical galaxy and structure formation
- Triggering mechanisms of nuclear activities
- Black hole physics
- Gravitational wave detection, testing gravity theory

# kpc-scale dual AGNs

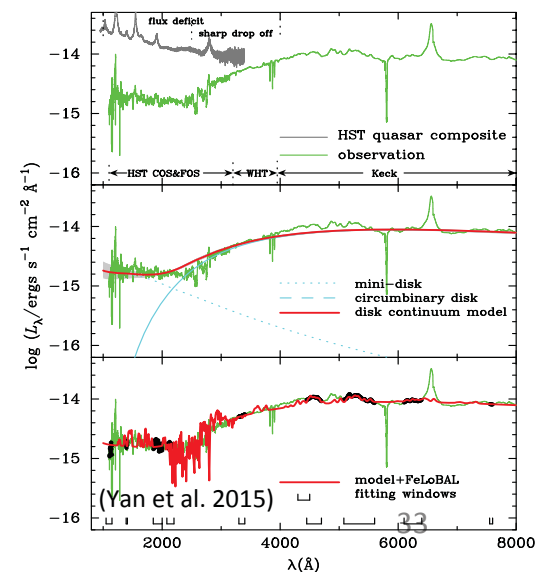
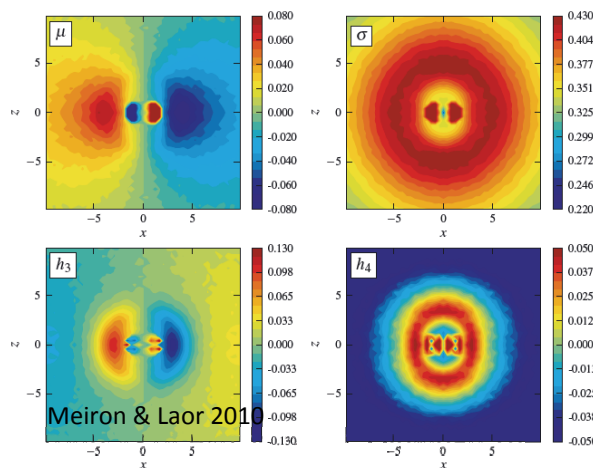
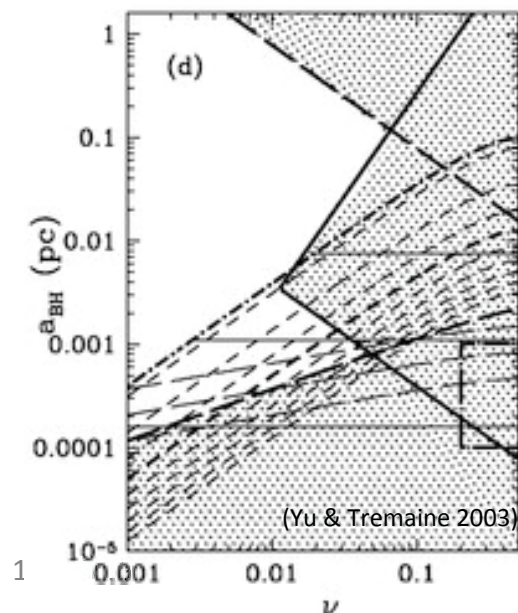


# BBHs: observational appearance?

- Gas-poor mergers
- Gas-rich mergers
- BH companion to Sgr A\* (GC)?

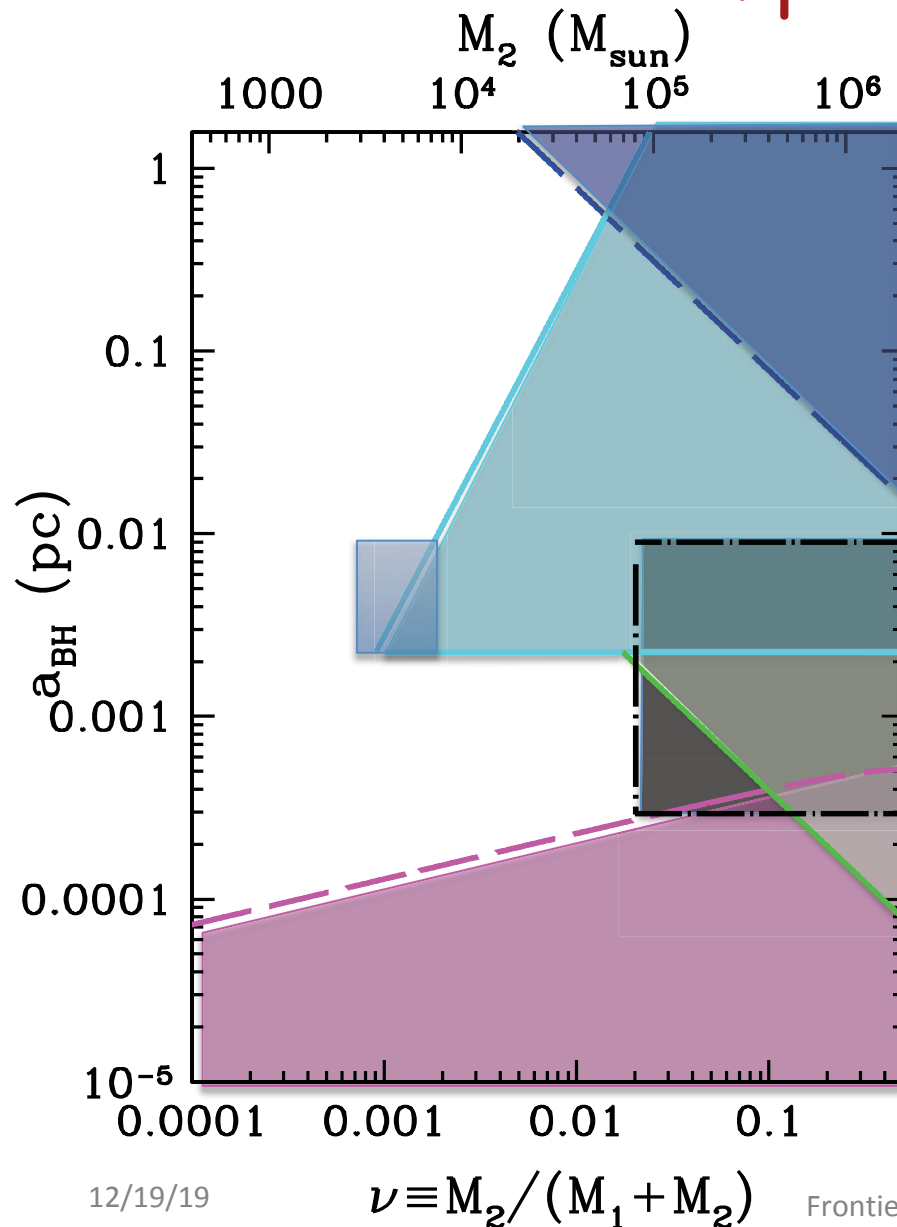


Examples... ..





# A BH companion to Sgr A\*?

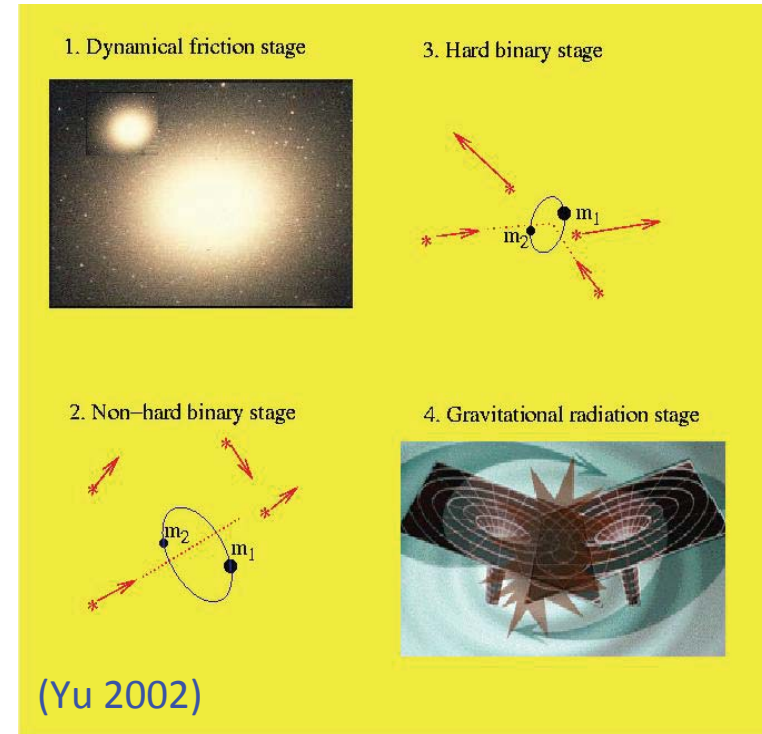


Existence of a BH companion in the Galactic center serves as one of the ways to explain the puzzling existence and distributions of the young stellar disk(s) and S stars, and also hypervelocity stars discovered in the Galactic halo.

- Peak of stellar surface density;
- Gravitational wave radiation;
- Proper motion of Sgr A\*:
  - Upper limit of peculiar motion perpendicular to the Galactic plane;
  - Position residual from motion;
- Eccentric Keplerian orbits of S stars at radii  $r \sim 0.1\text{--}1\text{ mpc}$  around a point mass;
- Long-term perturbations ( $10^7\text{ yr}$ ) on the inclination and eccentricity distributions of S stars due to an IMBH;

# Orbital evolution of massive BBHs: gas-poor mergers

- Dynamical friction stage (several ten kpc down to ten pc or pc scale)
- Gravitationally bound BBHs
  - Non-hard binary stage (10 pc or pc-scale):
    - three-body interactions with stars
    - dynamical friction
  - Hard-binary stage (pc or sub-pc scale)
    - three-body interactions with stars
    - depending on galaxy shapes and galaxy properties
- Gravitational wave radiation stage ( $< \sim 10^{-2}$  pc scale)



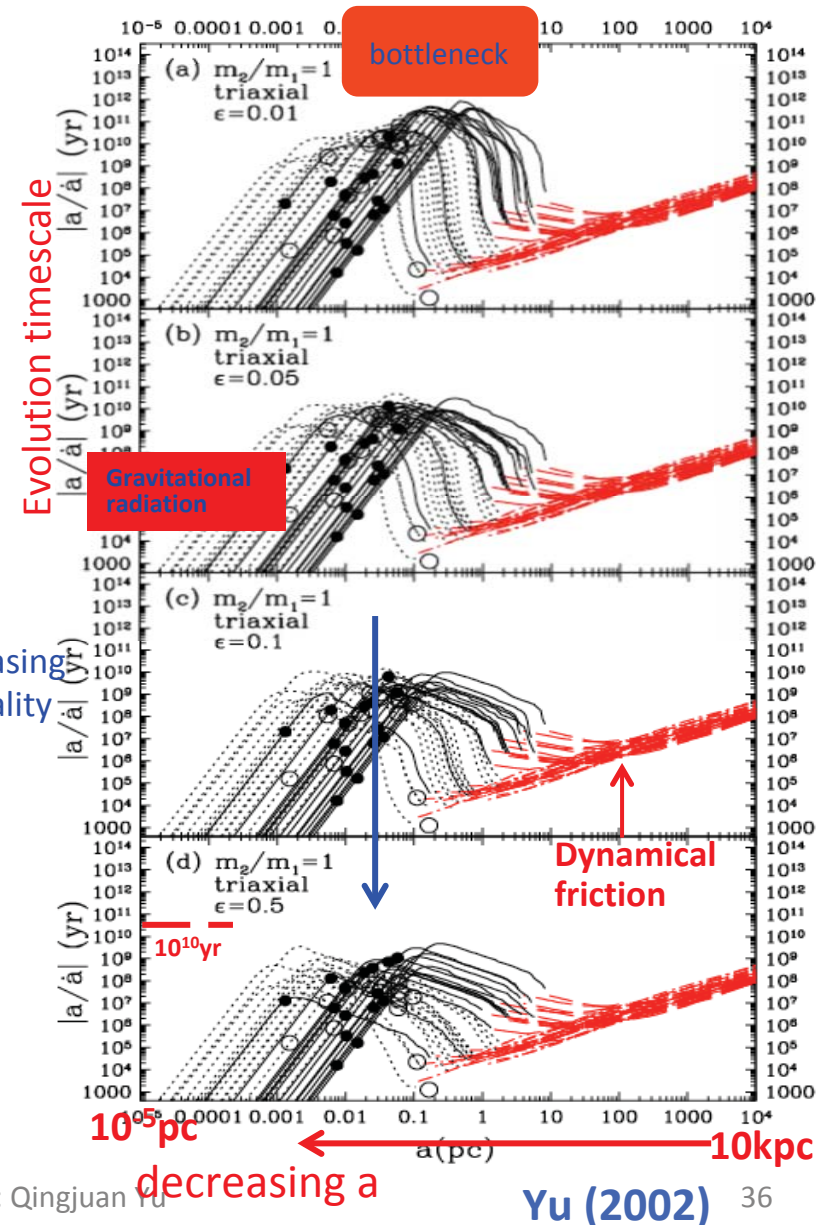
Are low- $J$  stars depleted before the gravitational radiation stage?

spherical:  $\rho(r)$

triaxial:  $\rho\left(\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2}\right)$

# Orbital evolution of massive BBHs: gas-poor mergers

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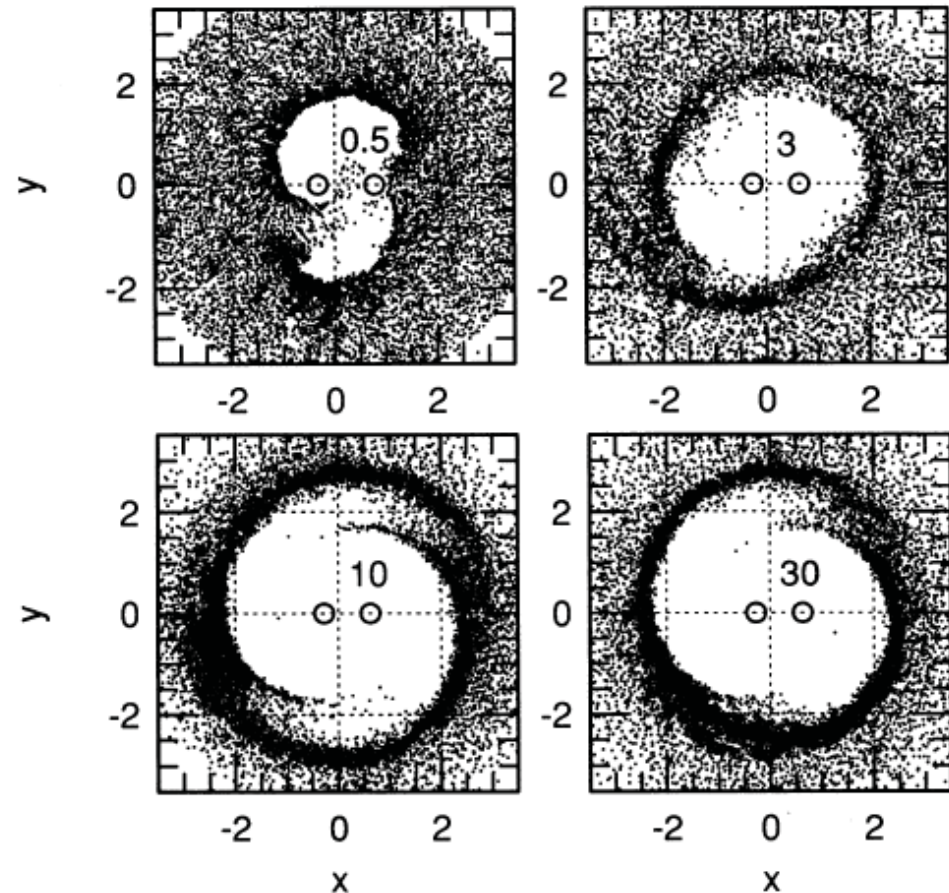
# Role of galaxy triaxiality

- Semimajor axis evolution
  - Decreasing bottleneck timescale
- Orbital orientation evolution
  - Alignment erasing effects in rotating systems

(Cui & Yu 2014)
- Eccentricity evolution
  - Decreasing eccentricity in counter-rotating systems

# Orbital evolution of binary MBHs: gas-rich mergers

- Dynamical friction stage (several kpc down to ten pc or pc scale)
- Gravitationally bound BBHs
  - Gas-rich mergers
    - Dynamical friction/migration to circum-nuclear gas reservoir (10-1pc-scale)
    - BBHs embedded in accretion (sub-pc-scale): **gap opening**
      - Viscosity driven;
      - Migration: similar to the type 2 migration of planets in planetary disks
- Gravitational wave radiation stage ( $\sim 10^{-2}$  pc scale)

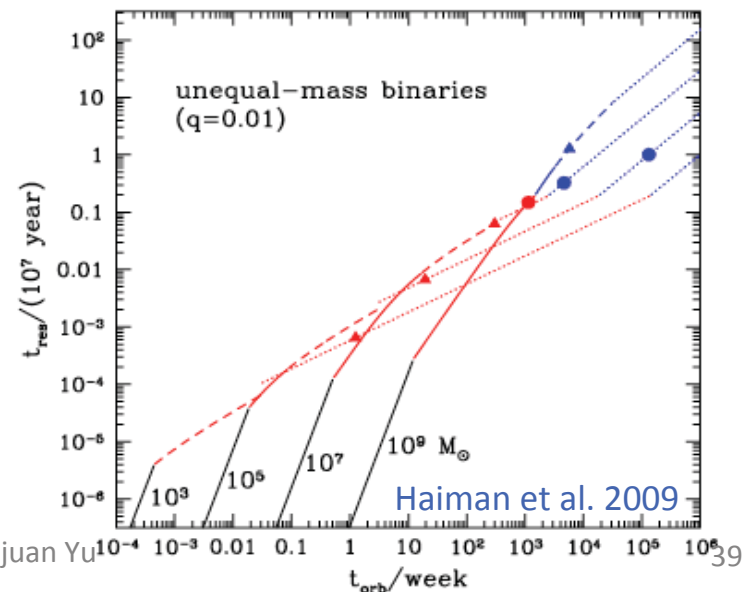
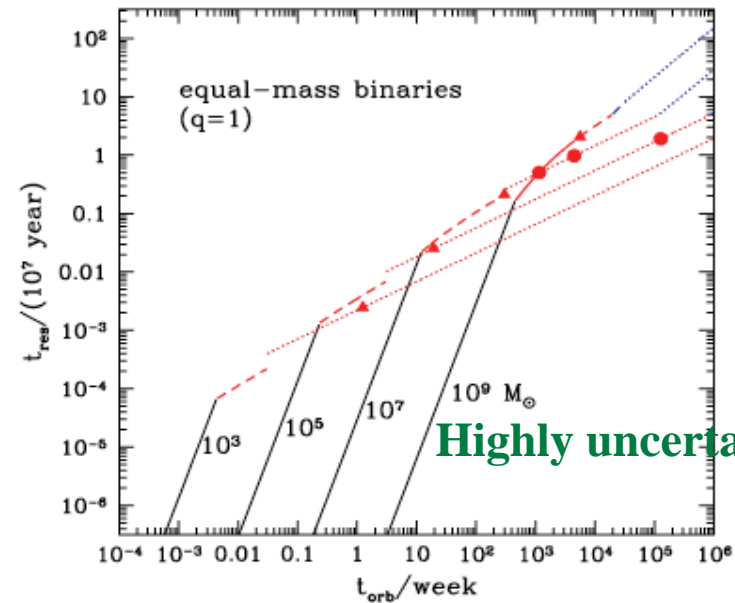


Goldreich & Tremaine 1979  
 Lin & Papaloizou 1979  
 Artymowicz & Lubow 1994  
 Artymowicz 1998



# Orbital evolution of massive BBHs: gas-rich mergers

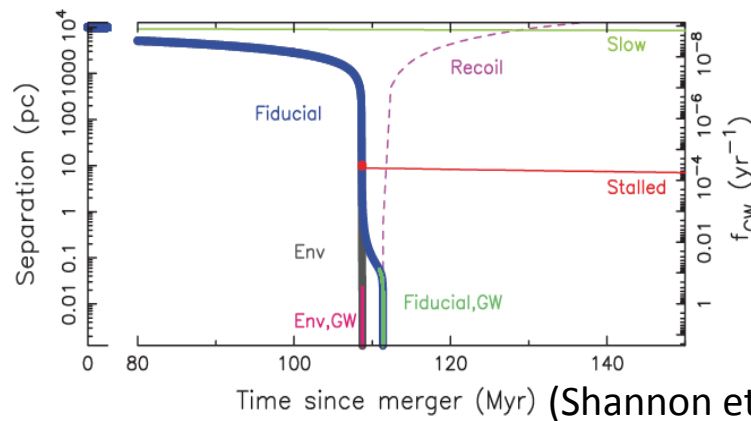
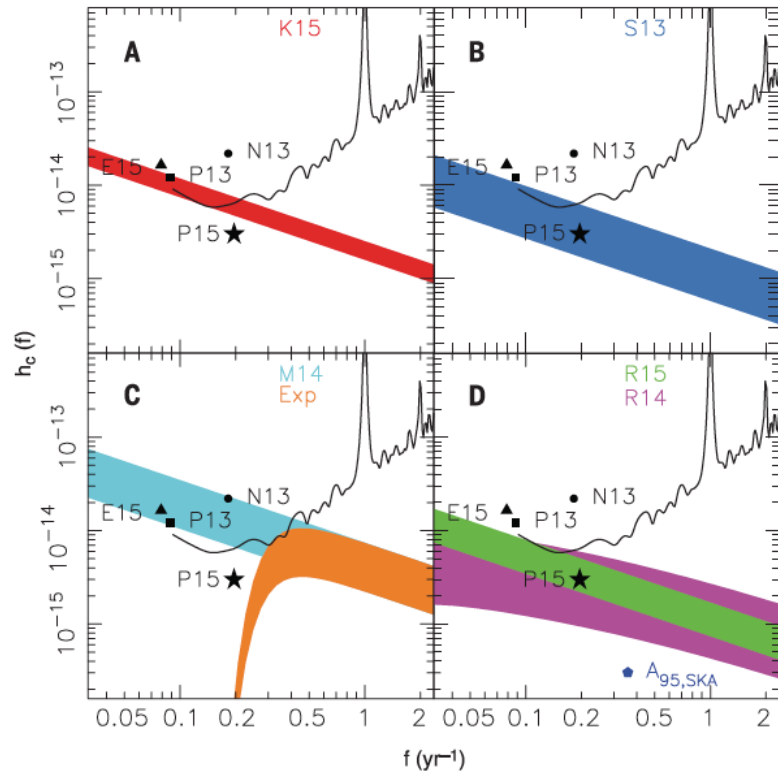
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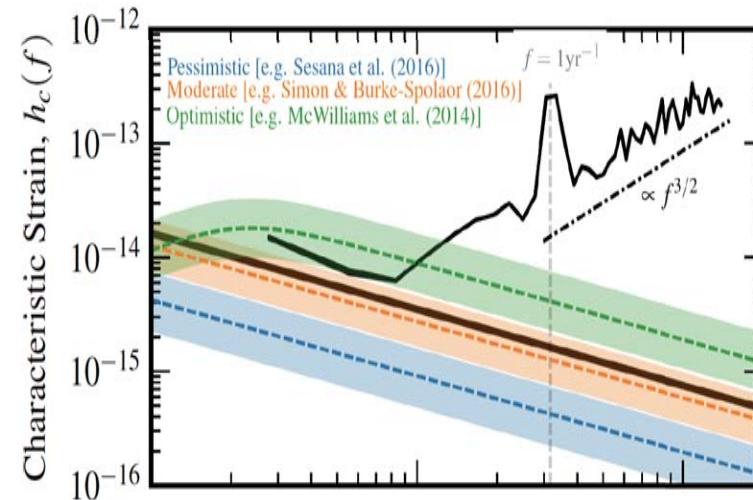
## Possible sources at the PTA bands

- Supermassive binary black holes
  - Stochastic backgrounds
  - Individual sources
- Cosmic strings
- QCD-scale phase transitions in the early universe

# Problems in *GWB* contributed by BBHs



- galaxy merger rates
- BH-galaxy properties relations
- BBH evolution
  - Hardening timescale

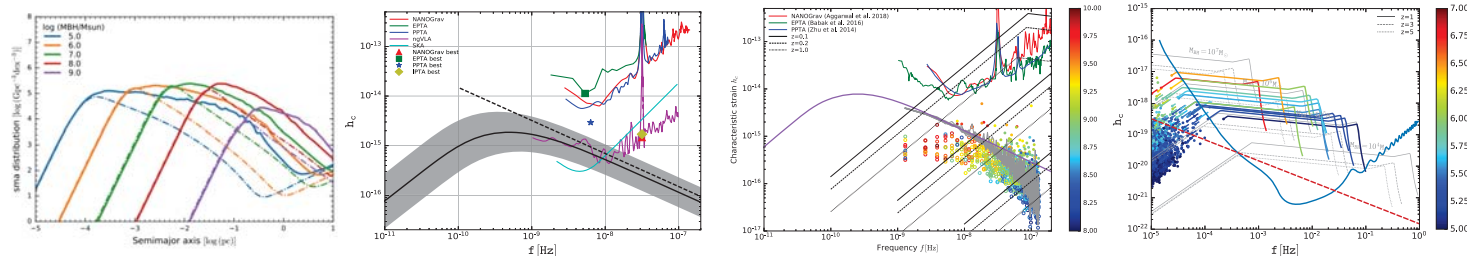


$$h_c(f) = A_{\text{GWB}} \frac{(f/\text{yr}^{-1})^\alpha}{(1 + (f_{\text{bend}}/f)^\kappa)^{1/2}}$$

(Arzoumanian et al. 2018)

# BBHs in realistic galaxy distributions

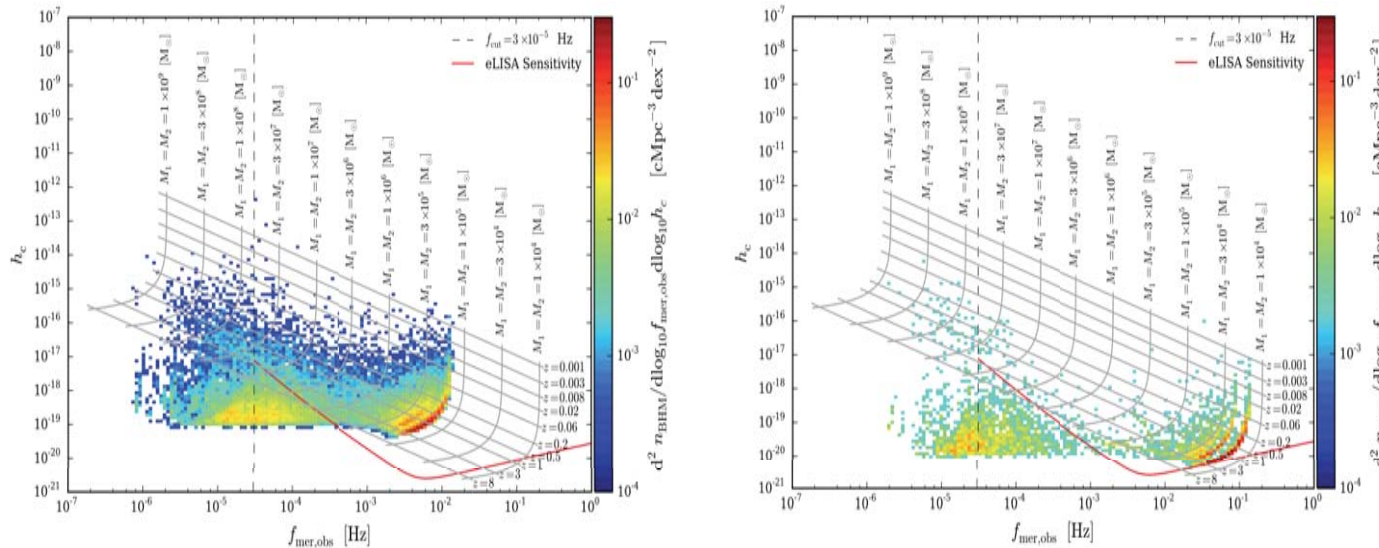
- Realistic intrinsic shape distributions
  - triaxiality
- Realistic light/mass distributions
- Distributions of surviving BBHs
- Expected stochastic GWB at PTA bands
- Prospects for GWs from individual sources
  - PTA bands
  - LISA bands (including EMRIs)



# BBH mergers at eLISA bands: depending on seeding BH models

EAGLE simulations, eLISA bands  
Different black hole seeding models

Seed black holes:  
Remnants of the first generation of stars  
Collapsing nuclear star clusters  
Direct collapse of supermassive stars

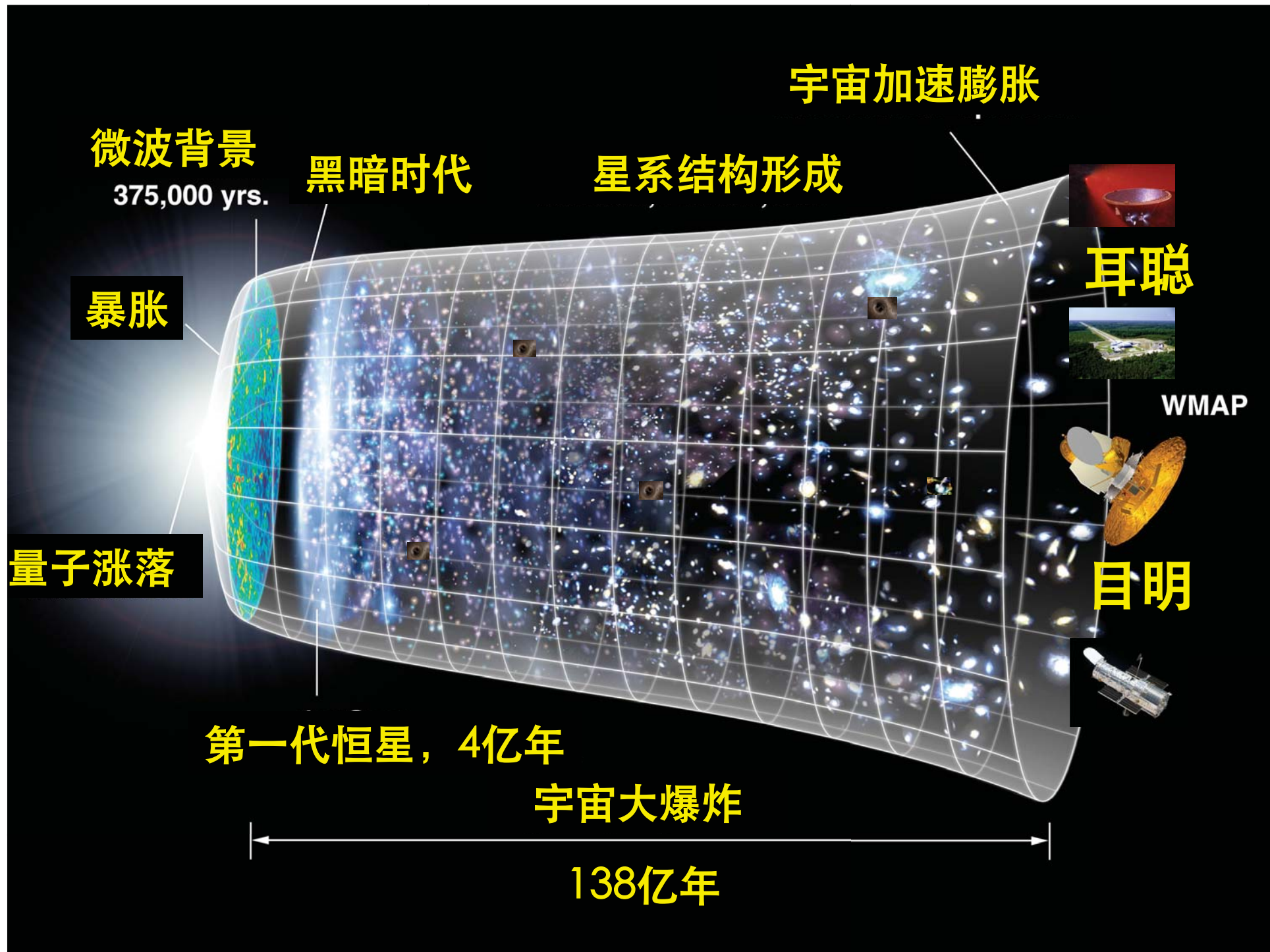


- Dominated by mergers between seed mass black holes merging at redshifts between  $z \sim 2$  and  $z \sim 1$ .
- Predicted event rate of GWs for the inspiral and merger phases:  $\sim 2$  events/year.



# Summary

- Massive binary black holes are natural products of galaxy mergers.
- Observational appearance of a BBH depends on the evolutionary stage of the BBH.
- Evolution of BBHs depends on BH masses, and velocity dispersions and shapes, and gas environment of host galaxies
  - Triaxiality: Overcoming evolution timescale bottleneck
- Evolution of BBHs in realistic galaxy distributions determines
  - Distribution of surviving BBHs
  - Strength of stochastic *GWB* from mergers of BBHs
    - compatible with current PTA observations and to be tested in the near future (FAST, ngVLA, SKA)
  - Mergers of individual sources (FAST, ngVLA, SKA, LISA), EMRIs (LISA)
- **Events: testing black hole physics, gravity theory in a new regime etc.**
- **Streng & Event rates: Probing structure formation and evolution, formation and evolution of BHs and galaxies**



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    - Supermassive at galactic centers
      - Evidence: AGNs & Nearby galaxies
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The luminosity function of QSOs as a function of redshift traces the accretion history of the local MBHs. (Soltan 1982)

- **Accreted:**

$L_{\text{bol}}$ : bolometric luminosity;

$\epsilon$ : mass-to-energy efficiency;

$\dot{M} = \frac{(1 - \epsilon)L_{\text{bol}}}{\epsilon c^2}$ : mass accretion rate;

$$\int_0^{t_0} dt \int_0^\infty dL \frac{(1 - \epsilon)L_{\text{bol}}}{\epsilon c^2} \psi(L, t)$$

$\psi(L, t)$ : QSO luminosity function

bolometric correction:  $L \rightarrow L_{\text{bol}}$ .

- **Local:**

$$\int_0^\infty M_0 n(M_0, t_0) dM_0$$

BH mass function

$n(M_0, t_0)$

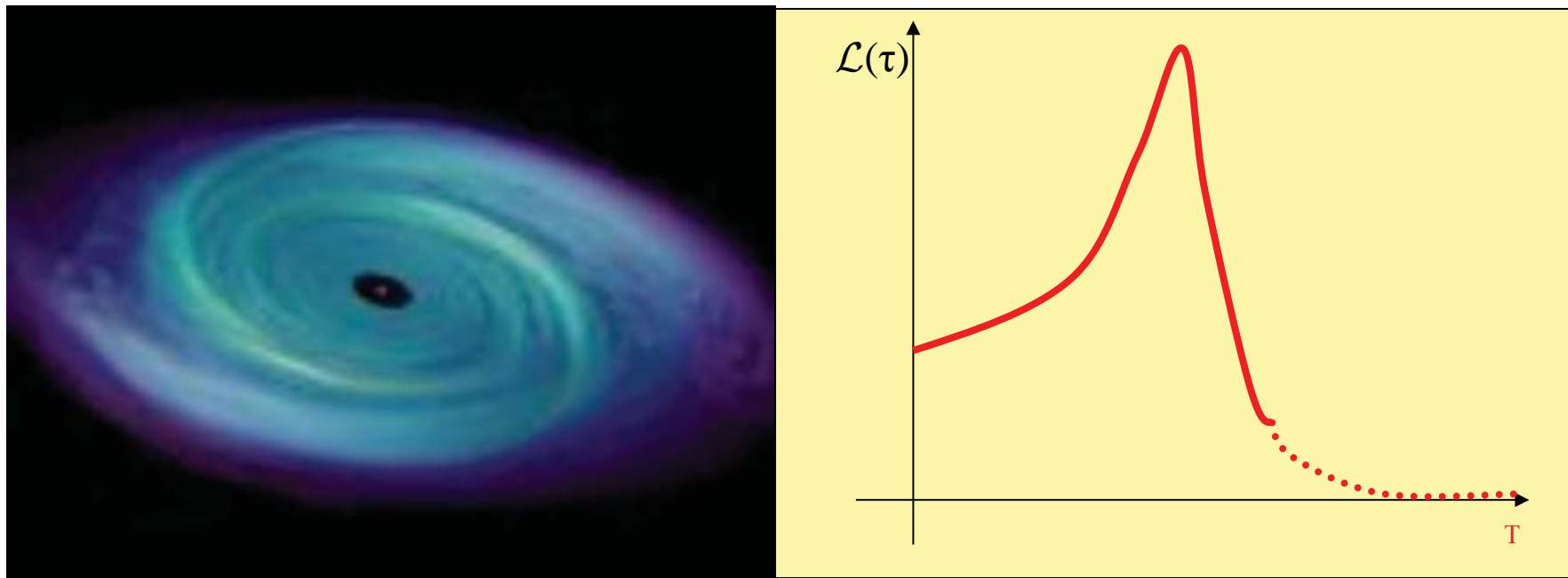
- BH mass M-sigma or M-L relation
- galaxy sigma or L distribution

Total local BH mass density is consistent with the expected density of QSO/AGN remnants if  $\epsilon \approx 0.1-0.3$ . (consistent with GR expectation)

Yu & Tremaine 2002; Marconi et al. 2004; Shankar et al. 2004, 2008;

Yu & Lu 2004, 2008; Merloni & Heinz 2008

- Mass growth of massive BHs comes mainly from accretion due to bright QSO phases. (Dark accretion ruled out.)
- How does the accretion/luminosity of individual QSOs evolve?



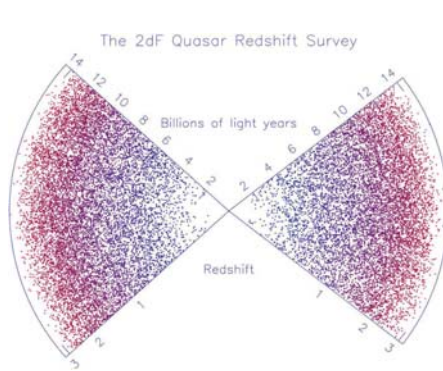
Evolution after the nuclear activity of a QSO/AGN is triggered

$$\dot{M}(\tau) = \frac{(1 - \epsilon)\mathcal{L}(\tau)}{\epsilon c^2}$$

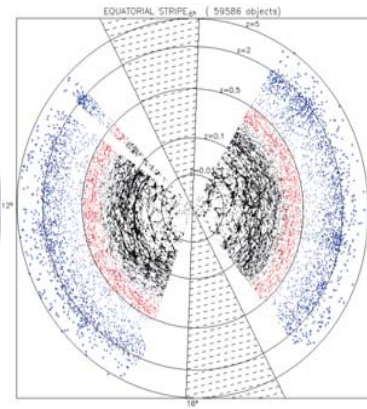
$$M(\tau) = M_i + \int_0^\tau \dot{M}(\tau') d\tau'$$



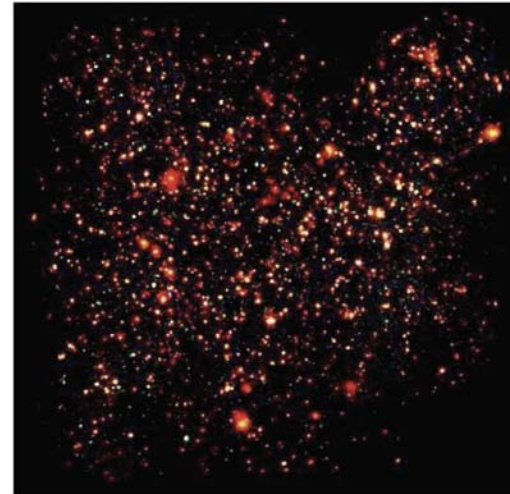
## Extracting evolution of accretion from observations



2dF



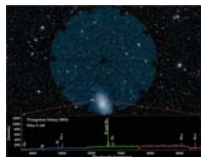
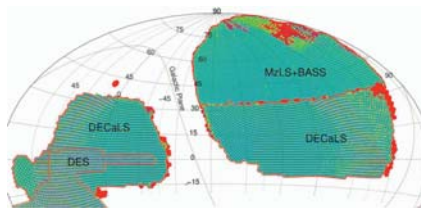
SDSS



X-ray  
survey

Statistical methods involving a large sample of QSOs/AGNs are required.

- A single AGN may only represent one specific period in a prolonged phase of nuclear activity.
- A large sample of AGNs with different ages will span all phases of this activity and allow us to extract information about evolution.



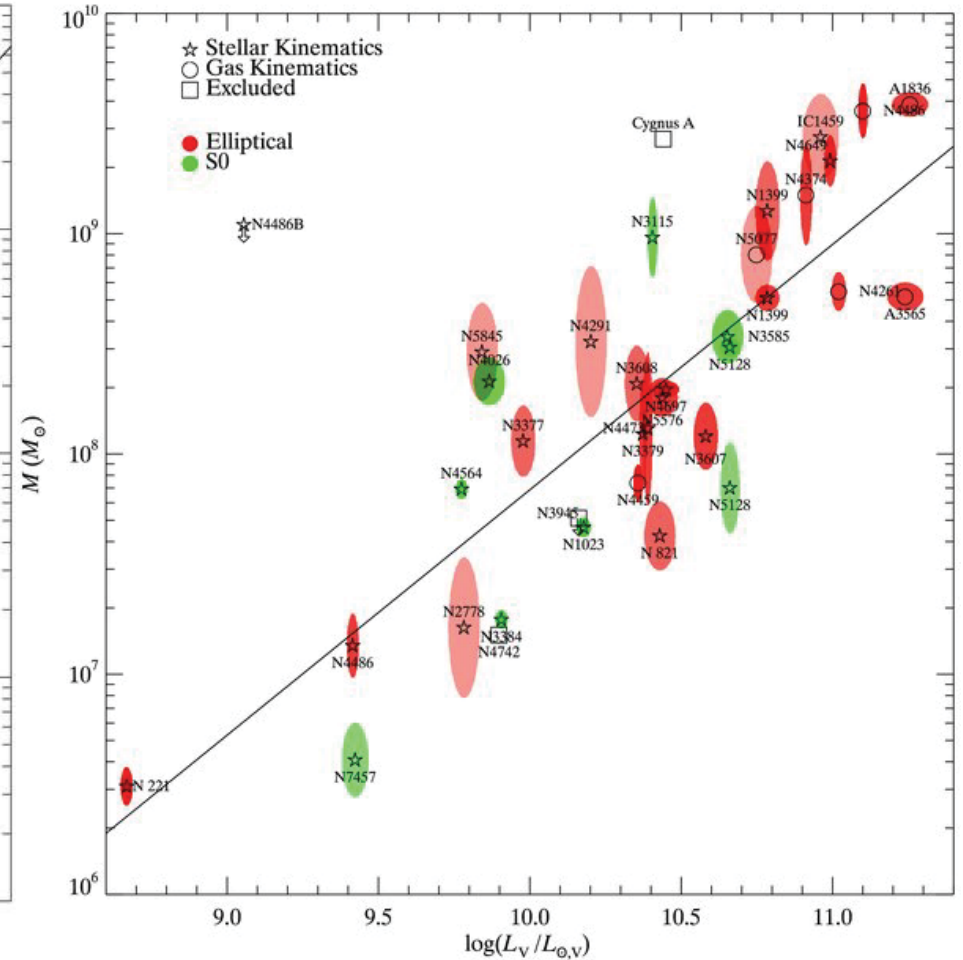
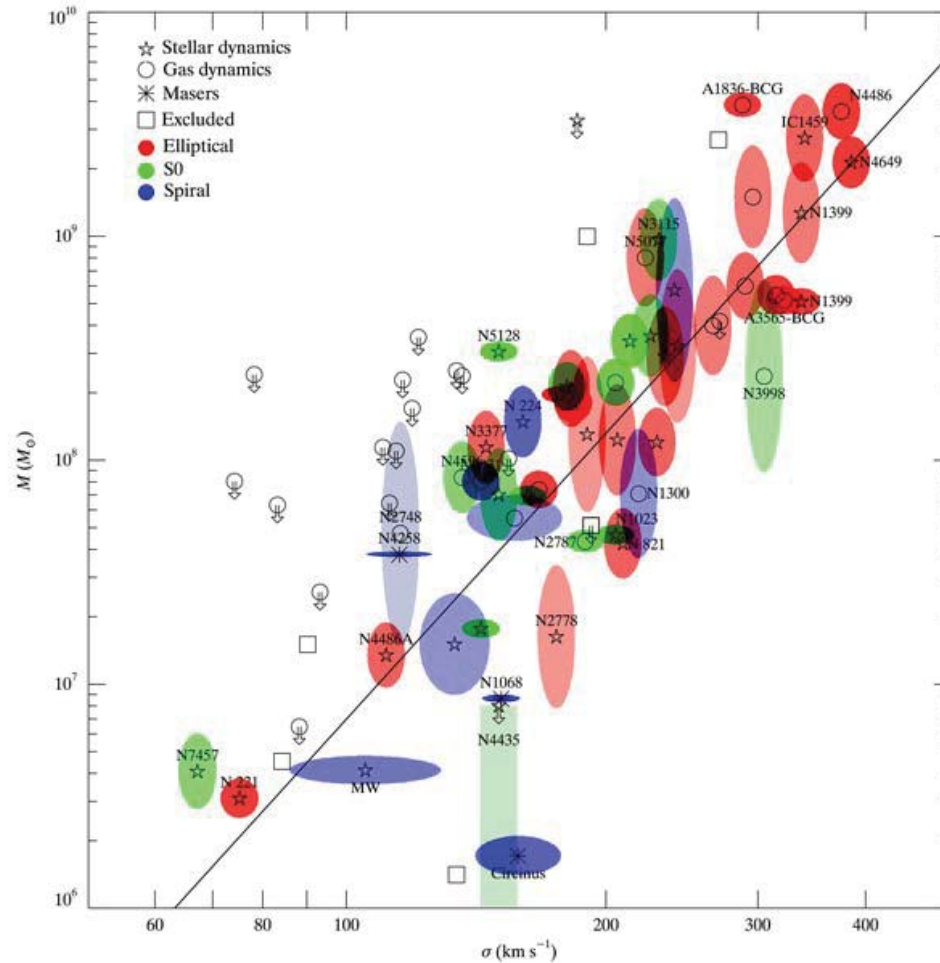
DESI



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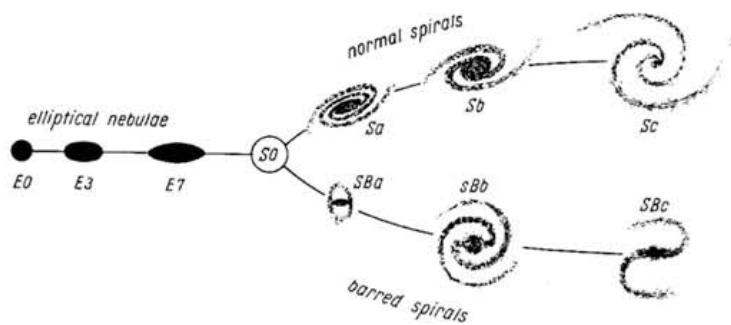
# Correlations between MBH masses and galaxy properties



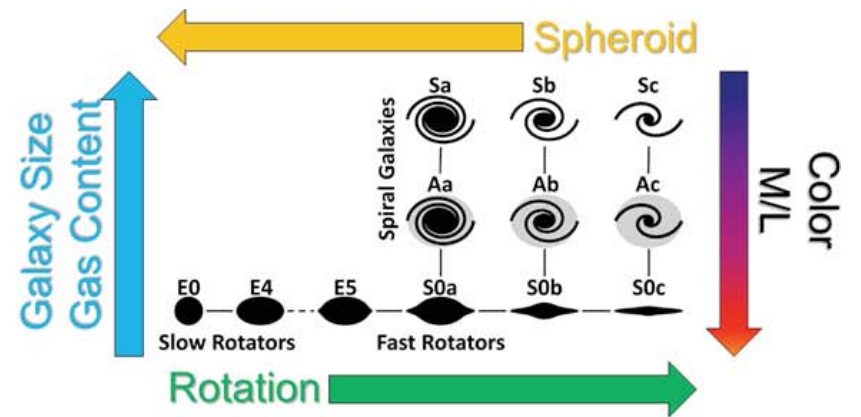
$$\log\left(\frac{M}{M_\odot}\right) = (8.12 \pm 0.08) + (4.24 \pm 0.41) \log\left(\frac{\sigma_e}{200 \text{ km s}^{-1}}\right)$$

$$\log\left(\frac{M}{M_\odot}\right) = (8.95 \pm 0.11) + (1.11 \pm 0.18) \log\left(\frac{L_V}{10^{11} L_{\odot,V}}\right)$$

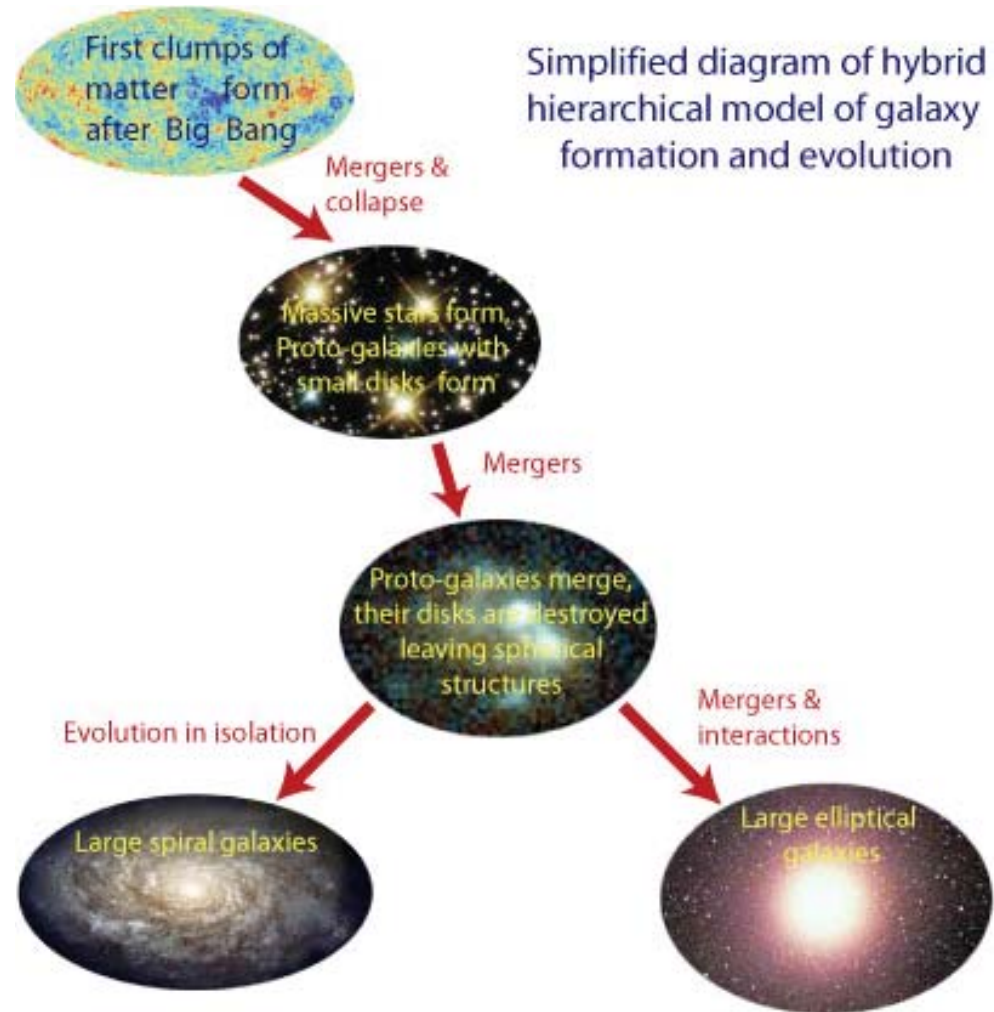
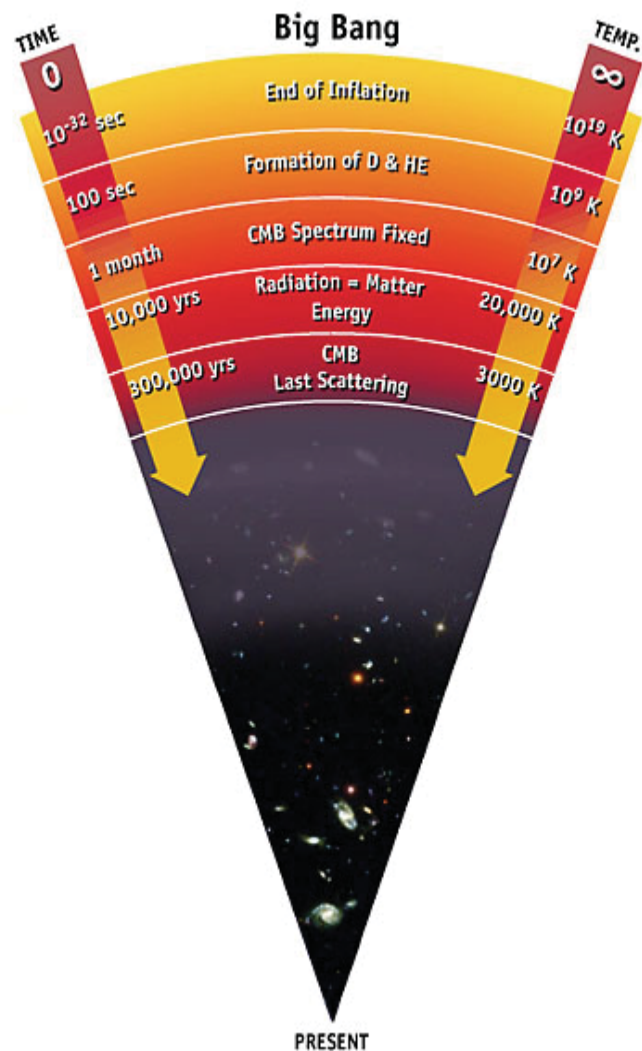
Gültekin et al. 2009



Hubble (1936) tuning fork



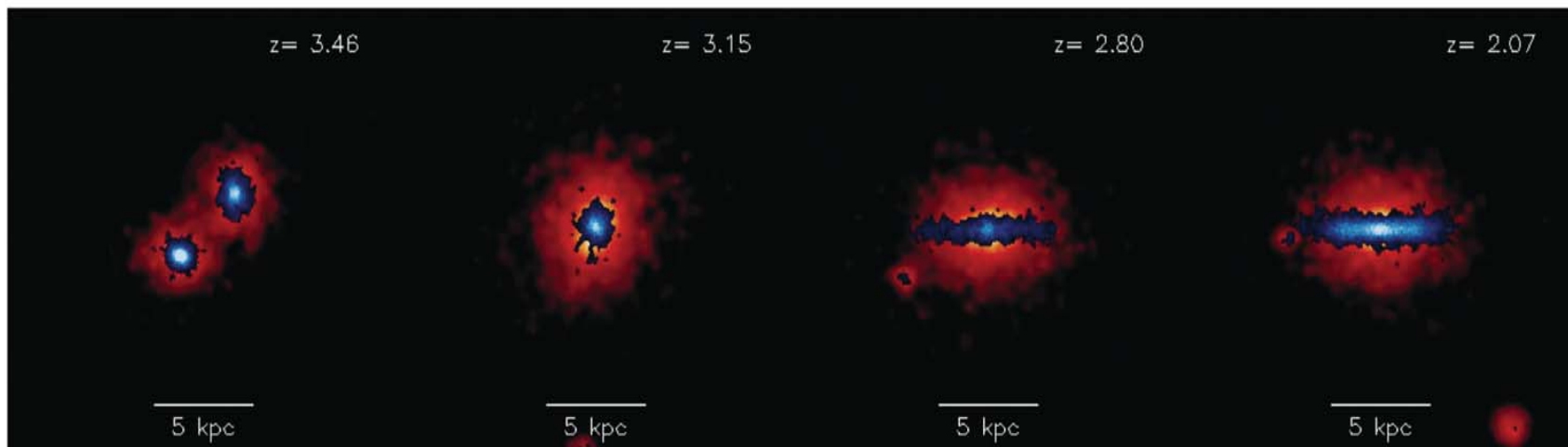
The ATLAS<sup>3D</sup> comb (2011)



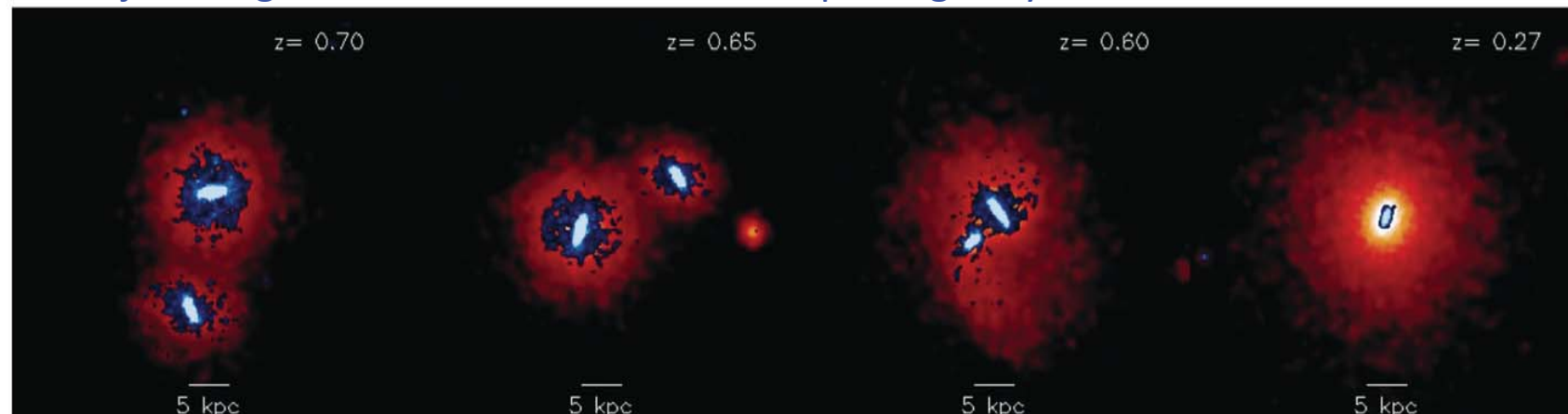


# Major mergers of galaxies: morphological and color transformation

The formation of bulge and rebirth of a disk



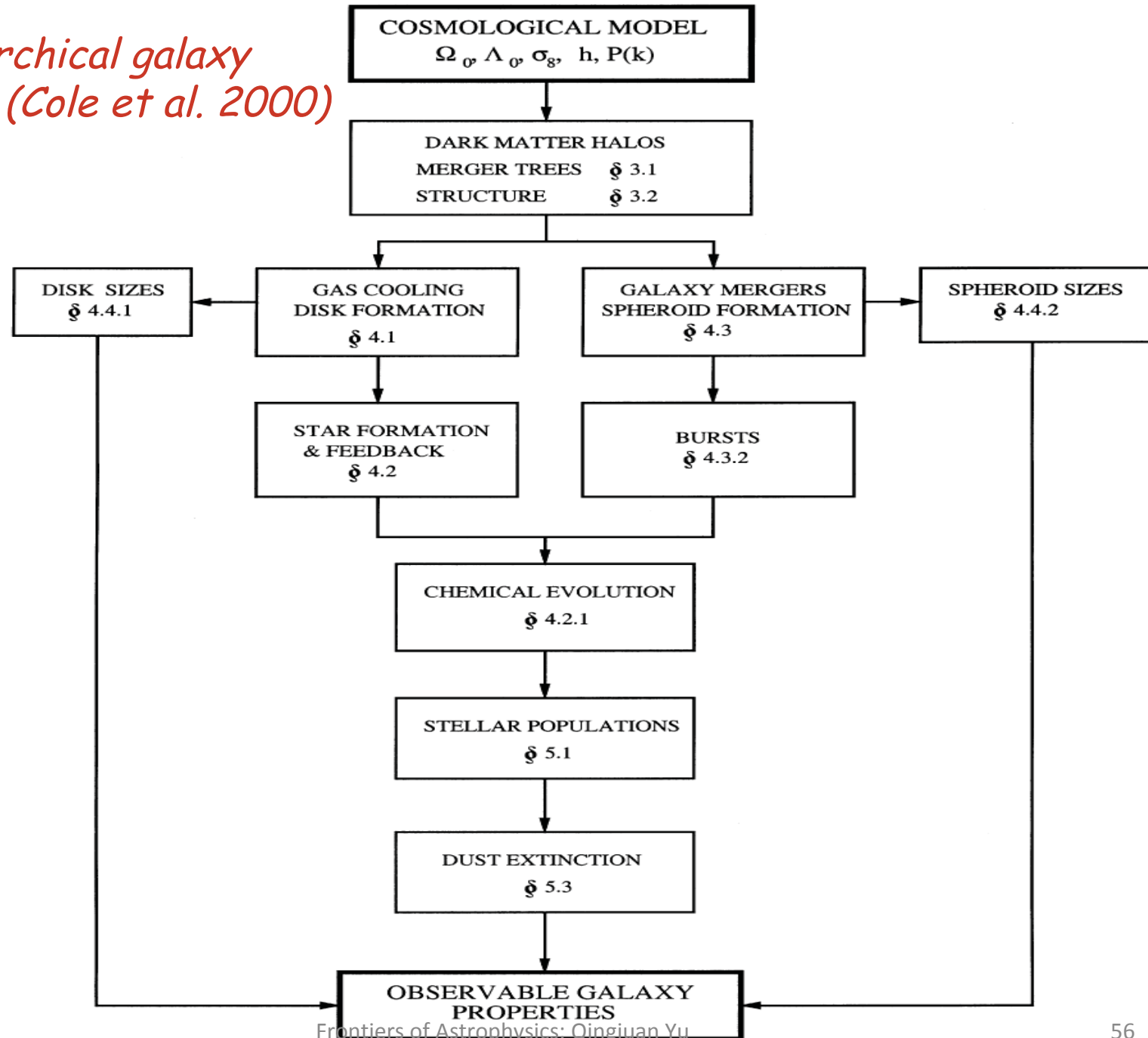
A major merger and the formation of an elliptical galaxy



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*Hierarchical galaxy  
formation (Cole et al. 2000)*



# Background: structure formation

- Press-Schechter mass function:
  - Halo mass distribution at a given cosmic time  $t$

$$\frac{dn(M, t)}{dM} dM = \left(\frac{2}{\pi}\right)^{1/2} \frac{\bar{\rho}_0}{M^2} \frac{\delta_c(t)}{\sigma(M)} \left| \frac{d \ln \sigma}{d \ln M} \right| \exp \left[ -\frac{\delta_c^2(t)}{2\sigma^2(M)} \right] dM$$

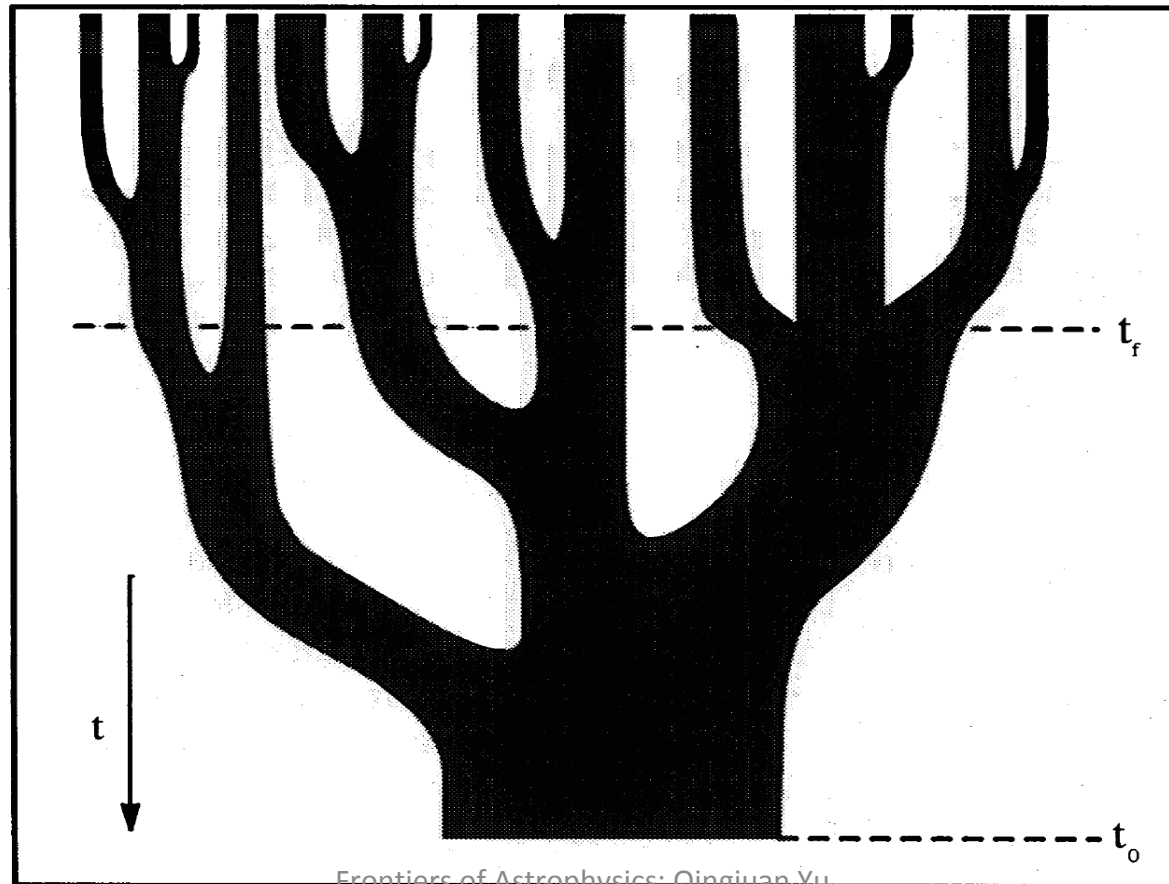
- Extended Press-Schechter mass function (conditional distribution mass function):
  - The fraction of mass in haloes of mass  $M_2$ , at time  $t_2$ , which at an earlier time,  $t_1$ , was in haloes of mass in the range  $M_1$  to  $M_1+dM_1$

$$f_{12}(M_1, M_2) dM_1 = \frac{1}{\sqrt{2\pi}} \frac{(\delta_{c1} - \delta_{c2})}{(\sigma_1^2 - \sigma_2^2)^{3/2}}$$

$$(M_1 < M_2) \times \exp \left[ -\frac{(\delta_{c1} - \delta_{c2})^2}{2(\sigma_1^2 - \sigma_2^2)} \right] \frac{d\sigma_1^2}{dM_1} dM_1$$

# Merger trees from conditional Mass distribution function

- Using Monte Carlo method (or directly using numerical simulations)





# Recipes for Galaxy formation

- Cooling of the hot gas in haloes

$$\tau_{\text{cool}} = \frac{3}{2} \frac{\rho_{\text{gas}}(r)}{\mu m_{\text{H}}} \frac{k_{\text{B}} T_{\text{gas}}}{n_{\text{e}}^2(r) \Lambda(T_{\text{gas}}, Z_{\text{gas}})} \quad (\text{example})$$

- Star formation from cold gas (formation of disk)

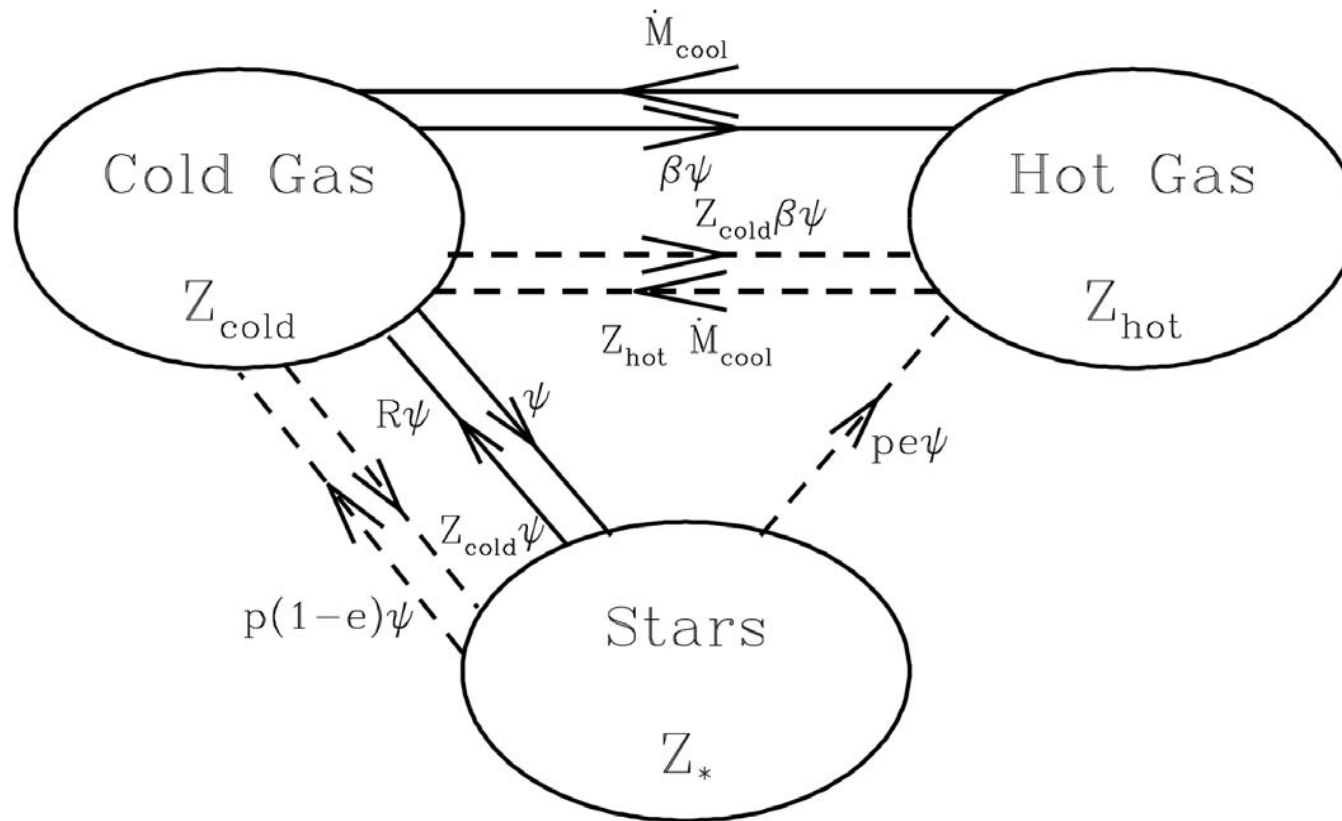
$$\psi = M_{\text{cold}} / \tau_{\star}$$

$$\tau_{\star} = \epsilon_{\star}^{-1} (V_{\text{disk}} / 200 \text{ km s}^{-1})^{\alpha_{\star}} \tau_{\text{disk}}$$

(example)

# Recipes for Galaxy formation

- Supernovae feedback, metal enrichment



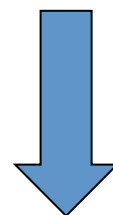
# Recipes for Galaxy Formation

- Galaxy merging
  - 1) dynamical friction

$$\tau_{\text{mrg}} = f_{\text{df}} \Theta_{\text{orbit}} \tau_{\text{dyn}} \frac{0.3722}{\ln(\Lambda_{\text{C}})} \frac{M_{\text{H}}}{M_{\text{S}}} \quad (\text{example})$$

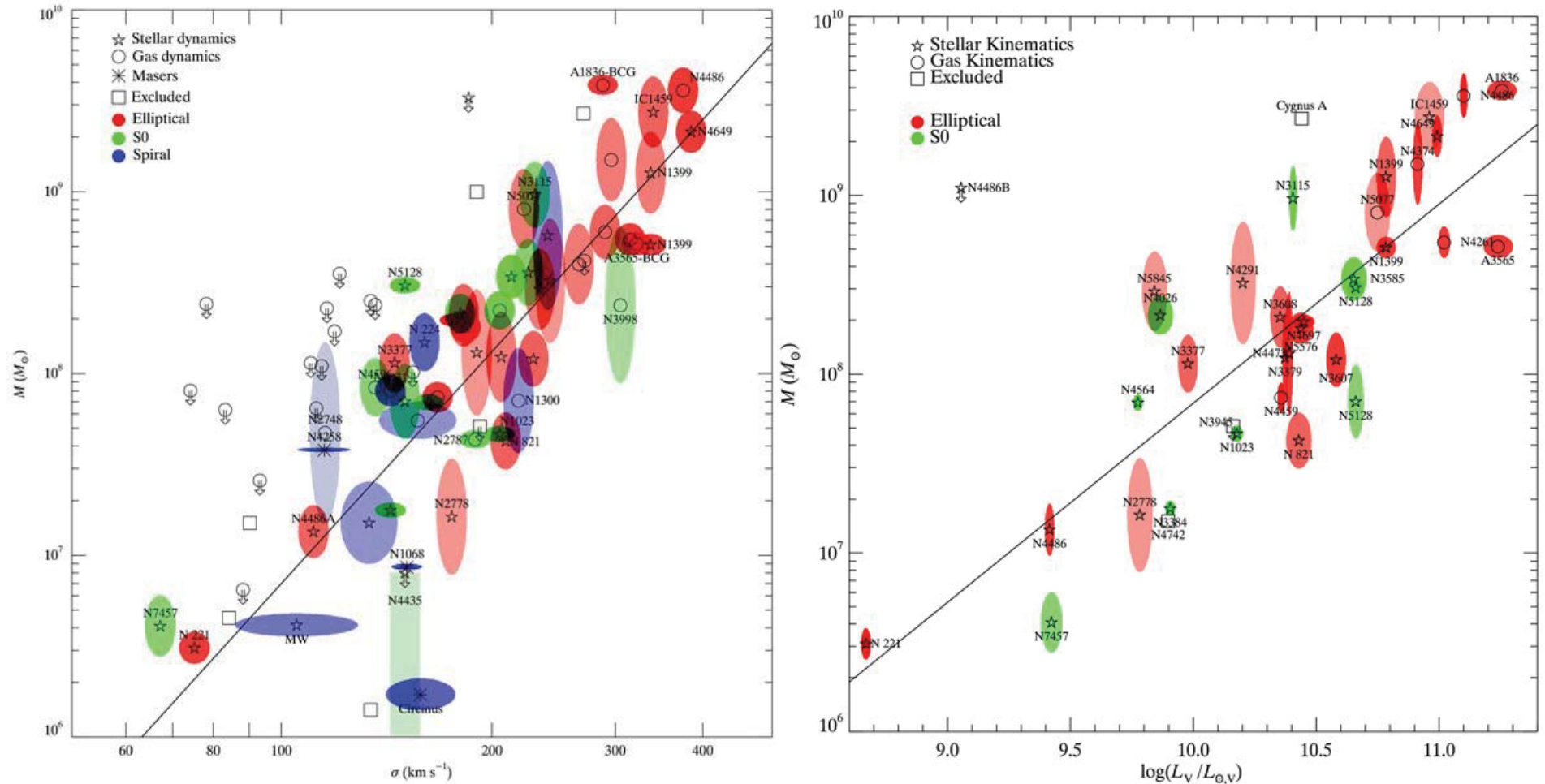
- 2) Spheroid formation (major mergers / minor mergers)  
disk and bulge size  
mainly determined by the angular momentum and  
mass in the formed stars; trigger star bursts

- Spectral synthesis model  
and dust extinction



Galaxies formed

# Correlations between MBH masses and galaxy properties



These correlations strongly suggest a close link between the formation and evolution of galaxies and their central BHs. What is the physical origin?

# AGN Feedback

- Relations between SMBH mass and velocity dispersion, bulge luminosity or bulge mass

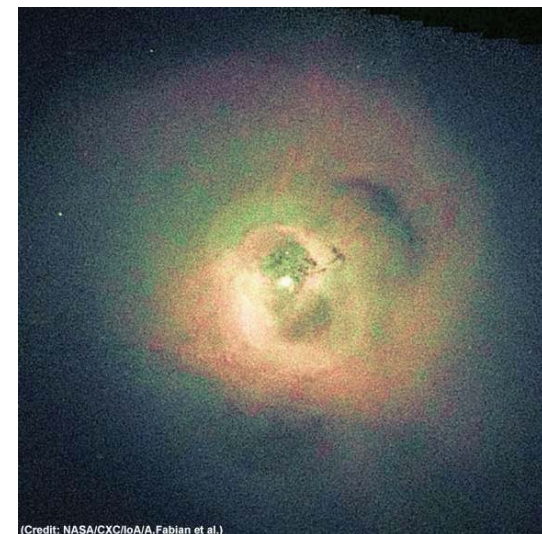
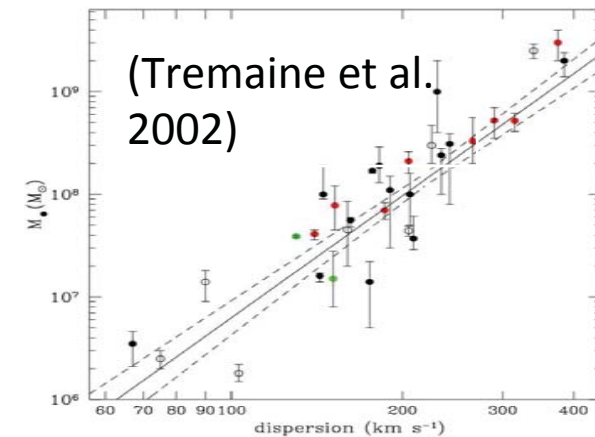
Total energy output from a QSO:

$$E_{\text{output}} \approx \epsilon M_{\bullet} c^2 \approx 10^{62} \left( \frac{\epsilon}{0.1} \right) \left( \frac{M_{\bullet}}{10^8 M_{\text{sun}}} \right) \text{erg}$$

Total bounding energy of the galaxy:

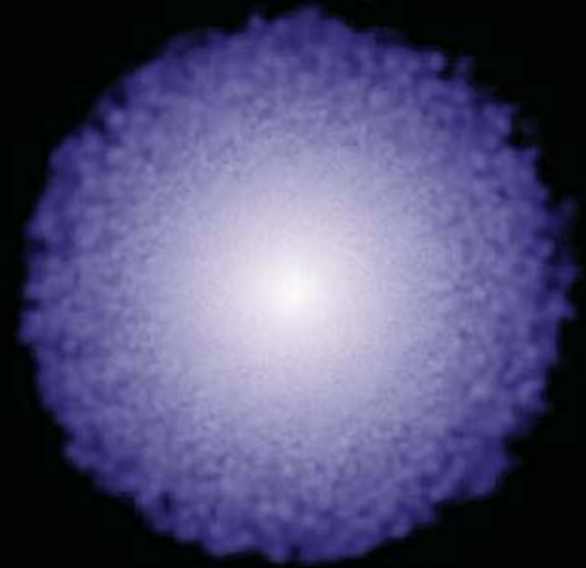
$$E_{\text{binding}} \approx C M_{\text{Gal}} \sigma^2 \approx 10^{60} \left( \frac{C}{1} \right) \left( \frac{M_{\text{Gal}}}{10^{12} M_{\text{sun}}} \right) \text{erg}$$

Even a small fraction of QSO energy incorporated into galactic medium may expels all the medium out of the galaxy





T = 0 Myr



12/19/19

Frontiers of Astrophysics: Qingjuan Yu

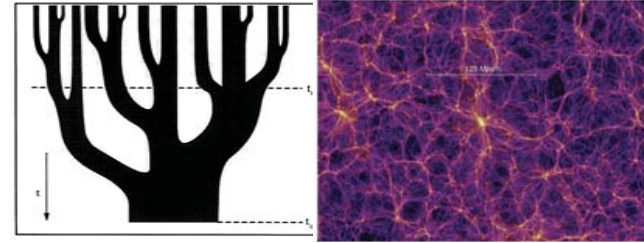
10 kpc/h



64

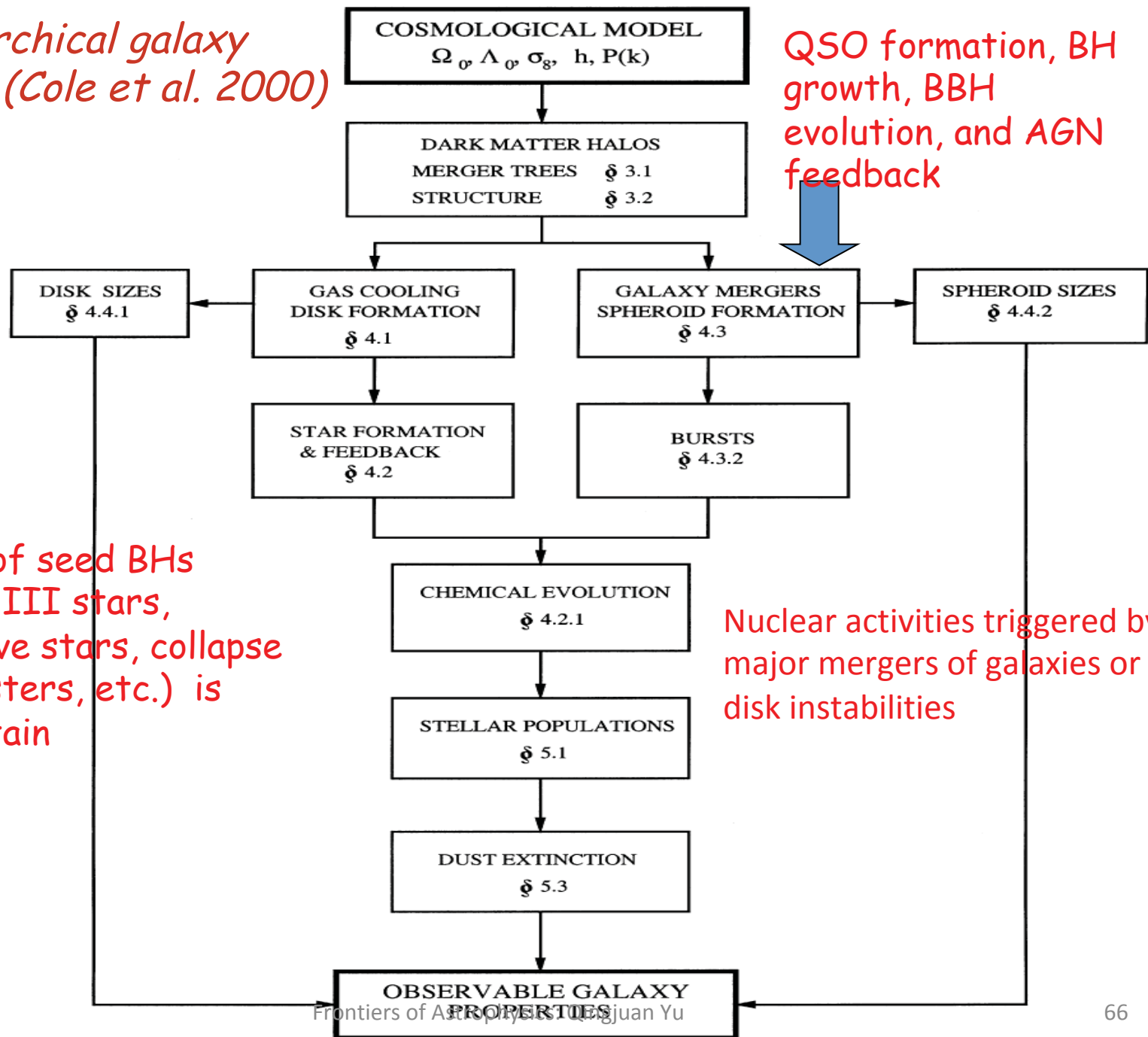
# Formation and evolution of BHs and galaxies

- Structure formation: halo merger tree
- Recipes for galaxy formation
- Recipes for formation and evolution of BHs and QSOs, gas accretion
  - QSOs: triggered by major mergers of galaxies/halos or disk instability
  - BH growth: BH mergers + gas accretion during major mergers of galaxies/halos or disk instability
  - AGN feedback: suppressing star formation and BH growth (QSO mode & Radio mode)
  - Seed BH formation and dynamics of BBHs and triple BH interaction
- Model output
  - QSO luminosity function, BH mass function, SFRs, galaxy properties etc.
  - BBHs, binary quasars/dual AGNs, wandering BHs in halos, BHs in IGM



Involving many uncertain parameters and assumptions (though some even controversial). Any progress in the mechanisms involved may help to improve the understanding.

*Hierarchical galaxy formation (Cole et al. 2000)*



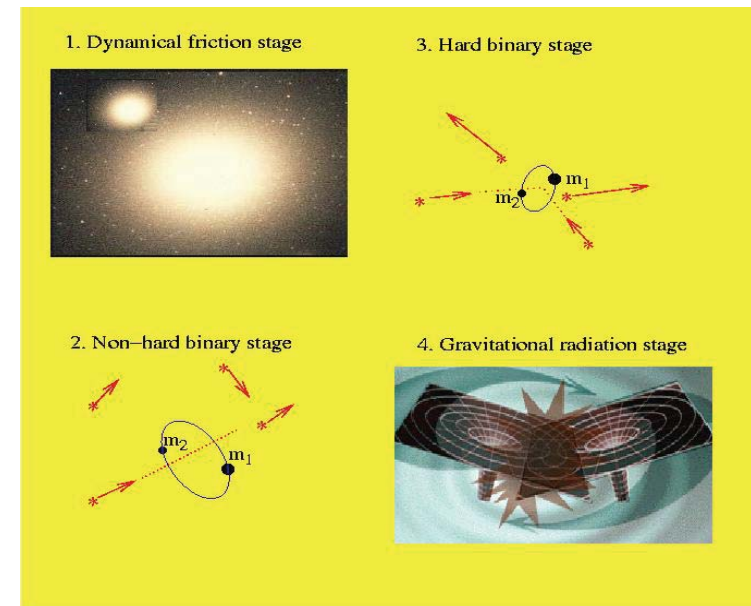
QSO formation, BH growth, BBH evolution, and AGN feedback

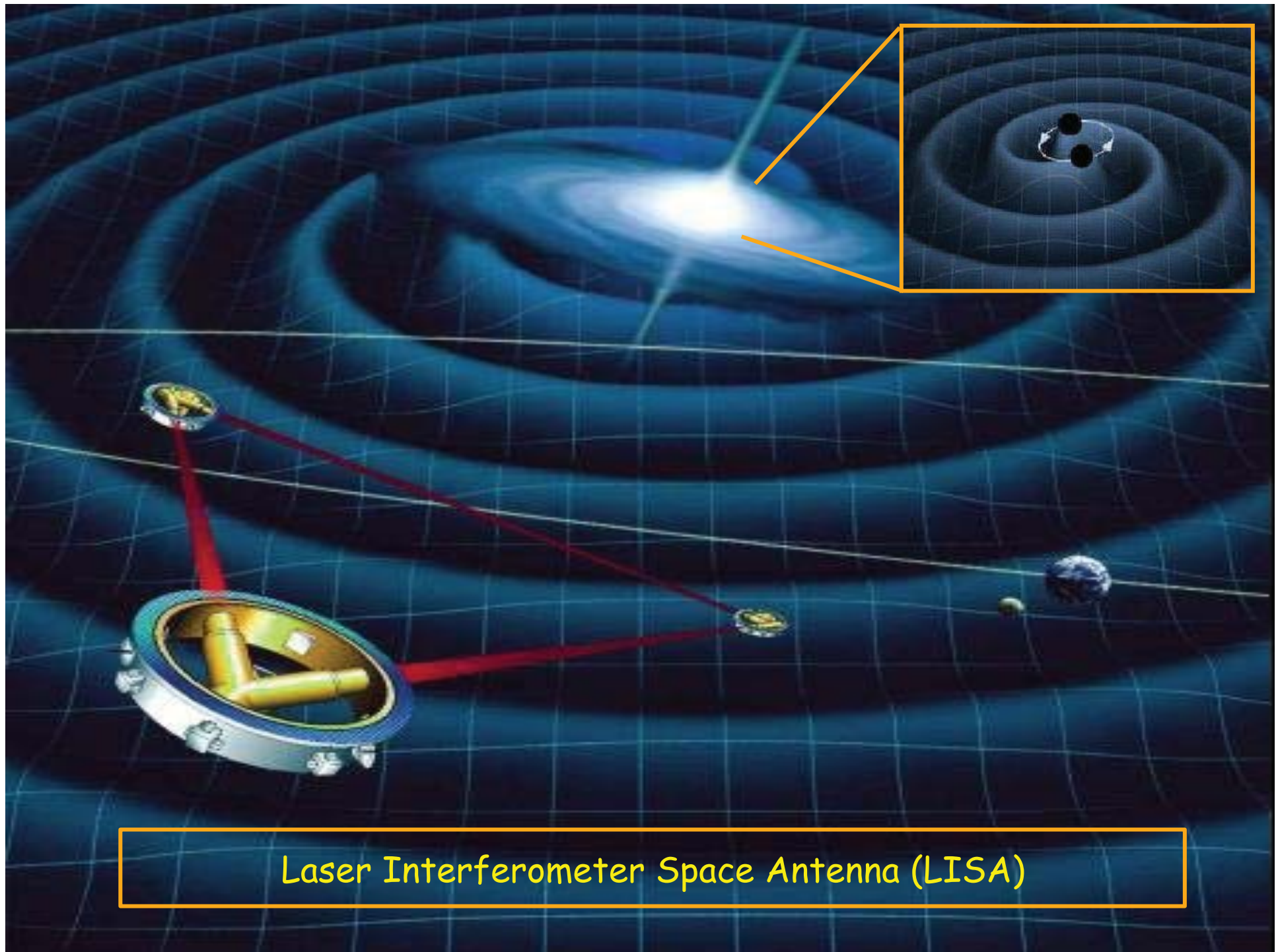
Formation of seed BHs (population III stars, supermassive stars, collapse of star clusters, etc.) is very uncertain

Nuclear activities triggered by major mergers of galaxies or disk instabilities

# Seed BHs and dynamics of BBH evolution

- Seed BHs:
  - Mass, redshift, over-density of haloes (little effect if the mass of seed BHs is small)
- BH mergers?
  - Dynamical evolution of BBHs
    - BH masses
    - Velocity dispersions, shapes, stellar densities of galaxies
    - Amount of gas in galactic nuclei
  - Three-body interactions of BHs (gravitational slingshot)
    - scattering or exchange
  - Recoil by gravitational radiation
  - Products of BH mergers

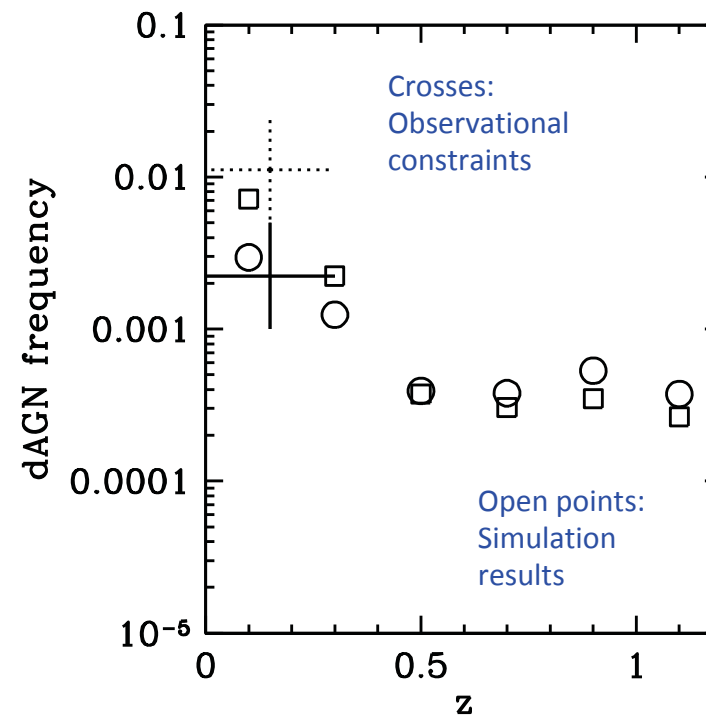
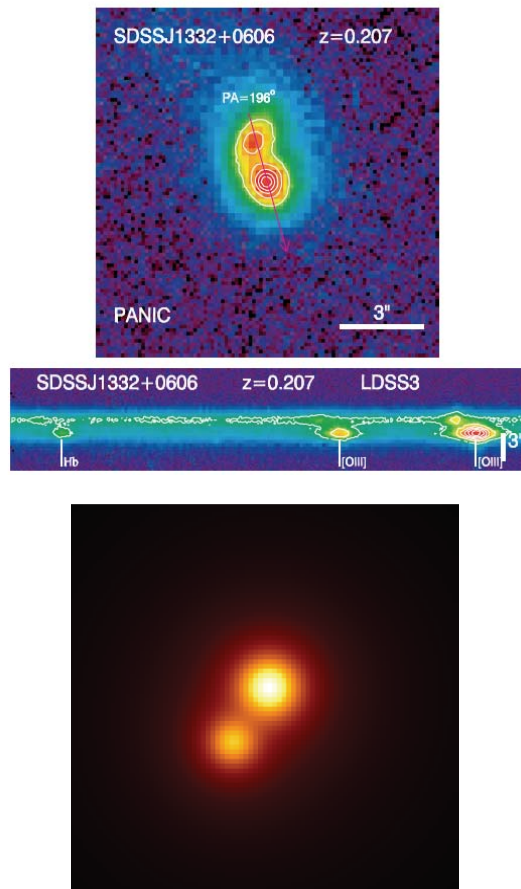




Laser Interferometer Space Antenna (LISA)




## Dual AGNs: frequency consistent with major merger rates of galaxies?



(Yu et al. 2011)

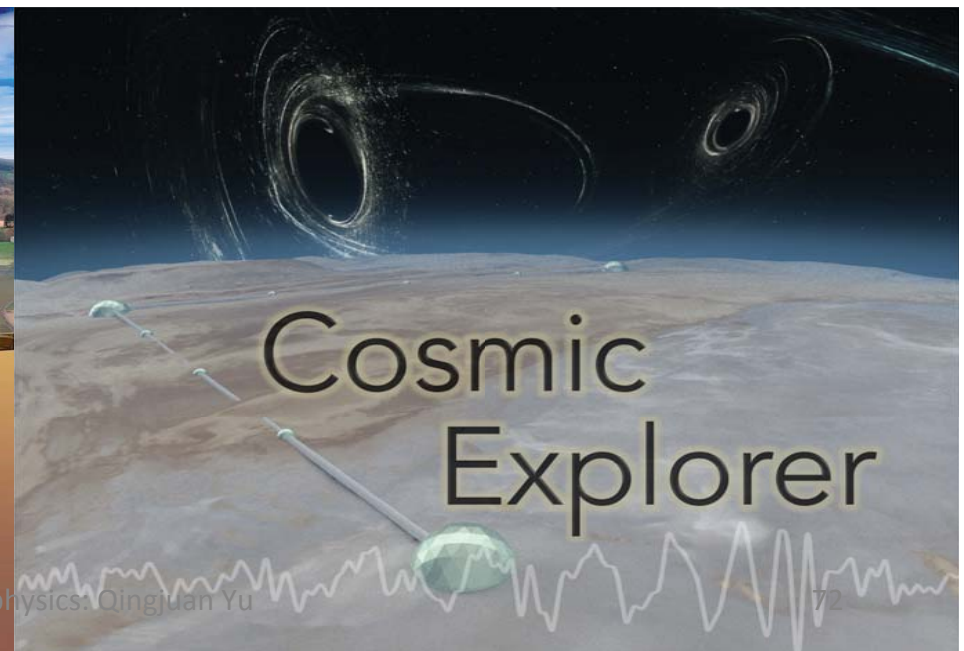
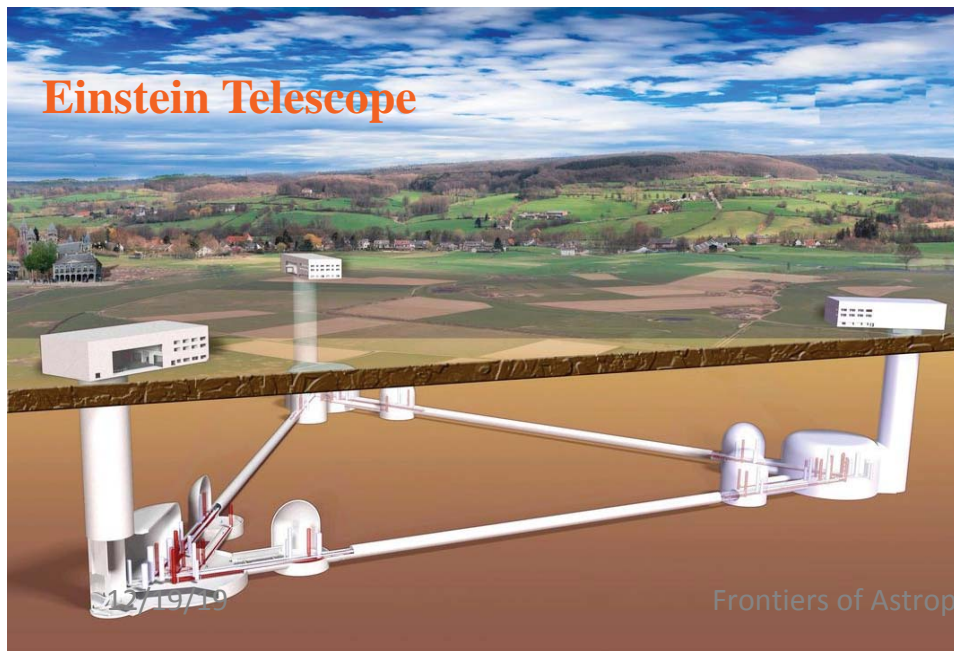
# Summary

- We are entering an epoch to learn the formation and evolution of massive BHs from large observational samples and understand the role of BHs in the framework of galaxy formation and evolution and in the cosmological context.
- The semi-analytical model provides a framework for understanding the co-evolution of galaxies and SMBHs and can well explain many current observations, although involving many assumptions.
- Further progress in the mechanisms involved may help to improve the understanding.
- GW detection results  insights on the model components
  - Massive stellar-mass BHs at LIGO band
  - GWR at PTA, LISA bands?
  - ....

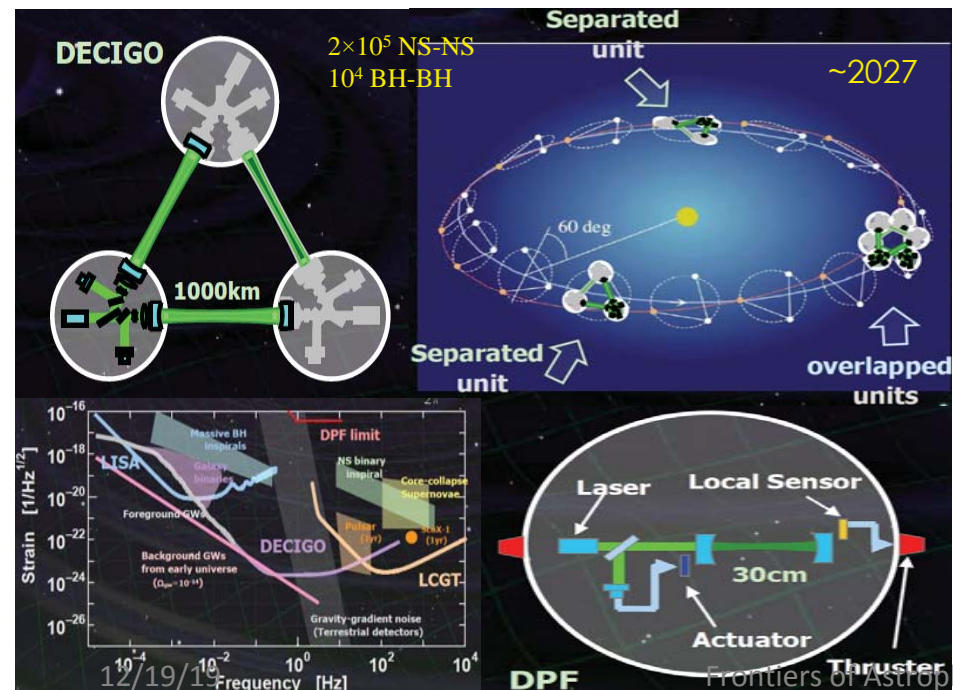
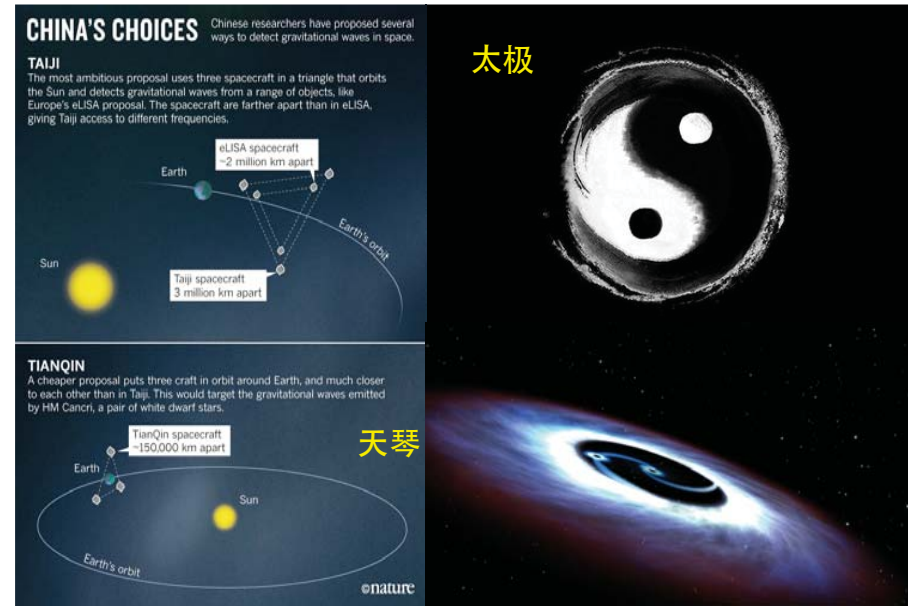
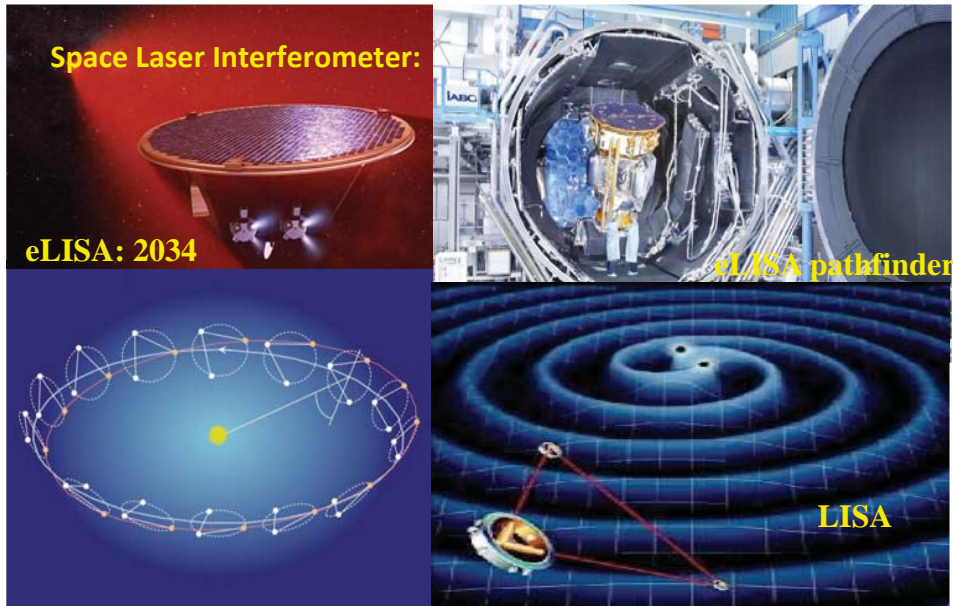
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Caption: CSIRO's Parkes radio telescope. Credit: David McClenaghan, CSIRO



# Big Questions

- 黑洞自旋及其演化？
- ~~引力波存在？~~ 新发现、新现象？
- 引力的本质？
- 宇宙中其它类型物态、天体？
- 宇宙的创生？

# Summary

- A new/great era to learn gravitational physics,
- A new/great era to re-learn astrophysics

- New insights for connection between math, physics, and astronomy?
- Huge stimulations for technology developments

- Interdisciplinary field

Fascinating  
Challenging  
Exciting  
Revolutionary?!

Thank You!

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